

Supplementary Information

Observation of Electron Orbital Signatures of Single Atoms within Metal-Phthalocyanines using Atomic Force Microscopy

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Supplementary Methods

Additional Simulation Methods

For AFM image simulations, we employ a quantum based computational method developed by J. R. Chelikowsky and coworkers¹, which differs from the particle-probe model² (a charge-density-based method). Although some groups^{3, 4, 5} model the tip with additional Cu atoms above the CO molecule, we find the inclusion of a Cu cluster has a negligible effect in terms of the interaction energy^{6, 7, 8, 9}. As a result, we model the CO tip with a previously optimized CO molecule. We generate 2D raster grids in the x-y plane over the sample molecules at three different tip heights (separated by 15.9 pm) and compute the total energy of the tip-sample system (E_{ts}) at each grid point. We then combine the small amplitude approximation and the three-point central finite-difference method to compute the relative frequency shift $(\Delta f)^{1, 10}$. The tip height in simulation is defined as the distance above the averaged z-coordinate of each MPc molecule (we set 312 pm to be our zero point). In addition, we use a tip-tilting correction developed by Guo *et al.*¹¹ to account for the effect of lateral force. A tip-tilting correction, in general, results in more distinct and sharper bond features^{5, 12}. We compute the displacement of the CO tip in the x and y directions, $\vec{\Delta}_{lat}(x, y)$, by assuming a linear relationship between the lateral force, $\vec{F}_{lat}(x, y)$, and the lateral displacement using Eq. (1):

$$\vec{\Delta}_{lat}(x, y) = \frac{\vec{F}_{lat}(x, y)}{k_{CO}} \quad (1)$$

where k_{CO} is the lateral spring constant of the CO tip. k_{CO} is an adjustable empirical parameter which is set to be 0.8 N/m here.

Since we have shown that the attraction between the center Fe atom in FePc and the two bridge Cu atoms is not negligible⁶, we simulate the AFM images of MPcs with (Supplementary Figs. 1 a&c) and without (Fig. 2c of the main text) Cu substrates. When the substrate is not included, we perform both spin-polarized and spin-paired calculations. In this case, a modification of the substrate could result in a change in the local spin state of the center metal atom. However, when the substrate is included, we only perform spin-polarized calculations because it is not realistic to quench the spin with the presence of the Cu(111) substrate. We find the inclusion of the Cu(111) substrate results in a slightly bright metal center (for both Fe and Co). We attribute this to the trans effect¹³. The interactions

between the metal center in MPcs and the Cu substrate weaken the constraints of the electrons from the nuclei in z direction. The inclusion of the Cu(111) substrate makes the AFM simulations extremely expensive. To reduce the computational cost to a reasonable value, we employ the frozen density embedding theory (FDET)^{9, 14} which divides the total charge density of a system ($n^{tot}(\mathbf{r})$) into two subsystems – tip ($n^t(\mathbf{r})$) and the sample ($n^s(\mathbf{r})$):

$$n^{tot}(\mathbf{r}) = n^t(\mathbf{r}) + n^s(\mathbf{r}) \quad (2)$$

Then the total energy functional, $E_{tot}[n^t(\mathbf{r}), n^s(\mathbf{r})]$, becomes:

$$\begin{aligned} E_{tot}[n^t(\mathbf{r}), n^s(\mathbf{r})] = & \iint \frac{\{n^t(\mathbf{r}) + n^s(\mathbf{r})\}\{n^t(\mathbf{r}') + n^s(\mathbf{r}')\}}{2|\mathbf{r} - \mathbf{r}'|} d\mathbf{r} d\mathbf{r}' \\ & + \int \{V_{nuc}^t(\mathbf{r}) + V_{nuc}^s(\mathbf{r})\}\{n^t(\mathbf{r}) + n^s(\mathbf{r})\} d\mathbf{r} \\ & + T_s[n^t] + T_s[n^s] + T_s^{nadd}[n^t, n^s] + E_{xc}[n^t + n^s] + E_{nuc} \end{aligned} \quad (3)$$

where V_{nuc} , T_s , E_{xc} and E_{nuc} represent the nuclear potential (or ionic potential when pseudopotentials are used), kinetic energy functional, exchange-correlation energy functional, and nuclear-nuclear interaction energy, respectively. The nonadditive kinetic energy term, $T_s^{nadd}[n^t(\mathbf{r}), n^s(\mathbf{r})]$, is approximated by adopting the analytic form of the kinetic energy functional proposed by Tran and Wesolowski¹⁵. Within FDET, we treat $V_{nuc}^s(\mathbf{r})$ and $n^s(\mathbf{r})$ as constants which are computed previously using one single full DFT run of the sample system. Next, we define the embedding potential of the sample, $V_{emb}(\mathbf{r})$, as:

$$\begin{aligned} V_{emb}(\mathbf{r}) = & \int \frac{n^s(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' + V_{nuc}^s(\mathbf{r}) + \frac{\delta E_{xc}[n]}{\delta n} \Big|_{n=n^{tot}} \\ & - \frac{\delta E_{xc}[n]}{\delta n} \Big|_{n=n^t} + \frac{\delta T_s[n]}{\delta n} \Big|_{n=n^{tot}} - \frac{\delta T_s[n]}{\delta n} \Big|_{n=n^t} \end{aligned} \quad (4)$$

and the ordinary Kohn-Sham potential of the tip as the effective potential, $V_{eff}^t(\mathbf{r})$:

$$V_{eff}^t(\mathbf{r}) = \int \frac{n^t(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' + V_{nuc}^t(\mathbf{r}) + \frac{\delta E_{xc}[n]}{\delta n} \Big|_{n=n^t} \quad (5)$$

We can then obtain the following Schrödinger-like equation in FDET using Eqs. (4) and (5):

$$\left[\frac{-\nabla^2}{2} + V_{eff}^t(\mathbf{r}) + V_{emb}(\mathbf{r}) \right] \psi_i^t(\mathbf{r}) = \epsilon_i^t \psi_i^t(\mathbf{r}) \quad (6)$$

where ϵ_i^t and ψ_i^t are a set of Kohn-Sham eigenvalues and wavefunctions.

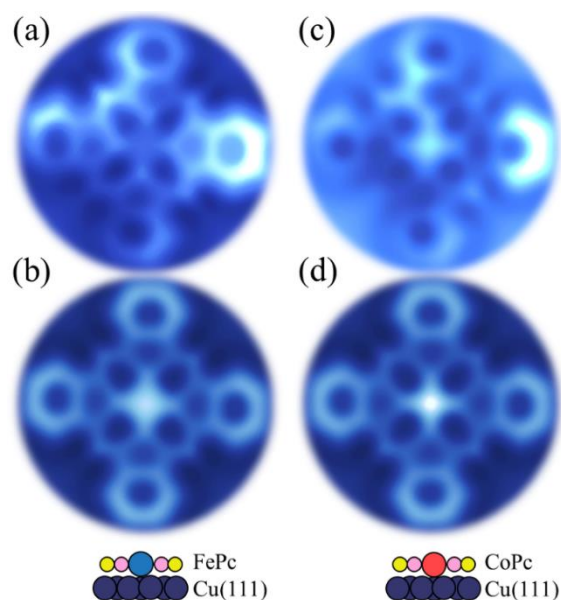
Pseudopotentials

We use Troullier-Martin norm-conserving pseudopotentials¹⁶. Specifically, for Fe, Co and Cu atoms, we use relativistic spin-polarized calculations to construct their pseudopotentials. Although other construction methods have been proposed for dealing with transition-metal atoms^{17, 18, 19}, we did not employ the methods in this work as our pseudopotentials (for systems like FePc/CO-FePc with and without Cu(111) substrates) provided good results in our previous work⁶. In addition, we find that including a nonlinear core correction¹⁷ for Fe and Co (tested isolated FePc and CoPc molecules only) does not induce any influential structural change or charge redistribution.

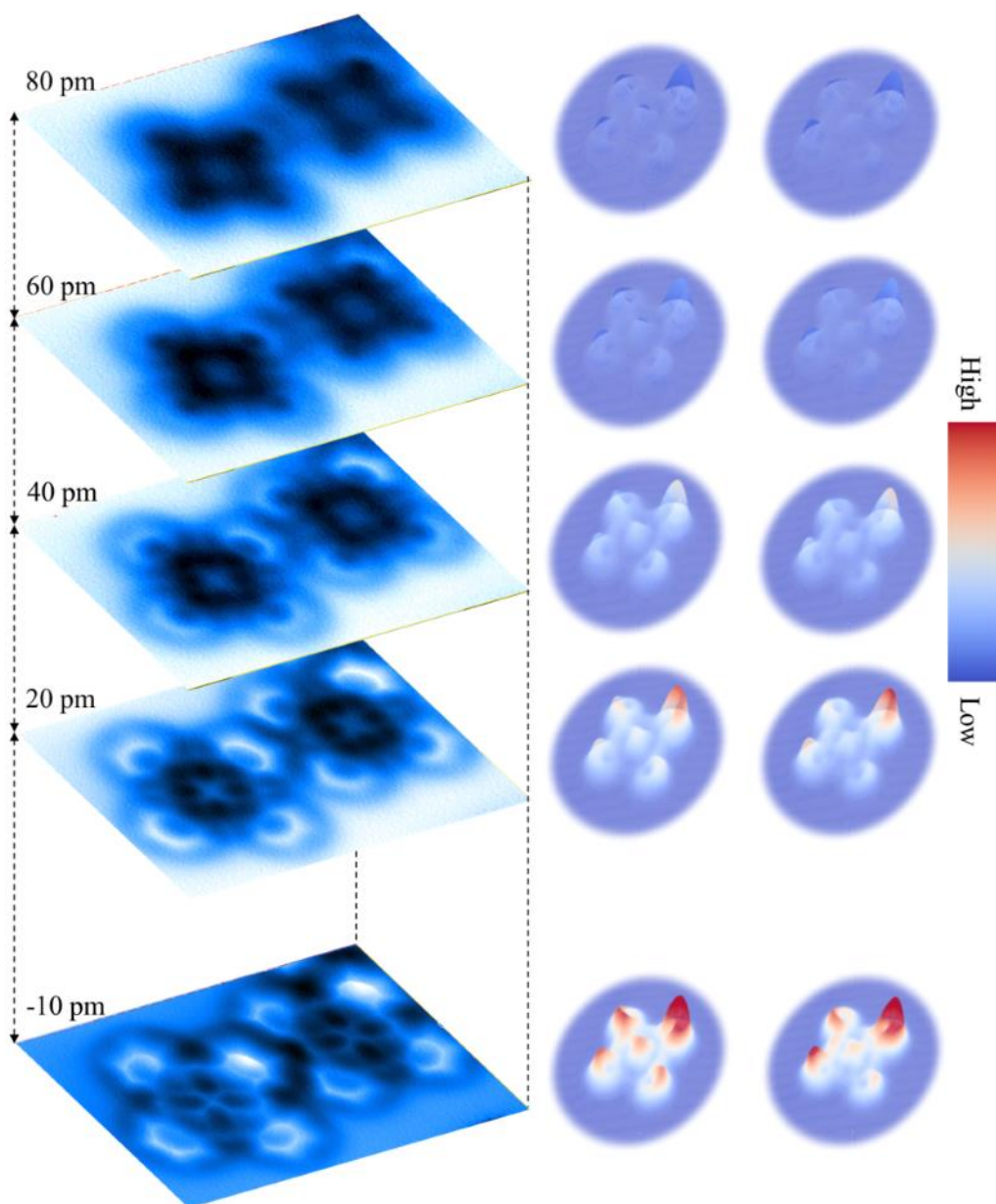
Exchange-Correlation Functionals

For the exchange-correlation (EX) functional, we tested local density approximations by Ceperley-Alder (CA)²⁰ and by Perdew-Wang (PW92)²¹. As CA and PW92 give similar results (adsorption height, molecular geometry and simulated AFM images), the calculations shown in the main text refer to CA only. A recent theoretical study on FePc and CO-FePc systems confirm that the choice of EX functional has very slight influence in terms of Fe-N bond length for a specific spin state²².

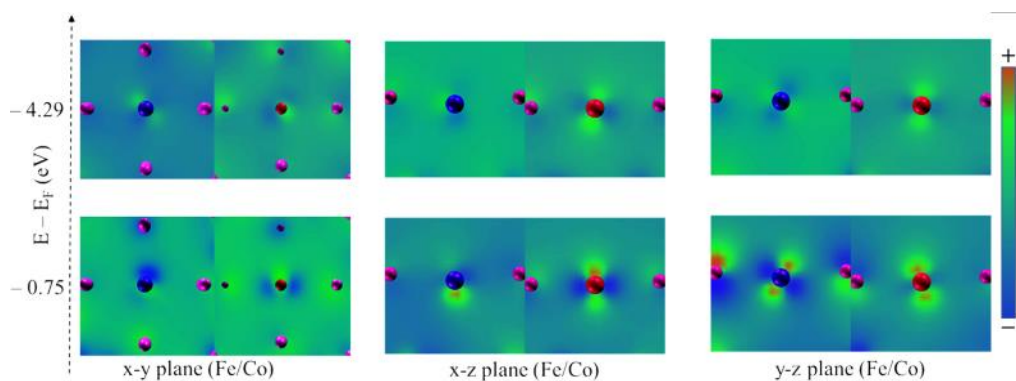
Supplementary Figures



Supplementary Fig 1. Simulated AFM images of FePc and CoPc on Cu(111) at a tip height of -10 pm (CO tip). (a-b) FePc; (c-d) CoPc. The center metal atom is placed at a bridge site. The Cu substrate is included in these spin-polarized DFT calculations. In (b) and (d), the MPc molecules are fully planar (no structural relaxations performed).



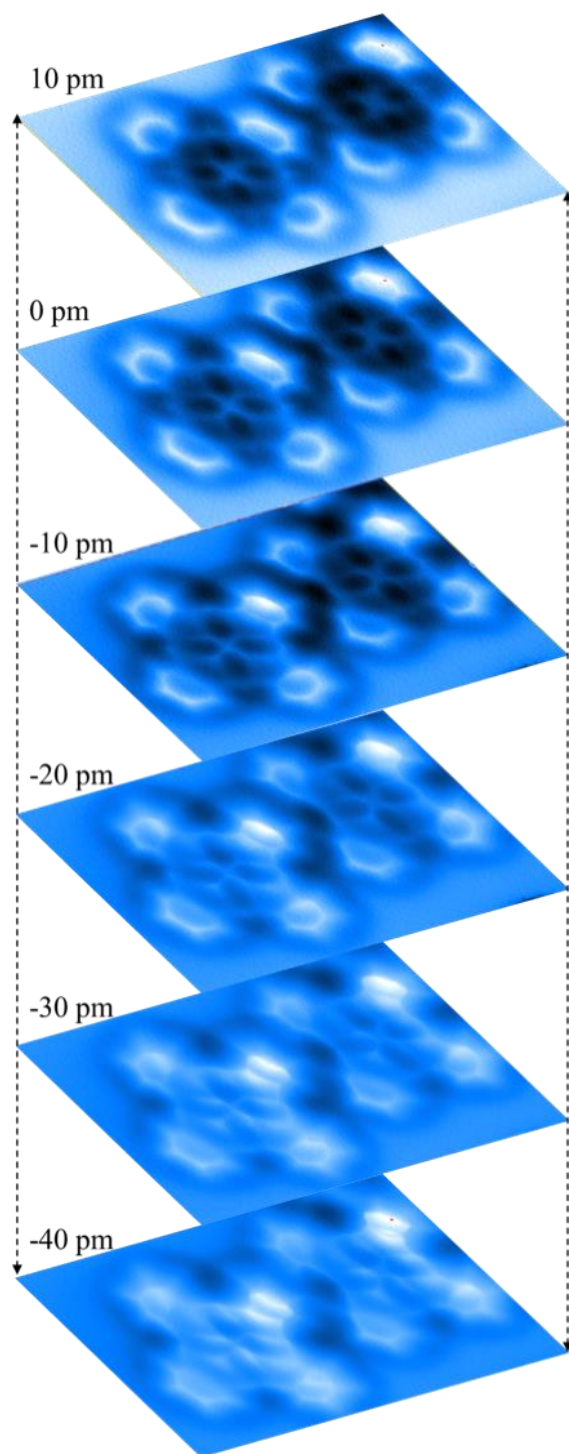
Supplementary Fig 2. Experimental AFM images (left panel) and the corresponding computed 3D electron density maps (right panel) at different tip heights. The experimental tip height is relative to a STM set point (100mV/100pA).



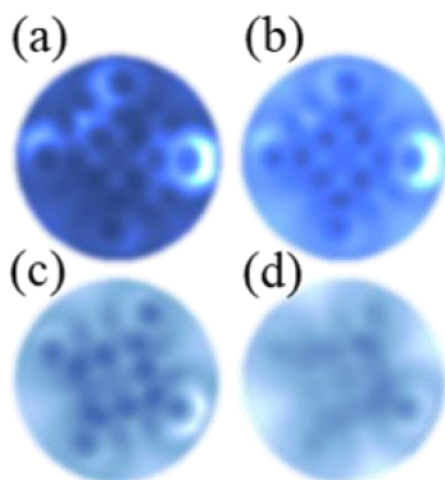
Supplementary Fig 3. 2D volume slice views of combined wavefunctions of MPc on Cu(111). Top panel: states that are 4.29 eV below Fermi level; bottom panel: states that are 0.75 eV below Fermi level. The molecular models are overlapped with the slices. Blue: Fe, red: Co, pink: N atoms.



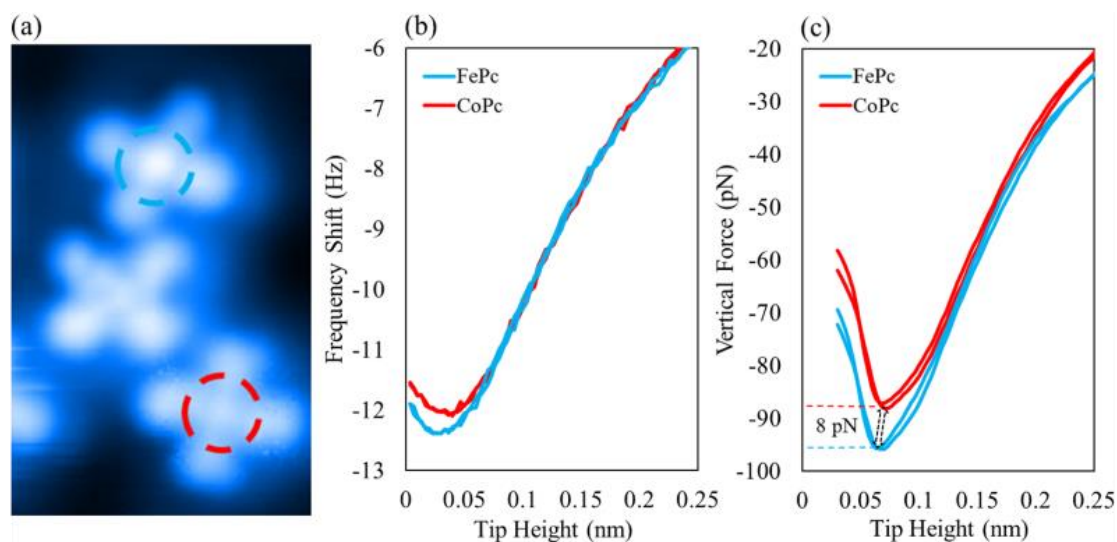
Supplementary Fig 4. 3D electron density maps. The computed 3D electron density map of CoPc when it is intentionally lifted upward by 12.6 pm from the zero point.



Supplementary Fig 5. Additional experimental AFM images at different tip heights around the zero point. The tip height is relative to a STM set point (100mV/100pA).



Supplementary Fig 6. Additional simulated AFM images of FePc (a-b) and CoPc (c-d) at larger tip heights. Tip heights are 5.9 pm (a & c) and 21.8 pm (b & d). Spin-polarized DFT calculations are used.



Supplementary Fig 7. Additional experiment performed using a different CO tip show that FePc and CoPc are clearly distinguishable based on either frequency shift or force despite the curves are slightly shifted. (a) STM image of FePc and CoPc molecules using a CO tip ($V = 100$ mV, $I = 30$ pA). (b) Measured frequency shift (Hz) and (c) vertical force (pN) acting on the CO tip when it is placed on the top of the (circled in (a)) center metal atom.

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