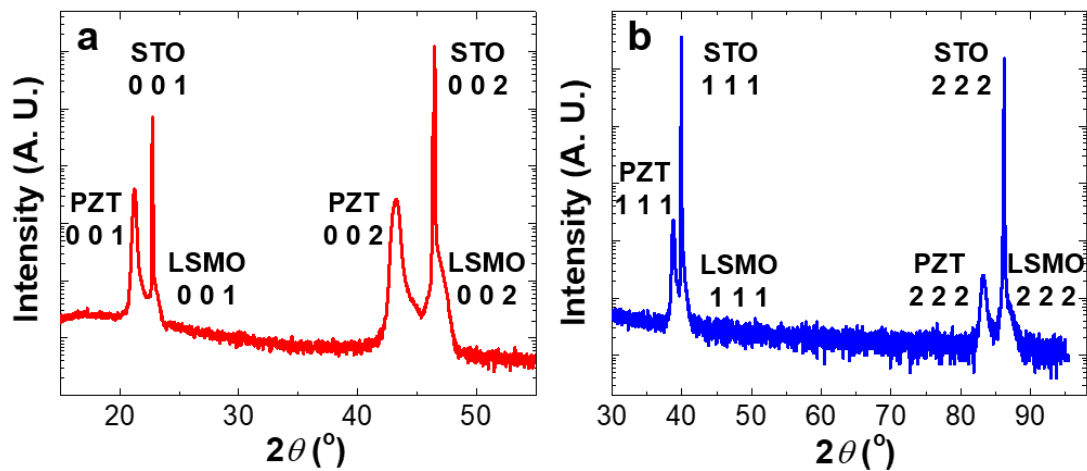


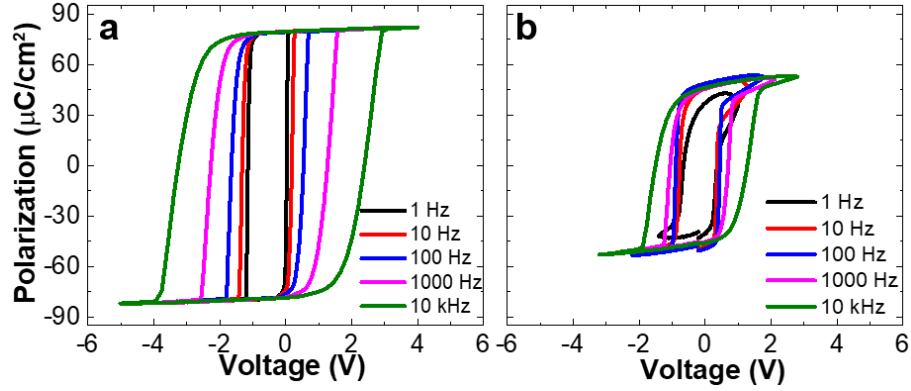
Supplementary Information

Tunable, Multi-state Switching in Ferroelectric Thin Films

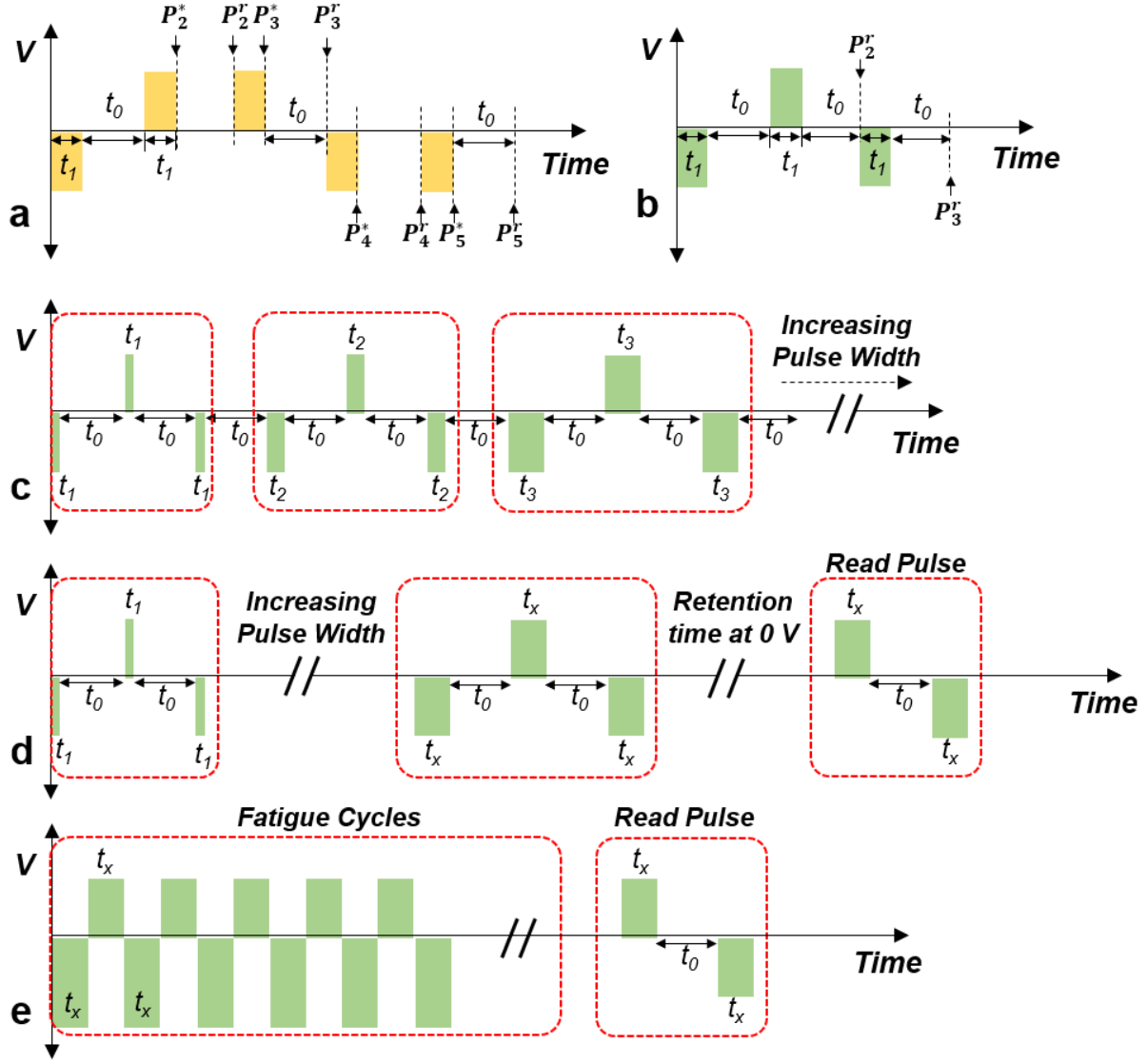
R. Xu *et al.*



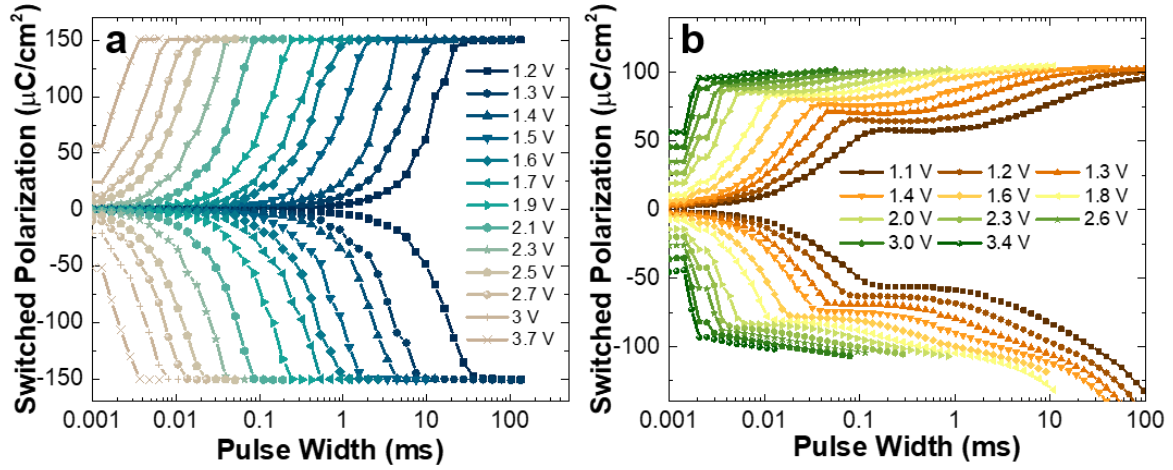
Supplementary Figure 1 | X-ray diffraction analysis. Wide-angle, θ - 2θ X-ray diffraction scans for **a**, (001)- and **b**, (111)-oriented $\text{PbZr}_{0.2}\text{Ti}_{0.8}\text{O}_3/\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3/\text{SrTiO}_3$ heterostructures. These results reveal that $\text{PbZr}_{0.2}\text{Ti}_{0.8}\text{O}_3$ films are epitaxial and single-phase.



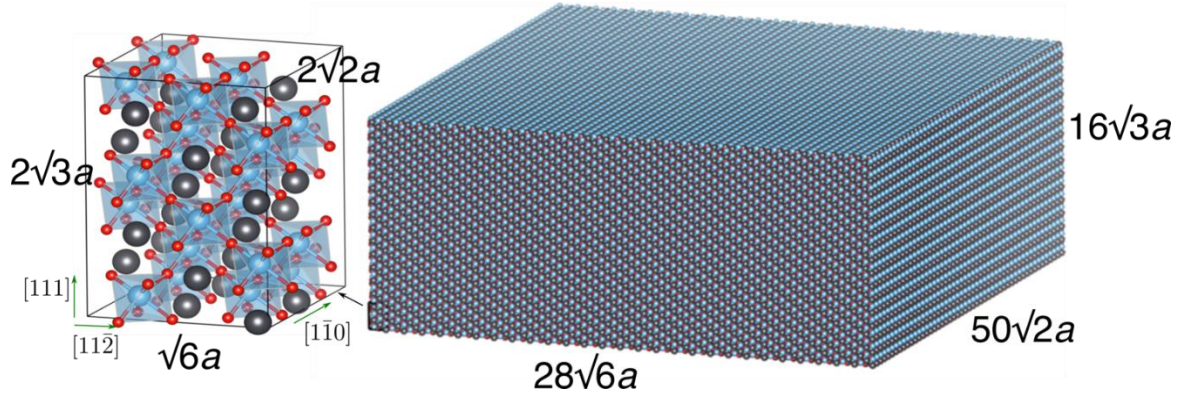
Supplementary Figure 2 | Ferroelectric hysteresis loop measurement. Ferroelectric hysteresis loops measured as a function of frequency for **a**, (001)- and **b**, (111)-oriented $\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3/\text{PbZr}_{0.2}\text{Ti}_{0.8}\text{O}_3/\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3/\text{SrTiO}_3$ capacitor structures. These films exhibit symmetric, well-saturated hysteresis loops that are maintained down to at least 1 Hz indicating low leakage and excellent ferroelectric properties.



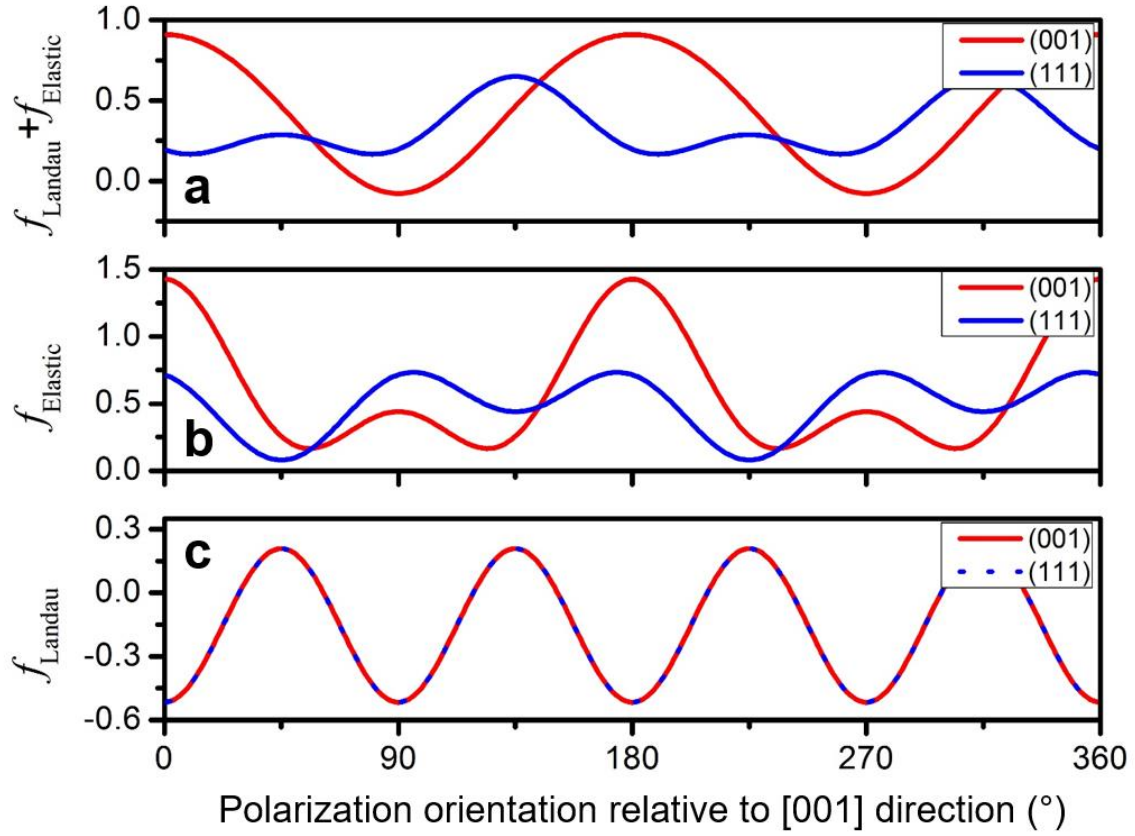
Supplementary Figure 3 | Pulse sequences used in the pulse-switching measurements. **a**, The pulse sequence used in conventional positive-up-negative-down (PUND) measurements. **b**, The modified PUND pulse sequence used in our measurements. **c**, The modified PUND measured as a function of pulse width for constant pulse voltages. **d**, The pulse sequence used in retention measurement. **e**, The pulse sequence used in fatigue measurement.



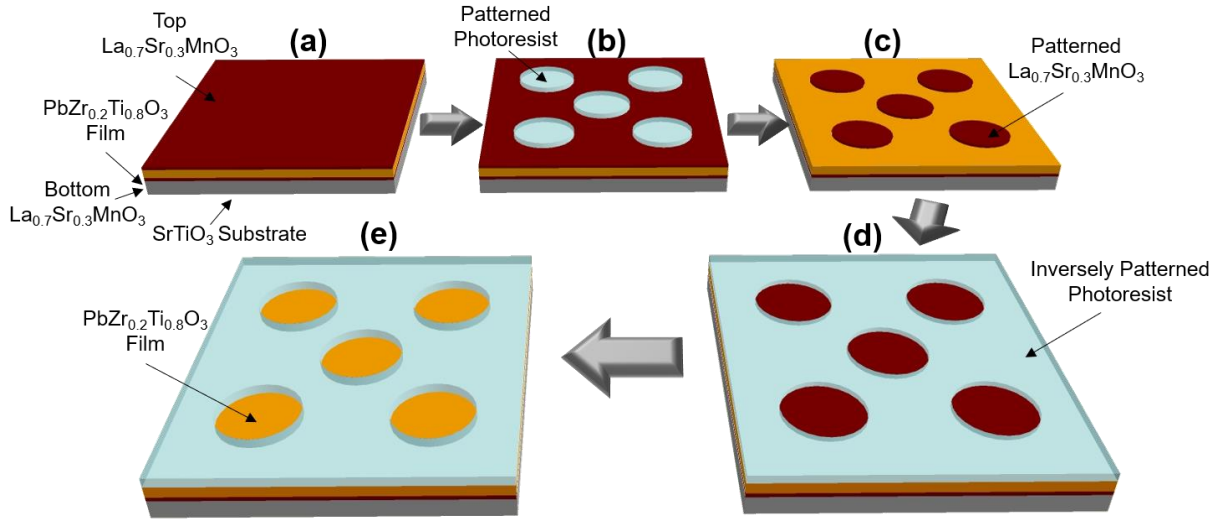
Supplementary Figure 4 | The full data profile of pulse-switching measurements. The switched positive and negative remanent polarization measured as a function of pulse width for different pulse voltages in **a**, (001)- and **b**, (111)-oriented heterostructures.



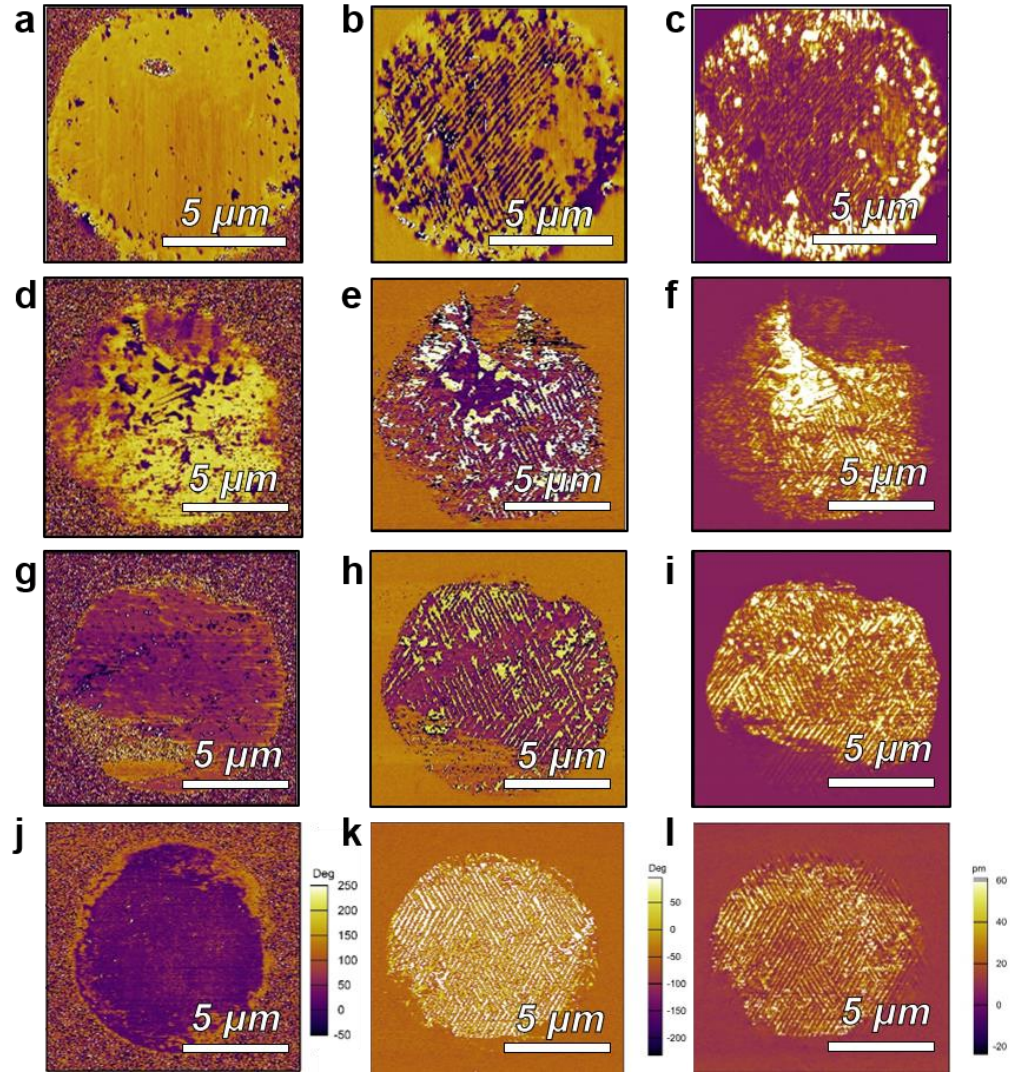
Supplementary Figure 5 | The supercell used in molecular dynamics simulations. The molecular dynamics simulations were performed on a (111)-oriented $28\sqrt{6} \times 50\sqrt{2} \times 16\sqrt{3}$ supercell of PbTiO_3 (672,000 atoms) with periodic boundary conditions (PBCs) and a bond-valence-based interatomic potential parameterized from first-principles. The supercell has the Cartesian axes aligned along crystallographic axes $[11\bar{2}]$, $[1\bar{1}0]$, and $[111]$, respectively.



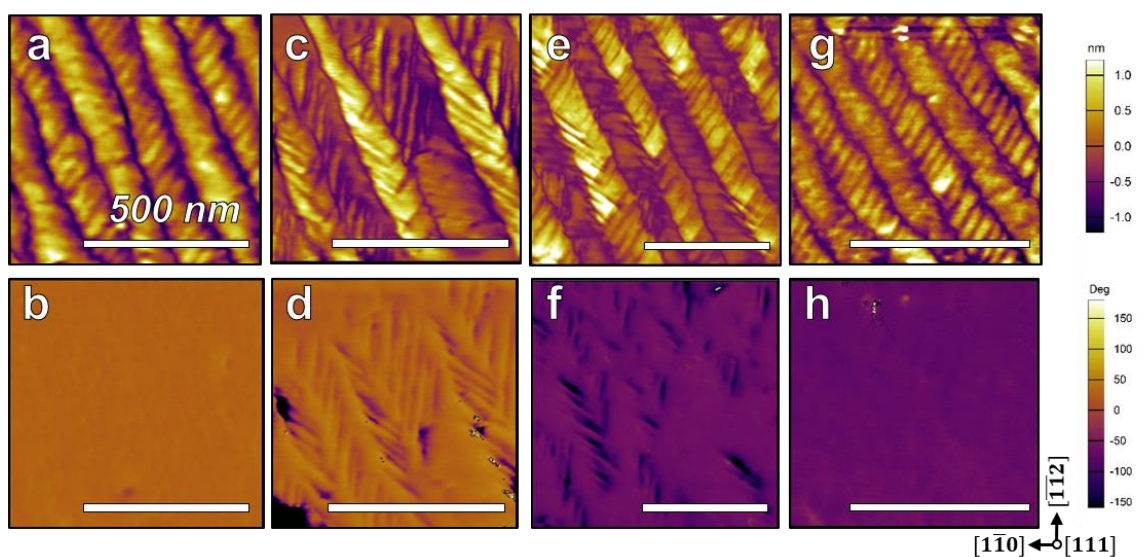
Supplementary Figure 6 | The phase-field energy landscape for polarization switching. **a**, Total, **b**, elastic, and **c**, Landau energies calculated as a function of polarization orientation. Regardless of film orientation, the Landau energy exhibits local minima at polarization orientations along 0°, 90°, 180°, and 270° due to the tetragonal symmetry of the $\text{PbZr}_{0.2}\text{Ti}_{0.8}\text{O}_3$ films. The elastic energy varies significantly and, therefore, the total energy, which is a sum of the Landau and elastic energies, differs for (001)- and (111)-oriented heterostructures. The angle between the two total energy minima is 180° and ~90° for (001)- and (111)-oriented heterostructures, respectively, which suggests 180° switching is favored in (001)-oriented films, while 90° switching is favored in (111)-oriented films.



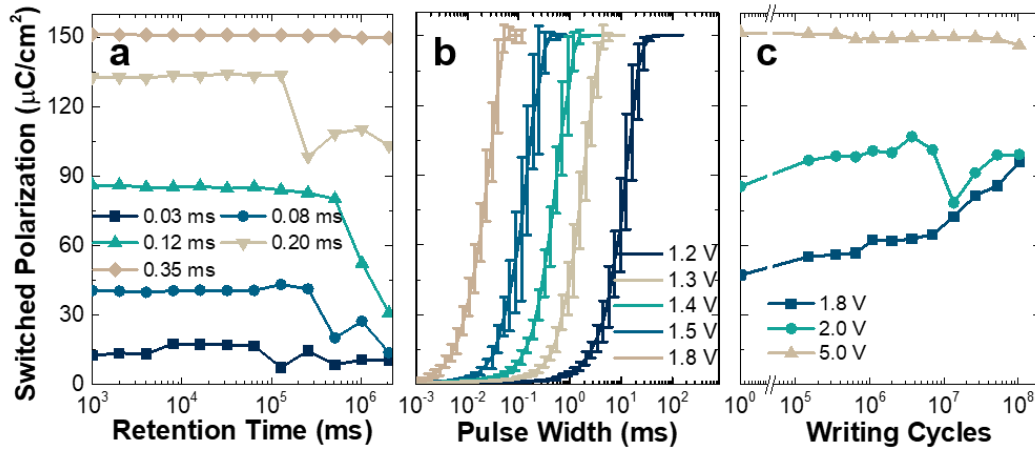
Supplementary Figure 7 | The schematic of the fabrication process to enable domain-structure characterization. **a**, The as-grown heterostructure before patterning. **b**, A layer of photoresist is patterned onto the as-grown heterostructures using photolithography which covers the circular electrode regions only. **c**, Using a dilute H_3PO_4 acid (dilution ratio 1 part acid : 5 parts water) the uncovered $\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$ was etched away within 30 seconds leaving circular $\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$ covered by photoresist. Subsequently, the photoresist was removed by acetone. **d**, Multiple capacitors were pre-poled into different polarization states and then a layer of inversely patterned photoresist was coated by photolithography that only covers the exposed $\text{PbZr}_{0.2}\text{Ti}_{0.8}\text{O}_3$ regions. **e**, The uncovered top $\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$ electrodes were then etched away using dilute H_3PO_4 acid as noted previously. The inversely-patterned photoresist was left on the film serving as a marker that aids the accurate location and imaging of regions that were under the pre-poled capacitors.



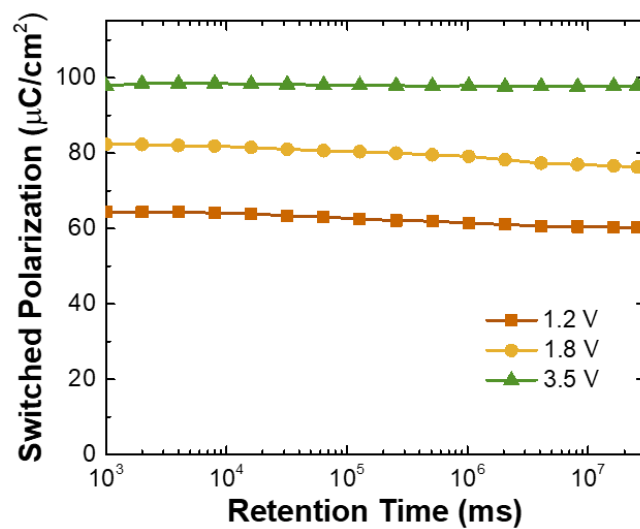
Supplementary Figure 8 | Piezoresponse force microscopy imaging of the domain structures in regions under the pre-poled capacitors. Piezoresponse force microscopy measurements of the domain structures inside the capacitor area for the four pre-poled polarization states discussed in Fig. 3, including those for the **a-c**, fully-up-poled state, **d-f**, the intermediate state poled at 1.1 V, **g-i**, the intermediate state poled at 1.6 V, and **j-l**, the fully-down-poled state. The left column is vertical phase, the center column is lateral phase, and the right column is lateral amplitude images.



Supplementary Figure 9 | Piezoresponse force microscopy characterization of domain structures. Lateral amplitude (**a**, **c**, **e**, **g**) and vertical phase (**b**, **d**, **f**, **h**) piezoresponse force microscopy images for the **a**, **b**, initial fully-up-poled state, **c**, **d**, intermediate state poled at 1.1 V, **e**, **f**, intermediate state poled at 1.6 V, and **g**, **h**, final fully-down-poled state poled at 3.0 V.



Supplementary Figure 10 | Pulse-switching measurements in (001)-oriented heterostructures. **a**, Retention measurements probing the time stability of intermediate-polarization states. **b**, Repeatability measurements in wherein the error bars were generated after repeating each pulse-switching measurement 10 times. **c**, Endurance measurements of the switched polarization as a function of writing cycles.



Supplementary Figure 11 | Retention measurement in (111)-oriented heterostructures.

Retention measurements probing the time stability of various intermediate-polarization states in (111)-oriented heterostructures up to 2×10^7 ms (7.5 hours).