

Reviewers' Comments:

Reviewer #1:

Remarks to the Author:

This paper discusses the mechanical properties of metallic nanoboxes including both yield stresses and strain hardening behaviors. The topic is interesting, and the material system is new. The authors took multiple steps (compression test, FEM, MD) to investigate the mechanisms. However, the study sounds incomplete and many suggested mechanisms were based on authors' assumption and not rationalized in detail by any of the simulation or experimental methods. Therefore, the reviewer believes that this paper needs substantial revision and cannot be recommended for publication. Following are some questions that should be addressed in better details.

- The nanobox with rough surfaces has much lower yield point. The reason behind this is not discussed in detail. The authors could possibly look into dislocation nucleation mechanisms of both rough and smooth surfaces and identify the sources of this difference. A detailed discussion should be devoted to the existences of the steps and ledges in the rough surface and how their distribution and orientation could affect the dislocation nucleation to be easier in the case of rough surfaces.

- In addition, the size of the rough and smooth boxes is different. Smooth nanoboxes are about 10% larger than the rough ones. The yield differences could simply be related to the size effects. The authors are recommended to address this phenomenon.

- Discussions on volume differences in page 6 are unclear and puzzling. The language of this discussion needs to be improved to address the main point of all these volume comparisons.

- Greater rate of hardening could be related to larger surface ratios. As the scale of roughness is similar to structure dimensions. This should also be discussed from both TEM and MD aspects. The authors only speculated two possible scenarios without backing up their hypothesis.

- Page 8 the following statement can be discussed in more details. In what terms are the similarities and differences. "The mechanical response of the hollow nanoboxes is substantially different from that of solid, single crystalline metallic nanostructures, but is similar to nano- and microporous metal foams, and thin-shelled nanostructures such as carbon nanotubes".

- Page 9. It is not clear if the deformation mode of the sidewalls includes any bending and buckling or they are just under compression. The authors first suggested buckling as a possible deformation mode. MD simulations also show signs of bending and buckling. However, the experimental observations decline any evidence of bending and buckling. This discrepancy and the major deformation modes need to be discussed in better details.

- In the methods section why the potential for Ag-Si is needed? There is no Si atoms in the system!

Reviewer #2:

Remarks to the Author:

Authors study hollow nanocubes made of Ag and Au, comparing the mechanical behavior under compression for nanocubes with smooth and rough surfaces. Hollow cube synthesis required several steps, resulting in cube sides about 140 nm with wall thickness around 15 nm. Some of the authors carried out a previous study, their ref. [42], compressing Ag nanocubes which are passivated with surfactants to tune surface properties which would affect dislocation nucleation. This new study also includes high resolution TEM with in situ nanomechanical testing, finite

element methods (FEM), and molecular dynamics (MD) simulations. It is concluded that the strong hardening at large compression, which is observed experimentally, is due to stacking fault-dislocation interactions.

The behavior of nanostructures depends on size, as discussed for instance in [Li 2018, Wang 2018], showing diffusion-dominated plasticity dominating below around 10 nm [Sun 2014], and dislocation slip [Shong 2016, Wang 2018a] and twinning [Wang 2018b] above that size. For nanocrystalline fcc metals a similar set of regimes appears with increasing grain size, with GB activity replacing surface diffusion mediated plasticity [Li 2018b]. There is a massive amount of research on nanowires but research on mechanical properties of metallic hollow structures is scarce, despite the possibility of technological applications. This paper is a welcomed contribution to the field of nanomechanics, but some of the conclusions are not convincing for this reviewer. A summary of results is provided below, along some of the caveats which can weaken the conclusions.

Regarding the experiment, loading curves under the TEM give a yield stress of approximately 130 and 95 GPa and 10% strain, for smooth and rough nanocubes, and deformation which can be as large as 60%-80%. TEM suggest the nucleation of dislocations during compression, but scale bar is 100 nm in Fig. 4, so individual dislocations cannot be resolved, as they are in some other studies for Ag nanostructures [Sun2014]. There is significant hardening starting at around 40% for the smooth cube and 20% for the rough cube. The comparison between smooth and rough is complicated by the fact that the density, chemical composition, and small-scale topology of the cubes are different.

Regarding FEM simulations, an isotropic elastic-plastic solid is assumed, with a bulk yield strength of 600 MPa, which gives nanocube yielding at around 230 MPa and 2% strain, and a stress plateau (with slight softening) after that. The authors indicate that, since FEM does not show hardening, materials rather than geometry determine experimental hardening. However, in order to obtain hardening, one has to include certain ingredients in FEM calculations, and it is not clear if that is the case. Was any type of hardening exponent used for the plastic behavior? In addition to this, FEM has to be applied out with care at the nanoscale: anisotropic crystal plasticity and plasticity nucleation effects [Li 2002] might be required. Typical representative volume elements might be larger than the nanostructure representative size (for instance cube side here). It would be useful to demonstrate that the FEM simulations used do have the ingredients required to produce hardening for some given wall thickness.

Finally, MD simulations of the hollow nanocube are scaled down with respect to the experiment, using a cube side of 50 nm, and 3 different values of thickness: 7, 3, and 2 nm. They assume Ag as the single component of the cube. MD simulations are carried out at different compression rates, to test for strain rate effects, given that experiments are carried out at a much longer time scale. They give, for the sample with 1:7 ratio of wall thickness to cube length, a plastic yielding near 585 MPa and 4% strain, with strong hardening associated with densification when walls start to touch due to compression after 48% strain. Snapshots of the simulations indicate stacking faults, but there is no detailed dislocation analysis. For instance, the paper says "At 53% strain, dislocations are found throughout the entirety of the sidewalls". Fig. 6c shows evidence for stacking faults and some disordered regions, but most partial dislocations would have disappeared leaving behind only stacking faults. Full dislocations are unlikely to appear for such thin wall. Is there any twinning in the MD samples?

Regarding simulation of hollow nanostructures of fcc metals, there are two recent studies: one focusing on elastic properties of Cu nanoshells [Yang 2018], and another including a study of plastic properties for Pd nanoshells [Valencia2018]. Pd has much higher SFE, but still shows mostly SFs and twins at high strain. A possible problem with the MD simulations presented in the paper is the use of an interatomic potential not suited for plasticity under compression up to large strains. Mordehai et al [Mordehai2018] showed that the plastic deformation of a solid nanocube

depends strongly on the potential used. There are many potentials for Ag [OpenKim2019]. The EAM potential used in this work [Foiles 1986] was not fit to describe properties related to dislocation plasticity, unlike more recent potentials like the one by Sheng [Sheng 2011], used in [Sun 2014]. A recent study [Rassoulinejad-Mousavi 2018] shows that elastic constants under pressure are not well described by this Ag potential. Another recent study [Su 2019] shows that the [Sheng 2011] potential is the one which compares better with ab-initio calculations of the generalized stacking fault energy surface, which is one of the main factors in stacking fault nucleation and motion. The potential by Foiles [Foiles 1986] gives a much lower value for the unstable and stable stacking faults. Therefore, the observed strong hardening might be partly due to the (artificially) large number of stacking faults due to this lower barrier.

There are always challenges when comparing experiments with different numerical techniques. In this case, the comparison does not provide quantitative agreement and improved simulations and analysis would be welcomed.

References:

- [Foiles 1986] S.M. Foiles et al., Embedded-atom method functions for the fcc metals Cu, Ag, Au, Ni, Pd, Pt, and their alloys, *Phys.Rev. B* 33, 7983 (1986).
- [Li 2002] J. Li et al., Atomistic mechanisms governing elastic limit and incipient plasticity in crystals, *Nature* 418, 307 (2002).
- [Li 2018] Qing-Jie Li & Evan Ma (2018) When 'smaller is stronger' no longer holds, *Materials Research Letters*, 6:5, 283-292.
- [Li 2018b] Duohui Li, Xinyu Shu, Deli Kong, Hao Zhou, Yanhui Chen. Revealing the atomistic deformation mechanisms of face-centered cubic nanocrystalline metals with atomic-scale mechanical microscopy: A review. *Journal of Materials Science & Technology* 2018, 34 (11) , 2027-2034. DOI: 10.1016/j.jmst.2018.03.006.
- [Mordehai 2018] D. Mordehai et al., Nucleation-Controlled Plasticity of Metallic Nanowires and Nanoparticles, *Adv.Mater.* 2018, 1706710.
- [OpenKim2019] <https://openkim.org/browse/models/by-species?species-search=Ag>
- [Rassoulinejad-Mousavi 2018] S.M. Rassoulinejad-Mousavi & Y. Zhang, Interatomic Potentials Transferability for Molecular Simulations: A Comparative Study for Platinum, Gold and Silver, *Scientific Reports* 8, 2424 (2018).
- [Sheng 2011] H.W. Sheng et al., Highly optimized embedded-atom-method potentials for fourteen fcc metals, *Phys. Rev. B* 83, 134118 (2011). <https://sites.google.com/site/eampotentials/Ag>
- [Shong 2016] L. Shong et al., Slip-activated surface creep with room-temperature super-elongation in metallic nanocrystals, *Nature Mat.* 16, 439 (2016).
- [Su 2019] Y. Su et al., Density functional theory calculations of generalized stacking fault energy surfaces for eight face-centered cubic transition metals, *J. Appl. Phys.* 126, 105112 (2019); <https://doi.org/10.1063/1.5115282>
- [Sun 2014] Sun et al. 2014, Liquid-like pseudoelasticity of sub-10-nm crystalline silver particles, *Nature Materials* 13, pages 1007–1012 (2014).
- [Valencia 2018] F. Valencia et al., Mechanical Properties Obtained by Indentation of Hollow Pd Nanoparticles, *J. Phys. Chem. C* 122, 25035-25042 (2018).
- [Wang 2018] X Wang et al., "Advances in understanding atomic-scale deformation of small-sized face-centered cubic metals with in situ transmission electron microscopy", *Materials Today Nano* 2, 58 (2018).
- [Wang 2018a] L Wang et al., Plastic Deformation through Dislocation Saturation in Ultrasmall Pt Nanocrystals and Its in Situ Atomistic Mechanisms, *Nano Lett.* 20171784733-4739
- [Wang 2018b] L. Wang, J. Teng, Y. Wu, J. Zou, G. Yu, Z. Zhang, X. Han. Size dependence of dislocation activities and independence on theoretical elastic strain limit in Pt nanocrystals revealed by atomic-resolution in situ investigation. *Materials Today Nano* 2018, 2, 1-6. DOI: 10.1016/j.mtnano.2018.04.007.
- [Yang 2018] Q. Yang et al., Mechanical properties of single crystal copper ellipsoidal nanoshells by molecular dynamics, *International Journal of Modern Physics B* Vol. 32, No. 16, 1850196 (2018). <https://doi.org/10.1142/S0217979218501965>.

Reviewer #3:

Remarks to the Author:

This manuscript presents a combined experimental and computational study of plastic deformation and strain hardening during compression of hollow Au-Ag nanoboxes fabricated by galvanic replacement from perfect solid Ag nanocubes. The authors have tested metallic nanostructures of ~100 nm in size made with either smooth or rough surfaces. Using in situ SEM/TEM compression experiments, they observe that these nanoboxes exhibit strain-hardening behaviors exceeding that predicted theoretically for bulk Ag, more so when the surface of nanoboxes is rough as opposed to smooth. FEA and MD simulations were used to study the mechanism responsible for this behavior. It is concluded that the observed hardening effects result from dislocation interaction with stacking-fault (SF) defects, rather than from structural plastic buckling effects. This research is new and interesting, and the article is well-written and well-presented. However, the main claim that the governing mechanism is associated with dislocation-SF interactions should be better substantiated before this manuscript could be accepted for publication in Nature Communications. In particular, the authors should address the following major concerns:

1. The authors did not clearly address the internal microstructure differences between smooth and rough nanoboxes, such as the presence of grain boundaries, which raises an important concern that grain-boundary hardening should not have been omitted in the models.
2. The author should better address how dislocation-SF interactions could significantly contribute to the overall hardening and how they are truly impacted by roughness effects. Particularly, experimental and MD simulation evidence suggests that dislocation interactions with pre-existing SFs are associated with very small transmission energy barriers (e.g. see Wang et al. Nanoscale, 2019, 11, 12672). Therefore, the authors should propose a better model to explain the observation that rough nanoboxes exhibit superior hardening. In its current version, the manuscript remains unsettled on this question.
3. FEA simulation results presented are not meaningful and should be further developed because (1) they focused on only plastic buckling effects at strains < 20%, while structural effects in MD simulations become only evident at strains > 40%, and (2) the elastic-plastic constitutive law used for FEA is unclear. In fact, the authors should test their hypothesis by simulating constitutive laws with different hardening exponents to study how it could affect the strain-strain response of metallic nanoboxes. These results would be more insightful.
4. The authors must clarify the following technical aspects in the text: (1) how stress was computed in each method, especially in MD simulations, (2) how strain-hardening exponents were measured experimentally, and if the last densification stage where stress increases sharply was taken into account or not, and (3) if strain-hardening exponent was quantified in MD simulations, and that such prediction should be compared to the experimental exponents.

Response to Reviewer Comments for

Hardening in Au-Ag Nanoboxes from Stacking Fault-Dislocation Interactions

Radhika P. Patil^a, David Doan^a, Zachary H. Aitken^c, Shuai Chen^c, Mehrdad T. Kiani^b,
Christopher M. Barr^d, Khalid Hattar^d, Yong-Wei Zhang^c, X. Wendy Gu^{*a}

^aDepartment of Mechanical Engineering, and ^bDepartment of Materials Science and Engineering,
Stanford University, Stanford, CA 94305, United States

^cInstitute of High Performance Computing, A*STAR, 1 Fusionopolis Way, #16-16 Connexis,
138632 Singapore

^dMaterials, Physical, and Chemical Sciences, Sandia National Laboratories, Albuquerque, NM,
87185, USA

Reviewer #1 comments:

This paper discusses the mechanical properties of metallic nanoboxes including both yield stresses and strain hardening behaviors. The topic is interesting, and the material system is new. The authors took multiple steps (compression test, FEM, MD) to investigate the mechanisms. However, the study sounds incomplete and many suggested mechanisms were based on authors' assumption and not rationalized in detail by any of the simulation or experimental methods. Therefore, the reviewer believes that this paper needs substantial revision and cannot be recommended for publication. Following are some questions that should be addressed in better details.

44 - The nanobox with rough surfaces has much lower yield point. The reason behind this is not
45 discussed in detail. The authors could possibly look into dislocation nucleation mechanisms of
46 both rough and smooth surfaces and identify the sources of this difference. A detailed discussion
47 should be devoted to the existences of the steps and ledges in the rough surface and how their
48 distribution and orientation could affect the dislocation nucleation to be easier in the case of
49 rough surfaces.

50 Response: We hypothesize that the rough nanoboxes yield at a lower stress because the rough
51 protrusions behave as stress concentrations. We agree that more careful characterization of the
52 surface roughness on the nanoboxes would be desirable for this analysis, but unfortunately it is
53 nearly impossible to do this using TEM, which is the highest resolution imaging technique that is
54 available to us. Due to the high density of protrusions, a TEM image oriented along the [100]
55 face of the nanobox shows the superposition of many different protrusions. This means that it is
56 impossible to estimate the shape of a single protrusion from this TEM image. To address this
57 issue, we were able to synthesize nanocubes with sparse protrusions by lowering the etchant
58 concentration. Figure 1 (below) shows TEM images of nanocube samples with low-density
59 protrusions, which were used to estimate the size of individual protrusions. Figure 1b shows a
60 high resolution TEM image of the corner of a nanocube, which shows lattice fringes within the
61 protrusion that are aligned with the crystal orientation of the cube. This indicates single
62 crystallinity and the lack of grain boundaries at the protrusion.

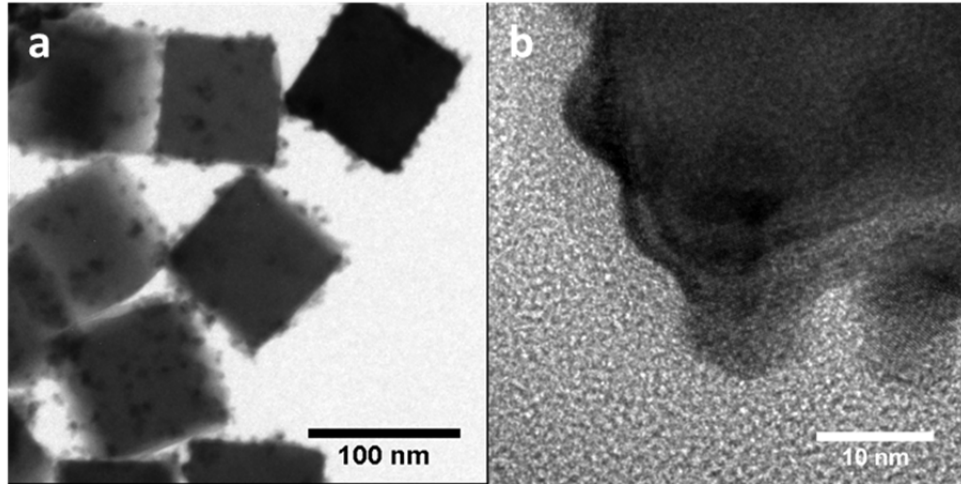


Figure 1. **a** TEM image of solid Ag nanocubes with sparse surface roughness. **b** HRTEM image of individual surface protrusion.

Based on these images, we estimate that protrusions with a radius of curvature (fillet radius) of $\sim 1\text{-}3\text{ nm}$ at the base and diameters of $\sim 10\text{ nm}$. Using the classical stress concentration corresponding to a shoulder fillet in stepped circular shafts (Fig. 2) and the dimensions of the protrusions resulted in stress concentrations of ~ 1.58 .¹ Experimentally, the relative yield strengths of the rough and smooth nanoboxes indicate a stress concentration factor of ~ 1.35 for the rough nanoboxes, which is in the range of our estimate. This discussion has been added to the manuscript on page 14, line 286-290.

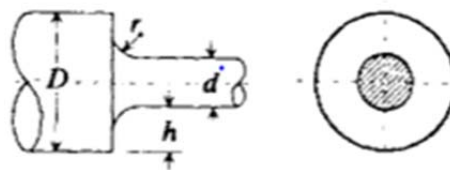


Fig. 2 Illustration of shoulder fillet in stepped circular shafts

We have also performed additional MD simulations of rough nanoboxes (nanoboxes with hemispherical protrusions) (see figure below). The most notable difference between the stress-strain curves of the rough and smooth samples is the significant decrease in yield strength in the rough sample. Both samples yield via partial dislocation emission from the surface. This suggests that the protrusions act to promote nucleation of dislocations, likely as stress concentrators, with a stress concentration factor of ~ 2 . We have included this discussion in the manuscript on page 13, line 275-286 and the following figure in the Supplemental Information.

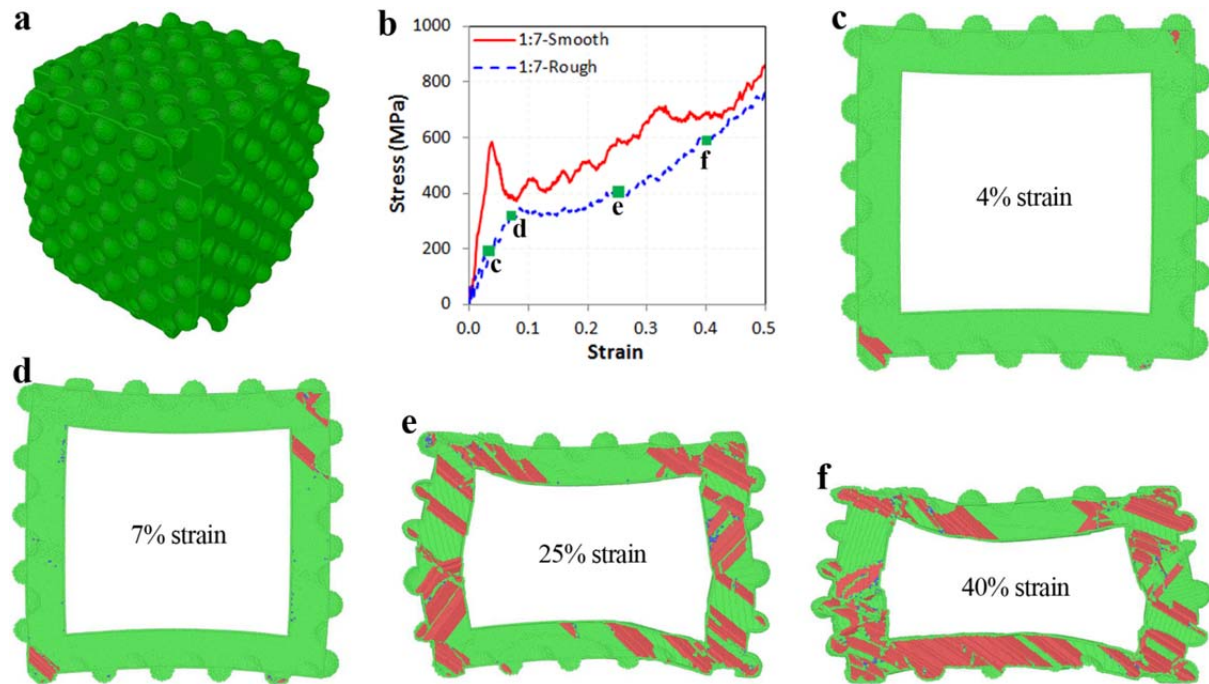


Fig. 3. MD simulations of Ag nanobox with rough protrusions and indents. **a** The rough nanobox sample. **b** Comparison between the generated stress-strain data of smooth and rough nanoboxes. Cross-sectional view of 1:7 rough sample (ratio of wall thickness to length) at **c** 4% strain, **d** 7% strain, **e** 25% strain, and **f** 40% strain. Green atoms have FCC coordination and red atoms are stacking faults.

89

90 - *In addition, the size of the rough and smooth boxes is different. Smooth nanoboxes are about*
91 *10% larger than the rough ones. The yield differences could simply be related to the size effects.*
92 *The authors are recommended to address this phenomenon.*

93 Response: While the overall size of the smooth nanoboxes is larger than the rough nanoboxes,
94 the characteristic length scale of interest is the thickness of the sidewall, as this is the load-
95 bearing structure within the nanobox. The rough nanoboxes have thinner walls than the smooth
96 nanoboxes. Considering the “smaller is stronger” size effect in nanoscale single crystalline
97 metals², the thinner walls should be stronger than the thicker ones, which is not observed. Other
98 researchers have proposed a size-independent strength when metallic nanostructures are in the
99 200 nm regime.³ This would result in rough nanoboxes with the same strength as smooth
100 nanoboxes per nanobox cross-sectional (load-bearing) area. This is also not observed. In
101 addition, the overall size of the rough nanoboxes is smaller than the smooth nanoboxes. The
102 rough nanoboxes would be stronger than the smooth if strength scaled as overall nanobox size
103 according to the trend of “smaller is stronger”, but this is not the case. Therefore, we conclude
104 that differences in yield strength are not due to size effects. The main difference between the
105 rough and smooth samples is surface roughness, so we propose that this difference is responsible
106 for differences in yield strength and hardening.

107 This discussion has been added to the manuscript on page 8, line 149-161.

108

109 - *Discussions on volume differences in page 6 are unclear and puzzling. The language of this*
110 *discussion needs to be improved to address the main point of all these volume comparisons.*

111 Response: We apologize for the confusion and lack of clarity. The main point of the discussion is

that both Au and Ag are present in the final nanoboxes, which indicates that the galvanic exchange reaction does not go to completion. The evidence for this is the differences between the volume of the solid Ag nanocube (starting structure), smooth nanobox and rough nanobox. The section has been modified to better convey this main point (page 6, line 111-122).

- Greater rate of hardening could be related to larger surface ratios. As the scale of roughness is similar to structure dimensions. This should also be discussed from both TEM and MD aspects. The authors only speculated two possible scenarios without backing up their hypothesis.

Response: We have performed additional MD simulations to address this issue (see figure below). The most notable difference between the stress-strain curves of the rough and smooth samples is the significant decrease in yield strength in the rough sample. Both samples yield via partial dislocation emission from the surface. This suggests that the protrusions act to promote nucleation of dislocations, likely as stress concentrators. Beyond yielding, there is a regime (~10-20% strain) where the smooth sample displays significant hardening and the rough sample displays negligible hardening. This difference appears to be related to the difference in location of the dislocation nucleation sites. In the smooth sample, initial yielding involves nucleation of multiple dislocations from the center of the side walls (manuscript Figure 6). These dislocations easily encounter each other and interact. In the rough sample, initial yielding involves dislocations that are spaced far away from each other and have no opportunity to interact. It is only beginning at ~25% strain, when further dislocations are emitted and begin to interact does the rate of stress increase in the rough sample begin to match that of the smooth sample. Further straining indicates similar levels of hardening between the smooth and rough samples. Although the hardening rate of the rough sample approaches and then matches the hardening rate of the

smooth sample, we note that the distribution of protrusions that we use in our MD sample do not contact each other throughout the entire compression simulation. We have included this discussion in the manuscript on page 14, line 283 and have included the following figure in the Supplemental Information.

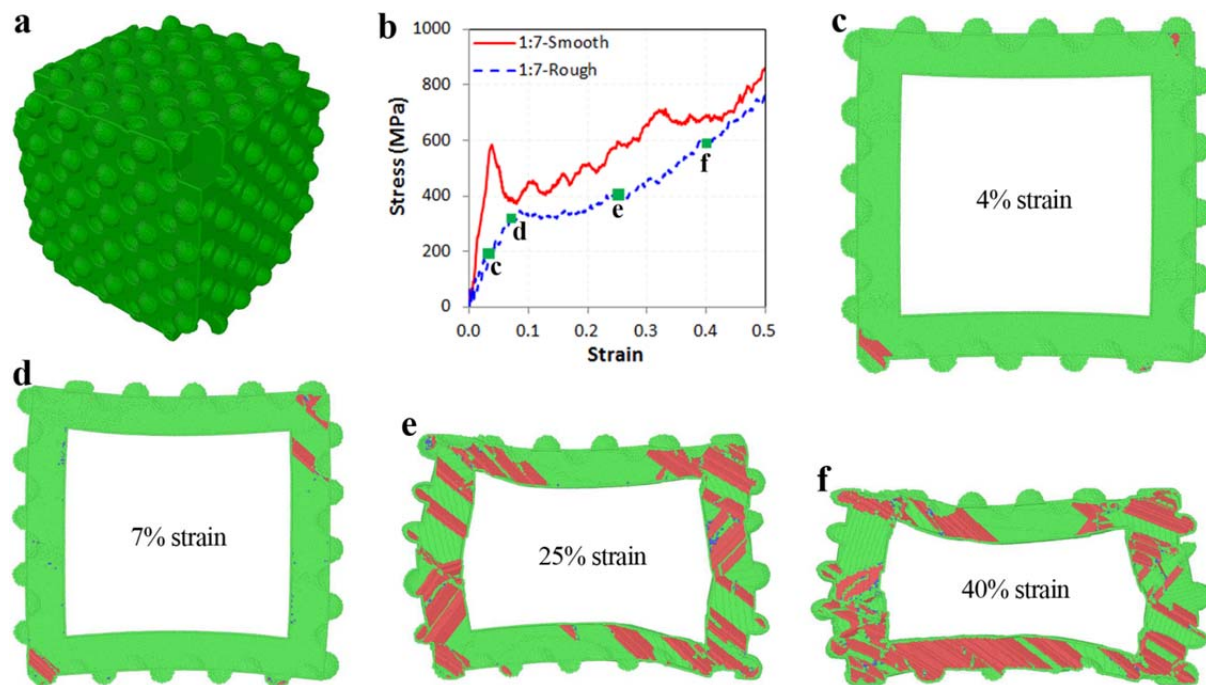


Fig. 4. MD simulations of Ag nanobox with rough protrusions and indents. **a** The rough nanobox sample. **b** Comparison between the generated stress-strain data of smooth and rough nanoboxes. Cross-sectional view of 1:7 rough sample (ratio of wall thickness to length) at **c** 4% strain, **d** 7% strain, **e** 25% strain, and **f** 40% strain. Green atoms have FCC coordination and red atoms are stacking faults.

We agree with the reviewer that the presences of surface protrusions will increase surface area and alter the corresponding surface free energy. We have discussed the morphology of the

surface protrusions using TEM imaging in response to reviewer #1 comments (see Figure 1). From this analysis, we can get an estimate of the ratio of surface protrusion base diameter (l) to height (d). The average $l:d$ ratio of the roughness is 1. Previously, MD simulations have been performed on tensile testing of silicon nanowires with notched rough surface for varying ($l:d$) ratios.⁴ These simulations show that surface roughness-induced stress concentrations dominate the yield stress. The effect of surface energy change due to presence of roughness was also investigated in this work. The generated stress-strain plots of these wires show no post yield hardening despite the roughness altered surface energies. On the contrary, stress drops after yielding in these simulations. Therefore, we hypothesize that surface energy alterations are not a dominant factor for the observed hardening in our nanoboxes. Rather it is the interaction of stacking faults and dislocations due to bending of the side walls and multiple nucleation sites as seen from the above MD simulations which was not possible in a tensile tested sample. This discussion has been added to the manuscript on page 14 line 290-294.

- Page 8 the following statement can be discussed in more details. In what terms are the similarities and differences. “The mechanical response of the hollow nanoboxes is substantially different from that of solid, single crystalline metallic nanostructures, but is similar to nano- and microporous metal foams, and thin-shelled nanostructures such as carbon nanotubes”.

Response: The compressive stress-strain responses of single crystalline metallic nanostructures like nanocubes, nanowires and nanopillars are characterized by large slip events in the plastic regime, and lack of hardening. Metallic foams and thin-shelled nanostructures have stress-strain curves without large slip events, with hardening. This difference is primarily due to deformation modes such as bending and buckling. This behavior (gradual deformation without large slip

events and hardening) is similar to that of the nanoboxes, while the behavior of the solid single crystalline nanostructures (large slip events, no hardening) is different from that of the nanoboxes. This discussion has been added to the manuscript on page 9, line 164-172.

- Page 9. It is not clear if the deformation mode of the sidewalls includes any bending and buckling or they are just under compression. The authors first suggested buckling as a possible deformation mode. MD simulations also show signs of bending and buckling. However, the experimental observations decline any evidence of bending and buckling. This discrepancy and the major deformation modes need to be discussed in better details.

Response: The nanoboxes are deforming in bending and plastic buckling. This is clearly shown in MD simulation. Unfortunately, in-situ SEM compression videos cannot be obtained at high enough resolution to observe bending/buckling as it occurs. But, post-compression SEM images (Figure 4a) show a compressed, smooth nanobox that is wider than that expected from elastic deformation alone. This indicates that bending or buckling must occur during compression to result in this final shape. A discrepancy arises when MD simulations and the post-compression SEM image are compared to the in-situ TEM movie of nanobox compression, which does not show bending, but does show a gradual increase in nanobox width during compression. This indicates that the loading state for the in-situ SEM test is closer to ideal compression as in MD simulations, while the in-situ TEM test may deviate further from ideal conditions. However, we see failure of the sidewall in the *in-situ* TEM movie that is very similar to failure in MD simulation. In the manuscript, we explain this discrepancy as “Differences in the post-compression *in-situ* SEM and TEM mechanical testing images may be due to differences in strain rate, noise levels, or subtle differences in nanobox geometry. In addition, the experimental

stress-strain curves show a range of behaviors for both the smooth and rough nanoboxes, which may result in different deformation modes.” We have clarified these issues in the manuscript by revising the text on page 10, line 188 (section page 9,177-200) and rearranging and adding text to page 12, line 236-241.

- In the methods section why the potential for Ag-Si is needed? There is no Si atoms in the system!

Response: Our MD methodology involves compressing the nanobox between two stiff plates. Due to availability of potentials, we chose to construct these plates out of Si atoms. These plates interact with the Ag atoms via a Lennard-Jones potential, but do not interact with other Si atoms. We have clarified the purpose of the Ag-Si potential in the methods section, page 18, line 382-384.

Reviewer #2 comments:

Authors study hollow nanocubes made of Ag and Au, comparing the mechanical behavior under compression for nanocubes with smooth and rough surfaces. Hollow cube synthesis required several steps, resulting in cube sides about 140 nm with wall thickness around 15 nm. Some of the authors carried out a previous study, their ref. [42], compressing Ag nanocubes which are passivated with surfactants to tune surface properties which would affect dislocation nucleation. This new study also includes high resolution TEM with in situ nanomechanical testing, finite element methods (FEM), and molecular dynamics (MD) simulations. It is concluded that the strong hardening at large compression, which is observed experimentally, is due to stacking

fault-dislocation interactions.

The behavior of nanostructures depends on size, as discussed for instance in [Li 2018, Wang 2018], showing diffusion-dominated plasticity dominating below around 10 nm [Sun 2014], and dislocation slip [Shong 2016, Wang 2018a] and twinning [Wang 2018b] above that size. For nanocrystalline fcc metals a similar set of regimes appears with increasing grain size, with GB activity replacing surface diffusion mediated plasticity [Li 2018b]. There is a massive amount of research on nanowires but research on mechanical properties of metallic hollow structures is scarce, despite the possibility of technological applications. This paper is a welcomed contribution to the field of nanomechanics, but some of the conclusions are not convincing for this reviewer. A summary of results is provided below, along some of the caveats which can weaken the conclusions.

Regarding the experiment, loading curves under the TEM give a yield stress of approximately 130 and 95 GPa and 10% strain, for smooth and rough nanocubes, and deformation which can be as large as 60%-80%. TEM suggest the nucleation of dislocations during compression, but scale bar is 100 nm in Fig. 4, so individual dislocations cannot be resolved, as they are in some other studies for Ag nanostructures [Sun2014]. There is significant hardening starting at around 40% for the smooth cube and 20% for the rough cube. The comparison between smooth and rough is complicated by the fact that the density, chemical composition, and small-scale topology of the cubes are different.

Regarding FEM simulations, an isotropic elastic-plastic solid is assumed, with a bulk yield

241 strength of 600 MPa, which gives nanocube yielding at around 230 MPa and 2% strain, and a
242 stress plateau (with slight softening) after that. The authors indicate that, since FEM does not
243 show hardening, materials rather than geometry determine experimental hardening. However, in
244 order to obtain hardening, one has to include certain ingredients in FEM calculations, and it is
245 not clear if that is the case. Was any type of hardening exponent used for the plastic behavior? In
246 addition to this, FEM has to be applied out with care at the nanoscale: anisotropic crystal
247 plasticity and plasticity nucleation effects [Li 2002] might be required. Typical representative
248 volume elements might be larger than the nanostructure representative size (for instance cube
249 side here). It would be useful to demonstrate that the FEM simulations used do have the
250 ingredients required to produce hardening for some
251 given wall thickness.

252 Response: A perfectly elastic-plastic material model without strain hardening was used in the
253 FEM simulation. The reviewer is correct that more complicated material models are typically
254 required to represent nanostructures using FEM. The goal of the FEM simulations was actually
255 not to reproduce the experimental results (this is left to the MD simulations, which are more
256 appropriate for the size scale and complexity of the nanoboxes). Rather, the point of the FEM
257 simulations is to answer the question, “What is the structural response for a material model that
258 does not include strain hardening?” The reason that this is relevant to our system, is that the solid
259 Ag nanocube (the parent structure from which the nanobox is formed) does not show strain
260 hardening. It has been shown in previous work from our group that Ag nanocubes have a stress-
261 strain curve typical of single crystalline nanostructures, where there is no hardening after yield.⁵
262 Starting from this point, we postulate that because the hollow nanoboxes are simply the solid
263 nanocubes with the interior and corners removed, the same material model should be used for the

nanoboxes and solid nanocubes. For instance, the crystal anisotropy and surface dislocation nucleation effects should remain the same for the hollow nanoboxes and solid nanocubes. Using this approach results in a discrepancy between the FEM and experimental results on the hollow nanoboxes. This indicates that a different material model, which includes mechanisms that lead to hardening, is required to simulate the nanoboxes accurately. MD simulations are used to capture this behavior. Thus, the fact that the FEM and experiments of the nanoboxes show different results indicate that it is not the shape of the nanobox that gives rise to hardening. Hardening at the structural level cannot be achieved without a corresponding material model that includes hardening, which is in agreement with the reviewer's comments.

However, in line with the reviewer's comments, we have run additional FEM simulations in order to account for the anisotropy of a single crystalline Ag nanobox. For an FCC metal, only 3 constants (C_{11} , C_{12} , and C_{44}) are necessary to fully populate the elastic stiffness matrix.⁶ The local material coordinate system and global coordination are aligned so we are compressing in a principal direction, which is in line with our experiments. The same loading conditions and boundary conditions are used as previously. The resulting force-displacement curves closely mimic that of an isotropic model, yielding around 230MPa at ~2% and a stress plateau (with slight softening after that). This discussion has been added to the manuscript on page 17 line 359-364 and Supplementary Information.

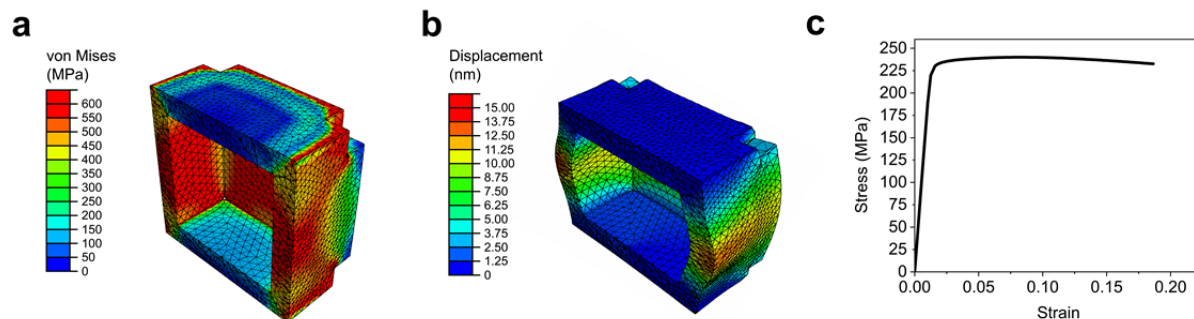


Fig. 5. FEM simulation of a smooth nanobox using an anisotropic model. Cross-sectional view of **a** von Mises stress at $\sim 1.5\%$ strain, **b** radial displacement at $\sim 18\%$ strain, and **c** corresponding engineering stress-strain curve.

Finally, MD simulations of the hollow nanocube are scaled down with respect to the experiment, using a cube side of 50 nm, and 3 different values of thickness: 7, 3, and 2 nm. They assume Ag as the single component of the cube. MD simulations are carried out at different compression rates, to test for strain rate effects, given that experiments are carried out at a much longer time scale. They give, for the sample with 1:7 ratio of wall thickness to cube length, a plastic yielding near 585 MPa and 4% strain, with strong hardening associated with densification when walls start to touch due to compression after 48% strain. Snapshots of the simulations indicate stacking faults, but there is no detailed dislocation analysis. For instance, the paper says “At 53% strain, dislocations are found throughout the entirety of the sidewalls”. Fig. 6c shows evidence for stacking faults and some disordered regions, but most partial dislocations would have disappeared leaving behind only stacking faults. Full dislocations are unlikely to appear for such thin wall. Is there any twinning in the MD samples?

Response: We apologize for the confusion and have updated the statement in the manuscript to:

“At 53% strain, defects left behind from dislocation slip and interactions including stacking faults and disordered regions are found throughout the entirety of the sidewalls”. The figure below shows a summary of the dislocations and stacking faults that appeared in our simulations. We do not observe full dislocations in any simulated sample. Twinning appears rarely in our simulations. Any twins are typically 3-4 atomic layers thick as shown in subplot (c) of figure below. We have expanded our discussion of deformation mechanisms as obtained from MD simulations in the manuscript on page 12, line 248-252.

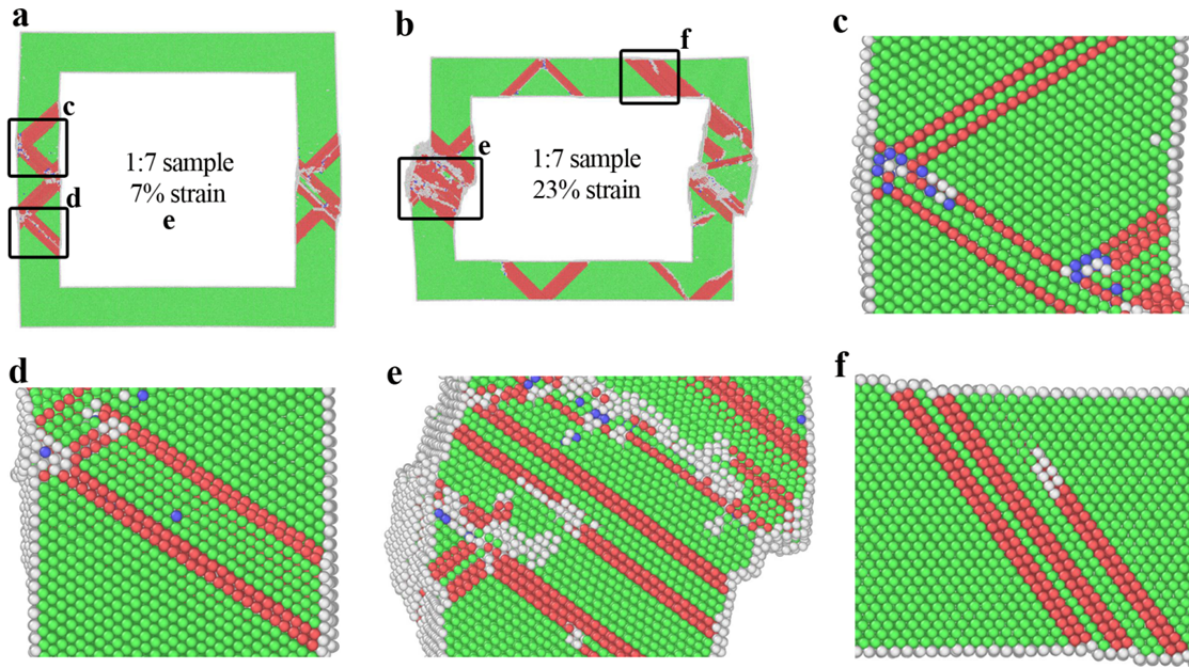


Fig. 6. Cross-sectional view of 1:7 smooth nanobox sample (ratio of wall thickness to length). Nanobox deformed to **a** 7% and **b** 23% strain showing nucleated stacking faults. Green atoms have FCC coordination and red atoms are stacking faults. **c,d,e,f** Enlarged regions marked by corresponding letter in **a,b**.

Regarding simulation of hollow nanostructures of fcc metals, there are two recent studies: one

focusing on elastic properties of Cu nanoshells [Yang 2018], and another including a study of plastic properties for Pd nanoshells [Valencia2018]. Pd has much higher SFE, but still shows mostly SFs and twins at high strain. A possible problem with the MD simulations presented in the paper is the use of an interatomic potential not suited for plasticity under compression up to large strains. Mordehai et al [Mordehai2018] showed that the plastic deformation of a solid nanocube depends strongly on the potential used. There are many potentials for Ag [OpenKim2019]. The EAM potential used in this work [Foiles 1986] was not fit to describe properties related to dislocation plasticity, unlike more recent potentials like the one by Sheng [Sheng 2011], used in [Sun 2014]. A recent study [Rassoulinejad-Mousavi 2018] shows that elastic constants under pressure are not well described by this Ag potential. Another recent study [Su 2019] shows that the [Sheng 2011] potential is the one which compares better with ab-initio calculations of the generalized stacking fault energy surface, which is one of the main factors in stacking fault nucleation and motion. The potential by Foiles [Foiles 1986] gives a much lower value for the unstable and stable stacking faults. Therefore, the observed strong hardening might be partly due to the (artificially) large number of stacking faults due to this lower barrier.

Response: We calculate the relaxed stable and unstable stacking fault energy of the Foiles potential⁷ used here as 6.24 mJ/m² and 116 mJ/m² respectively. The same quantities for the Sheng potential are 26 mJ/m² and 114 mJ/m².⁸ Thus, the energy barrier for creating the initial stacking fault is similar between both potentials.

A study from Van Swygenhoven, et al. that investigated potentials and their likelihood of nucleating full dislocations or partials with stacking faults showed that the ratio of the stable to unstable stacking fault energy was a good metric to predict this likelihood⁹. Among their

potentials, only potentials with such a ratio >0.9 displayed full dislocations while all other potentials (with maximum ratio of 0.7) displayed partials with extensive stacking faults. The ratio of the Foiles potential and Sheng potential is 0.054 and 0.228 respectively, suggesting both should display partials with stacking faults.

We repeated the MD simulations using the Sheng potential suggested by the reviewer. The figure below shows a summary of generated stress-strain data and atomic snap-shots of deformation of the nanobox using the Foiles potential and the Sheng potential. Quantitatively, the stress-strain data is similar. There is an initially elastic regime which culminates in a peak at ~ 600 MPa. There is then an intermediate regime with significant hardening before a final regime of densification. The atomic deformation mechanisms are similar between the Foiles and Sheng potentials, with initial deformation occurring by emission of partial dislocations from the free surface, generating stacking faults through the thickness of the nanobox walls. Increasing deformation leads to an increase in defect content with significant interaction between extended stacking faults and subsequently emitted partial dislocations. This suggests that the Foiles potential is able to capture the relevant deformation behaviour in these compression simulations of Ag nanoboxes.

We thank the reviewer for bringing these other previous studies to our attention and have cited them in the manuscript. We have also included the comparison between potentials and the above discussion in the manuscript on page 19, line 392-400.

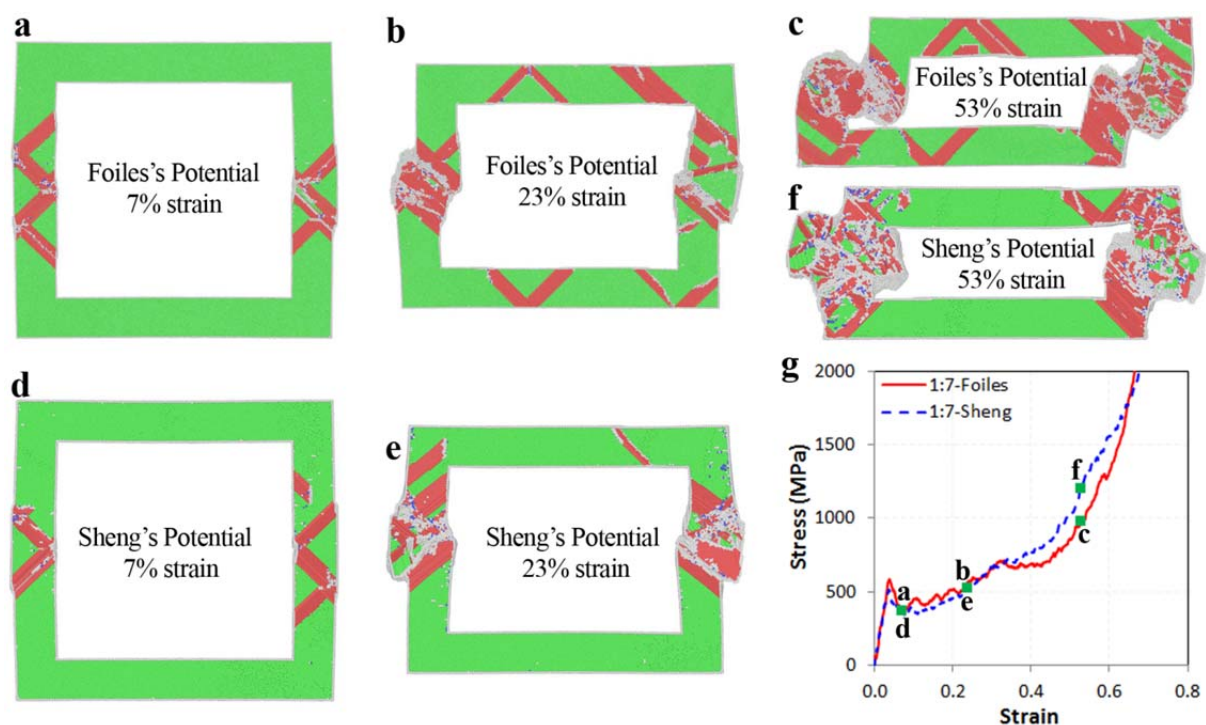


Fig. 7. MD simulations with the Foiles and Sheng potentials. Nanoboxes compressed to **a** 7%, **b** 23%, **c** 53% strain using the Foiles potential. Nanoboxes compressed to **d** 7%, **e** 23%, **f** 53% strain using the Sheng potential. **g** The stress-strain curves for the two potentials.

Reviewer #3 comments:

This manuscript presents a combined experimental and computational study of plastic deformation and strain hardening during compression of hollow Au-Ag nanoboxes fabricated by galvanic replacement from perfect solid Ag nanocubes. The authors have tested metallic nanostructures of ~100 nm in size made with either smooth or rough surfaces. Using in situ SEM/TEM compression experiments, they observe that these nanoboxes exhibit strain-hardening behaviors exceeding that predicted theoretically for bulk Ag, more so when the surface of

nanoboxes is rough as opposed to smooth. FEA and MD simulations were used to study the mechanism responsible for this behavior. It is concluded that the observed hardening effects result from dislocation interaction with stacking-fault (SF) defects, rather than from structural plastic buckling effects. This research is new and interesting, and the article is well-written and well-presented. However, the main claim that the governing mechanism is associated with dislocation-SF interactions should be better substantiated before this manuscript could be accepted for publication in Nature Communications. In particular, the authors should address the following major concerns:

1. The authors did not clearly address the internal microstructure differences between smooth and rough nanoboxes, such as the presence of grain boundaries, which raises an important concern that grain-boundary hardening should not have been omitted in the models.

Response: The synthesis of nanoboxes, nanoshells (hollow nanocubes without holes at cube corners) and nanocages using galvanic replacement is well established and covered in multiple review articles (for example, Skrabalak et al., *Acc. Chem. Res.* 2008).¹⁰ In these studies, careful microstructural analysis has been performed. For instance, high resolution TEM imaging and TEM diffraction have shown that the resulting hollow structures are single crystalline.^{11,12} Our nanoboxes are fabricated using identical synthetic protocols as in these previous studies, so they are also expected to be single crystalline. We have added this point to the manuscript on page 6, line 107-110, page 12, line 252-253. Additionally, as noted in response to reviewer #1 comments (see above), from Fig. 1 (b), we see that the surface protrusions are also single crystalline and with crystallographic orientation aligned with the base cube structure.

2. The author should better address how dislocation-SF interactions could significantly contribute to the overall hardening and how they are truly impacted by roughness effects. Particularly, experimental and MD simulation evidence suggests that dislocation interactions with pre-existing SFs are associated with very small transmission energy barriers (e.g. see Wang et al. *Nanoscale*, 2019, 11, 12672). Therefore, the authors should propose a better model to explain the observation that rough nanoboxes exhibit superior hardening. In its current version, the manuscript remains unsettled on this question.

Response: We have addressed the hardening in the rough nanoboxes in greater detail in response to reviewer #1 comments (see above). In summary, from analysis of TEM images and MD simulations of rough nanoboxes, we conclude that the rough protrusions act as stress concentrations that lead to lower yield strength but higher hardening in the rough nanoboxes. The reviewer refers to a paper entitled “Size-dependent dislocation-twin interactions” and concerns a TEM and MD investigation into transmission of dislocations across a twin boundary. As part of their analysis, the authors calculate the transmission energy across a twin boundary as a function of the twin size. For typical {111} transmission, the authors show that the transmission energy is independent of twin size at ~ 4 meV/atom for Au. We suppose that the reviewer refers to the similarity between the twin and stacking fault in the small-size limit. The energy barriers for slip transmission across a grain boundary in Cu are between 254.4-511.2 mJ/m².¹³ By comparison, the energy barriers for transmission of dislocations across a twin boundary in Cu are reported to be between 199-232 mJ/m², which is similar to the lower bound of grain boundary transmission¹³. Both of these interfaces are known to act as barriers to

dislocation motion and contribute to strengthening¹⁴. Although we are unable to find similar reported quantities for FCC Ag, this suggests that in FCC Cu, a wide range of transmission energies and interfaces can contribute to strengthening. We have included the preceding analysis in the manuscript on page 12, line 242-248.

We note that in our simulations, gliding partial dislocations that encounter an existing stacking fault tend to stop. Within the timescale of the simulation, transmission seldom occurs. An increasing number of stacking faults therefore both limits the amount of plasticity generated by individual dislocations and blocked dislocations create back-stresses requiring increasing applied stress to nucleate subsequent dislocations. These mechanisms are shown in the manuscript in Figure 6 and correlate with the stress-strain curves.

3. FEA simulation results presented are not meaningful and should be further developed because (1) they focused on only plastic buckling effects at strains < 20%, while structural effects in MD simulations become only evident at strains > 40%, and (2) the elastic-plastic constitutive law used for FEA is unclear. In fact, the authors should test their hypothesis by simulating constitutive laws with different hardening exponents to study how it could affect the strain-strain response of metallic nanoboxes. These results would be more insightful.

Response: The value of the FEA simulations is discussed in the response to reviewer #1. To summarize, the point of the FEA is to use the material model (perfectly elastic-plastic) that is appropriate for a solid Ag nanocube (the parent structure for the nanobox) and test whether this can result in hardening if it is applied to the nanobox geometry. The rationale behind this is to test whether the nanobox behaves like the solid Ag nanocube with the interior and corners removed, or whether new deformation mechanisms must be introduced. (1) In regard to

structural effects in FEA vs. MD simulation: The FEA simulation and MD simulation both show bulging at the center of the side walls at ~20% strain (Figure 5b,6b). The value of the FEA simulation is to show that this deformation mode occurs even in the absence of a material model that includes hardening. (2) The constitutive law for FEA is the perfectly elastic-plastic material model. This was chosen to mimic the behavior of solid Ag nanocubes in compression, which showed no hardening after yielding.⁵

4. The authors must clarify the following technical aspects in the text: (1) how stress was computed in each method, especially in MD simulations, (2) how strain-hardening exponents were measured experimentally, and if the last densification stage where stress increases sharply was taken into account or not, and (3) if strain-hardening exponent was quantified in MD simulations, and that such prediction should be compared to the experimental exponents.

Response:

(1a) How stress was computed in MD simulations:

For the case of compression along the z-axis, the standard definition of engineering stress is related to the atomic quantities that are computed during MD simulation according to:

$$\sigma_{zz} = \frac{F_z}{A_0} = \frac{\sum v s_{zz} / L_z}{L_{x0} L_{y0}}$$

where L_{x0} and L_{y0} are the initial cross-sectional dimensions of the nanobox, L_z is the height of the nanobox, and v and s_{zz} are the atomic volume and atomic stresses, respectively. The product, vs_{zz} , can be computed for each nanobox atom following standard definitions¹⁵ and then summed

over all nanobox atoms. L_z is taken as the separation distance between the two rigid plates and L_{x0} and L_{y0} are computed at the beginning of the simulation using the extrema atomic positions. This discussion is added on page 19, line 403-411 of the manuscript.

(1b) How stress was computed in experiments:

The stress was computed by dividing the measured force by the nominal (footprint) area of the structures. For example, if the length of the nanobox was 140nm, the force was divided by $140 \times 140 \text{ nm}^2$ to get the nominal engineering stress.

(2) How hardening exponents were measured experimentally:

The strain hardening exponents were derived by fitting an exponential relation of $\sigma = K\epsilon^n$ to post yield experimental data for each individual test curve (this is discussed on page 8, line 143-148 and page 17, line 344-349 of the manuscript). The values of n from all tests were then averaged for the reported value of strain hardening exponent for the smooth and the rough nanobox. The densification stage was not taken in the curve fitting as this sharp rise in stress is due to touching sidewalls and not the material strain hardening effect. The fitting was limited up to 50% strain to avoid the densification stage.

(3) If the strain hardening exponent was quantified in MD simulations:

Strain-hardening exponents were not computed for the generated MD stress-strain data primarily due to the difficulty in numerical comparison between the experimental and computational stress-strain data. For example, the high strain-rate of the simulated samples results in a much larger yield stress (and consequently overall stress level) as compared to experiments. This is an issue that occurs whenever MD simulations are compared to experiments. As a result, the MD

simulations are most valuable as a way to reveal deformation mechanisms and overall trends, rather than to perfectly reproduce experimental data.

We have included the above expanded discussion of computation and experimental methods in the Manuscript Methods section.

References

1. Pilkey, W. D. *Formulas for stress, strain, and structural matrices*. (John Wiley & Sons, 2005).
2. Greer, J. R. & De Hosson, J. T. M. Plasticity in small-sized metallic systems: Intrinsic versus extrinsic size effect. *Prog. Mater. Sci.* **56**, 654–724 (2011).
3. Han, W.-Z. *et al.* From “Smaller is Stronger” to “Size-Independent Strength Plateau”: Towards Measuring the Ideal Strength of Iron. *Adv. Mater.* **27**, 3385–3390 (2015).
4. Liu, Q., Wang, L. & Shen, S. Effect of surface roughness on elastic limit of silicon nanowires. *Comput. Mater. Sci.* **101**, 267–274 (2015).
5. Kiani, M. T., Patil, R. P. & Gu, X. W. Dislocation surface nucleation in surfactant-passivated metallic nanocubes. *MRS Commun.* 1–5 (2019).
6. Bower, A. F. & CRC Press. *Applied mechanics of solids*.
7. Foiles, S. M., Baskes, M. I. & Daw, M. S. Embedded-atom-method functions for the fcc metals Cu, Ag, Au, Ni, Pd, Pt, and their alloys. *Phys. Rev. B* **33**, 7983–7991 (1986).
8. Sheng, H. W., Kramer, M. J., Cadien, A., Fujita, T. & Chen, M. W. Highly optimized

501 embedded-atom-method potentials for fourteen fcc metals. *Phys. Rev. B* **83**, 134118
502 (2011).

- 503 9. Van Swygenhoven, H., Derlet, P. M. & Frøseth, A. G. Stacking fault energies and slip in
504 nanocrystalline metals. *Nat. Mater.* **3**, 399–403 (2004).

- 505 10. Skrabalak, S. E. *et al.* Gold Nanocages: Synthesis, Properties, and Applications. *Acc.*
506 *Chem. Res.* **41**, 1587–1595 (2008).

- 507 11. Hong, X., Wang, D., Cai, S., Rong, H. & Li, Y. Single-Crystalline Octahedral Au–Ag
508 Nanoframes. *J. Am. Chem. Soc.* **134**, 18165–18168 (2012).

- 509 12. Yugang Sun, Brian T. Mayers, A. & Xia, Y. Template-Engaged Replacement Reaction: A
510 One-Step Approach to the Large-Scale Synthesis of Metal Nanostructures with Hollow
511 Interiors. (2002). doi:10.1021/NL025531V

- 512 13. Sangid, M. D., Ezaz, T. & Sehitoglu, H. Energetics of residual dislocations associated
513 with slip–twin and slip–GBs interactions. *Mater. Sci. Eng. A* **542**, 21–30 (2012).

- 514 14. Lu, K., Lu, L. & Suresh, S. Strengthening Materials by Engineering Coherent Internal
515 Boundaries at the Nanoscale. *Science (80-.)*. **324**, 349–352 (2009).

- 516 15. Thompson, A. P., Plimpton, S. J. & Mattson, W. General formulation of pressure and
517 stress tensor for arbitrary many-body interaction potentials under periodic boundary
518 conditions. *J. Chem. Phys.* **131**, 154107 (2009).

Reviewers' Comments:

Reviewer #1:

None

Reviewer #3:

Remarks to the Author:

The authors have successfully addressed my first concern about grain-boundary effects, since it appears from the literature that the synthesized nanoboxes are single-crystalline.

The authors, however, have not provided convincing evidence that the origin of hardening directly resulted from dislocation-stacking-fault (SF) intersections, which is the primary hypothesis of this study. Given that the energy barrier from transmission of dislocations through SFs was found to be low in Au, all theoretical evidence suggests that the energy barrier for transmission in Ag should be very limited as well, because the SF energy of Ag is much lower than that of Au and Cu. In fact, further quantitative results from FEM analysis using a strain hardening constitutive law and MD simulations should be presented to convince me that the nanobox strain hardening does relate to dislocation-induced hardening from the sidewalls. In their current version, Figures 5, 6 and S1 are insufficient to substantiate this important claim.

Furthermore, the virial theorem used to compute the stress from their MD simulation is odd, as it is not clear if the authors have used the deformed or initial atomic volume in their equation. Using the initial atomic volume could yield inaccurate stress results when the simulation box is not periodic, large plastic deformation is applied and the model contains thin-walls. The authors should further clarify and verify their MD methodology.

While the manuscript quality is improving, I do not recommend its publication in Nature Communications yet without further evidence of the hardening mechanism at play.

Reviewer #4:

Remarks to the Author:

After carefully reviewing the answers to the reviewer's comments, I believe that the authors sufficiently address the main concerns and have expanded the technical robustness of the paper. However, I have two points for further clarification:

1. The FEM discussion did not appear to provide as much insight as the experimental tests or MD simulations. I think that using some language from the answers to the reviewers could clarify the FEM. For example, the authors state during their reply to reviewers 2 and 3 that : "The goal of the FEM simulations was actually not to reproduce the experimental results (this is left to the MD simulations, which are more appropriate for the size scale and complexity of the nanoboxes). Rather, the point of the FEM simulations is to answer the question, "What is the structural response for a material model that does not include strain hardening?" The reason that this is relevant to our system, is that the solid Ag nanocube (the parent structure from which the nanobox is formed) does not show strain hardening." Perhaps some version of this explanation could be incorporated into the text since it is not directly clear in the manuscript why the FEM presented is for a solid rather than a hollow system.

2. The Au:Ag ratios discussion is a bit confusing (pages 6&7). Are the authors implying that the Au:Ag ratios are 70/30 and 30/70? Those are two different alloys and perhaps the observed differences are highly impacted by the alloy composition. I think this section can be clearer and simply stating that the mechanical properties of Au and Ag are similar is not a sufficient explanation.

Response to Reviewer Comments (Second Round of Review)

Hardening in Au-Ag Nanoboxes from Stacking Fault-Dislocation Interactions

Radhika P. Patil^a, David Doan^a, Zachary H. Aitken^c, Shuai Chen^c, Mehrdad T. Kiani^b,
Christopher M. Barr^d, Khalid Hattar^d, Yong-Wei Zhang^c, X. Wendy Gu^{*a}

^aDepartment of Mechanical Engineering, and ^bDepartment of Materials Science and Engineering,
Stanford University, Stanford, CA 94305, United States

^cInstitute of High Performance Computing, A*STAR, 1 Fusionopolis Way, #16-16 Connexis,
138632 Singapore

^dMaterials, Physical, and Chemical Sciences, Sandia National Laboratories, Albuquerque, NM,
87185, USA

Reviewer #3 comments:

The authors have successfully addressed my first concern about grain-boundary effects, since it appears from the literature that the synthesized nanoboxes are single-crystalline.

The authors, however, have not provided convincing evidence that the origin of hardening directly resulted from dislocation-stacking-fault (SF) intersections, which is the primary hypothesis of this study. Given that the energy barrier from transmission of dislocations through SFs was found to be low in Au, all theoretical evidence suggests that the energy barrier for transmission in Ag should be very limited as well, because the SF energy of Ag is much lower

than that of Au and Cu. In fact, further quantitative results from FEM analysis using a strain hardening constitutive law and MD simulations should be presented to convince me that the nanobox strain hardening does relate to dislocation-induced hardening from the sidewalls. In their current version, Figures 5, 6 and S1 are insufficient to substantiate this important claim.

Response: As explained in our previous reply to comments from reviewer#2 during the first round of review (line 252), the goal of the FEM simulations was to analyze the structural response (nanobox shape) without the influence of the material response. Adding a strain hardening model in FEM would mean that we are attempting to reproduce the material response using the strain hardening model, and would defeat the purpose of performing FEM.

In order to compare the transmission energy in the Ag potentials used here, we attempted to reproduce the findings of the manuscript cited by the reviewer ¹ as reporting a low barrier for dislocation transmission. We were unfortunately unable to reproduce the methodology because the method is not provided in the cited paper. We do note several differences between the structure used in that work and the microstructure observed here. In that paper, a leading partial dislocation interacts with a single twinned zone (for a large twin region, this is in effect a single planar fault). In our simulations, we observe bundles of stacking faults and small (2-3 atomic layers) twinned regions. The result is that in our simulations, leading partial dislocations that are able to “break through” a stacking fault or twin boundary quickly encounters another boundary. The accumulated effect of these obstacles (even for low barriers) serves to create a hindrance to slip that increases with a growing amount of dislocation content.

Additionally, although the energy barrier for transmission of dislocation is low in Au, there is significant experimental evidence that stacking faults can accumulate in Au nanostructures. For

instance, stacking faults are found to pile up in deforming nanoporous Au nanowires which also show hardening.² There are also reports of planar defects acting as barriers to dislocation motion in Au. Bulge tests on single crystalline Au 105 nm thick films displayed strain hardening that was attributed to the presence of pinned deformation twins³. In-situ TEM experiments show stacking fault tetrahedra in Au acting as barriers to gliding dislocations, requiring significant bowing of the dislocation before shearing through the stacking fault tetrahedral⁴.

There is also ample evidence from MD simulations on Au and other fcc metals that stacking fault energies comparable to the ones used in our study are able to block dislocations. Previous MD simulations subjected nanotwinned Au nanowires to tension and reported significant strain hardening⁵. In these simulations, the authors employed an Au potential with stacking fault energy of 43.4 mJ/m² and observed that the coherent twin boundaries served as strong barriers to the glide of leading partial dislocations⁵. This phenomenon has also been observed in MD simulations performed using a Cu potential with similar stacking fault and twin boundary energy (44.42 mJ/m² and 22.27 mJ/m² respectively)⁶. These simulations showed a strong blocking effect of twin boundaries to dislocations in nanotwinned Cu samples. We performed compression simulations using two different Ag potentials with stacking fault energies of 6.24 mJ/m²⁷ and 26 mJ/m²⁸. In both sets of simulations, we observed stacking faults and twin boundaries acting as impediments to gliding dislocations. Previous MD simulations considered the interaction of a gliding partial dislocation with stacking fault tetrahedra in Cu using potentials with similar stacking fault energies^{9,10}. In these studies, the authors employed Cu potentials with stacking fault energies of 11.4 mJ/m²⁹ and 44.4 mJ/m²¹⁰ respectively. In both sets of simulations, the stacking fault tetrahedra acted as strong barriers to dislocation motion, leading to significant bowing of the leading partial dislocation.

We lastly note the difficulty in making any claims of transmissibility based solely on the planar defect formation energy (i.e. the stacking fault energy in this case). For example, dislocation emission and transmission through grain boundaries (GB) have been widely studied using MD and there is a reported inverse relation between the transmission energy and GB energy ¹¹.

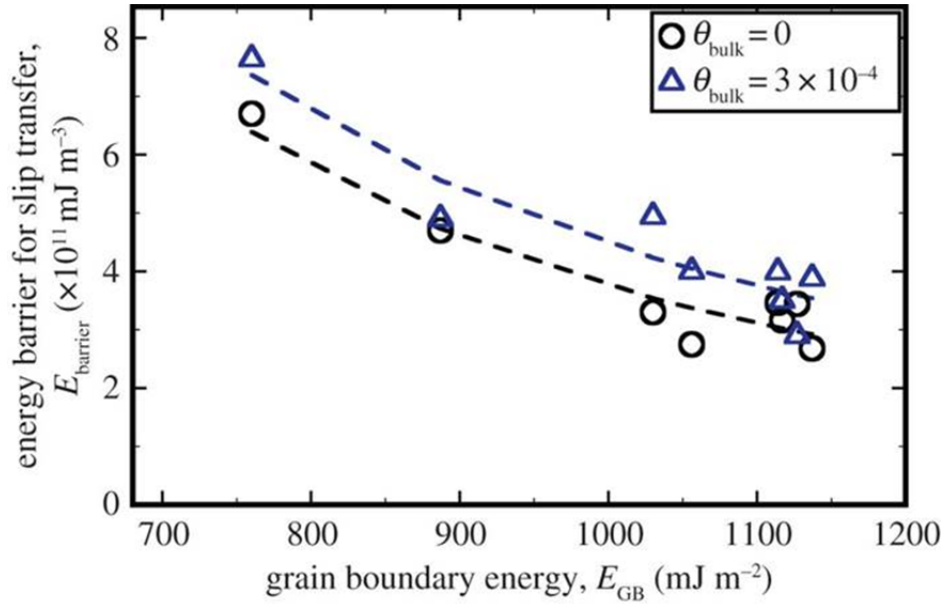


Fig. 1. Energy barrier for dislocation slip transfer across an Fe grain boundary

The above figure shows the energy barrier for dislocation slip transfer across a Fe GB as a function of the GB energy and under two different hydrogen contents (figure from ¹¹). Clearly, low energy GBs have a higher energy barrier for slip transmission. This can be understood in terms of the stability of the interface. High energy boundaries tend to contain a large amount of disorder and boundary free volume that serves as sites of dislocation nucleation or migration sites in the case of dislocation transmission ^{12,13}. Low energy boundaries contain more coherent sites, less boundary free volume and are thus more stable making transmission relatively more difficult. The twin boundary (i.e. a highly-coherent $\Sigma 3$ boundary in the terminology of the coherent site lattice) is a good example of a comparatively stable interface. These observations

and understanding are in contrast to the reviewer's suggestion that a reduction in the stacking fault planar boundary energy necessarily results in a reduction in the transmission barrier as to be negligible for blocking dislocation motion.

In order to address the reviewer's concern, we have included the following sentences on line 258 age 13 of the manuscript (note that super-scripts in the following text refer to manuscript references).

“Previous MD simulations subjected nanotwinned Au nanowires to tension and reported significant strain hardening that was attributed to coherent twin boundaries serving as strong barriers to the glide of leading partial dislocations⁵. This phenomenon has also been observed in MD simulations of nanotwinned Cu samples where twin boundaries were observed to have a strong blocking effect on dislocations⁶. We note that both of these studies employed interatomic potentials with similar low stacking fault energies, 43.4 mJ/m² for Au potential⁵ and 44.42 mJ/m² Cu potential⁶ which compares to the stacking fault energies of 6.24 mJ/m²⁷ and 26 mJ/m²⁸ of potentials used in this study.”

Furthermore, the virial theorem used to compute the stress from their MD simulation is odd, as it is not clear if the authors have used the deformed or initial atomic volume in their equation. Using the initial atomic volume could yield inaccurate stress results when the simulation box is not periodic, large plastic deformation is applied and the model contains thin-walls. The authors should further clarify and verify their MD methodology.

Response: The formula we have used to calculate stress of the nanobox in the MD simulations is:

$$\sigma_{zz} = \frac{F_z}{A_0} = \frac{\sum v s_{zz} / L_z}{L_{x0} L_{y0}}$$

In the equation, the numerator is computed using the standard definition of virial stress of the instantaneous nanobox configuration. In analogy to experiments, this is the instantaneously measured force. In order to match the experimental calculation of engineering stress, we divide by the initial cross-sectional area of the nanobox sample.

In order to address the reviewer's concern, we have included the following sentences in the manuscript on line 437 page 21.

“This form was chosen to most closely match the computation of engineering stress in experiments. The numerator in Eq. 3 uses the standard calculation of virial stress using the instantaneous sample configuration and is analogous to the instantaneous force as measured during compression experiments. In order to match the experimental calculation of engineering stress, we then divide by the initial cross-sectional area of the nanobox.”

While the manuscript quality is improving, I do not recommend its publication in Nature Communications yet without further evidence of the hardening mechanism at play.

Reviewer #4 comments:

After carefully reviewing the answers to the reviewer's comments, I believe that the authors sufficiently address the main concerns and have expanded the technical robustness of the paper.

However, I have two points for further clarification:

1. The FEM discussion did not appear to provide as much insight as the experimental tests or MD simulations. I think that using some language from the answers to the reviewers could

clarify the FEM. For example, the authors state during their reply to reviewers 2 and 3 that :
“The goal of the FEM simulations was actually not to reproduce the experimental results (this is left to the MD simulations, which are more appropriate for the size scale and complexity of the nanoboxes). Rather, the point of the FEM simulations is to answer the question, “What is the structural response for a material model that does not include strain hardening?” The reason that this is relevant to our system, is that the solid Ag nanocube (the parent structure from which the nanobox is formed) does not show strain hardening.” Perhaps some version of this explanation could be incorporated into the text since it is not directly clear in the manuscript why the FEM presented is for a solid rather than a hollow system.

Response: The reviewer has misunderstood - the FEM simulation included in the manuscript is of a hollow smooth nanobox, which was described on line 207 page 10 of the manuscript. FEM of a solid silver nanocube was included in supplementary information (line 47 page 3) to check that the solid cube results in the expected material response for an elasto-plastic material. In this way, we know that we can trust the results for the hollow nanocube. As suggested by the reviewer, we have clarified this issue and added an explanation of the purpose of the FEM simulation on page 10 line 205 of the manuscript (note that super-scripts in the following text refer to manuscript references):

“For further insight into the influence of structural architecture on deformation, a hollow smooth nanobox is simulated using FEM analysis. The purpose of this FEM simulation is to determine the structural response for a material that does not include strain hardening. This is relevant because the solid Ag nanocube (the parent structure from which the nanobox is formed) does not show strain hardening under compression.¹⁴ In this way, the FEM simulation reveals the deformation of a hollow box, without consideration of material or size effects. Thus, an elastic

plastic material model that does not include strain hardening was used in the FEM simulation, to mimic the material response of a Ag single crystal nanocube.¹⁴ The FEM model was then constructed to have a similar geometry as the experimental nanobox, with smooth walls and a hollow interior.”

2. The Au:Ag ratios discussion is a bit confusing (pages 6&7). Are the authors implying that the Au:Ag ratios are 70/30 and 30/70? Those are two different alloys and perhaps the observed differences are highly impacted by the alloy composition. I think this section can be clearer and simply stating that the mechanical properties of Au and Ag are similar is not a sufficient explanation.

Response: Yes, the estimated ratios of Au:Ag are 30:70 in the smooth nanobox samples and 70:30 in the rough nanobox samples. The discussion of the elemental ratios is intended to notify readers of this difference in compositions for the two samples. By stating that the mechanical behavior of Au and Ag are similar, we mean that the Au-Ag interface is not expected to significantly impact dislocation and stacking fault transmission. This has been observed in our previous study of Au-Ag core shell nanocubes,¹⁵ in which dislocations were able to cross the Au-Ag interface, such that the stress-strain response of the Au-Ag nanocubes was similar to that of solid Ag nanocubes.¹⁴ This behavior is not unexpected, considering the interactions of dislocations with bimetallic interfaces that are used to design nanolaminates and precipitate hardened alloys.^{16–18} Au and Ag form a coherent interface without significant lattice mismatch. This type of interface does not provide significant strengthening, or obstacles to dislocations, and

will not block the passage of dislocations. This issue has been clarified in the manuscript on line 124 on page 7:

“This difference in composition is not expected to cause a significant difference in the properties of the smooth and rough nanoboxes. The Ag and Au interface does not impede the passage of dislocations or stacking faults, such that the difference in composition should not affect the deformation mechanism for the nanoboxes.”¹⁵

References

1. Wang, J., Cao, G., Zhang, Z. & Sansoz, F. Size-dependent dislocation–twin interactions. *Nanoscale* **11**, 12672–12679 (2019).
2. Dou, R. & Derby, B. Deformation mechanisms in gold nanowires and nanoporous gold. *Philos. Mag.* **91**, 1070–1083 (2011).
3. Catlin, A. & Walker, W. P. Mechanical Properties of Thin Single-Crystal Gold Films. *J. Appl. Phys.* **31**, 2135–2139 (1960).
4. Matsukawa, Y. & Zinkle, S. J. Dynamic observation of the collapse process of a stacking fault tetrahedron by moving dislocations. *J. Nucl. Mater.* **329–333**, 919–923 (2004).
5. Deng, C. & Sansoz, F. Enabling Ultrahigh Plastic Flow and Work Hardening in Twinned Gold Nanowires. *Nano Lett.* **9**, 1517–1522 (2009).
6. Wu, Z. X., Zhang, Y. W. & Srolovitz, D. J. Dislocation–twin interaction mechanisms for ultrahigh strength and ductility in nanotwinned metals. *Acta Mater.* **57**, 4508–4518 (2009).

- 194 7. Foiles, S. M., Baskes, M. I. & Daw, M. S. Embedded-atom-method functions for the fcc
195 metals Cu, Ag, Au, Ni, Pd, Pt, and their alloys. *Phys. Rev. B* **33**, 7983–7991 (1986).
- 196 8. Sheng, H. W., Kramer, M. J., Cadien, A., Fujita, T. & Chen, M. W. Highly optimized
197 embedded-atom-method potentials for fourteen fcc metals. *Phys. Rev. B* **83**, 134118
198 (2011).
- 199 9. Wirth, B. D., Bulatov, V. V. & de la Rubia, T. D. Dislocation-Stacking Fault Tetrahedron
200 Interactions in Cu. *J. Eng. Mater. Technol.* **124**, 329–334 (2002).
- 201 10. Marian, J., Martínez, E., Lee, H.-J. & Wirth, B. D. Micro/meso-scale computational study
202 of dislocation-stacking-fault tetrahedron interactions in copper. *J. Mater. Res.* **24**, 3628–
203 3635 (2009).
- 204 11. Adlakha, I. & Solanki, K. N. Critical assessment of hydrogen effects on the slip
205 transmission across grain boundaries in α -Fe. *Proc. R. Soc. A Math. Phys. Eng. Sci.* **472**,
206 20150617 (2016).
- 207 12. Tschopp, M. a., Tucker, G. J. & McDowell, D. L. Structure and free volume of $\langle 110 \rangle$
208 symmetric tilt grain boundaries with the E structural unit. *Acta Mater.* **55**, 3959–3969
209 (2007).
- 210 13. Tucker, G. J., Tschopp, M. A. & McDowell, D. L. Evolution of structure and free volume
211 in symmetric tilt grain boundaries during dislocation nucleation. *Acta Mater.* **58**, 6464–
212 6473 (2010).
- 213 14. Kiani, M. T., Patil, R. P. & Gu, X. W. Dislocation surface nucleation in surfactant-
214 passivated metallic nanocubes. *MRS Commun.* 1–5 (2019).

- 215 15. Kiani, M. T., Wang, Y., Bertin, N., Cai, W. & Gu, X. W. Strengthening Mechanism of a
216 Single Precipitate in a Metallic Nanocube. *Nano Lett.* **19**, 255–260 (2019).
- 217 16. Beyerlein, I. J., Demkowicz, M. J., Misra, A. & Uberuaga, B. P. Defect-interface
218 interactions. *Progress in Materials Science* **74**, 125–210 (2015).
- 219 17. Beyerlein, I. J. *et al.* Structure-property-functionality of bimetal interfaces. *JOM* **64**,
220 1192–1207 (2012).
- 221 18. Nembach, E. *Particle strengthening of metals and alloys*. (Wiley, 1997).
- 222

Reviewers' Comments:

Reviewer #4:

Remarks to the Author:

The authors have fully addressed my concerns and modified the manuscript accordingly. The paper should be accepted.