
Mantle heterogeneity influenced Earth's ancient magnetic field

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1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100

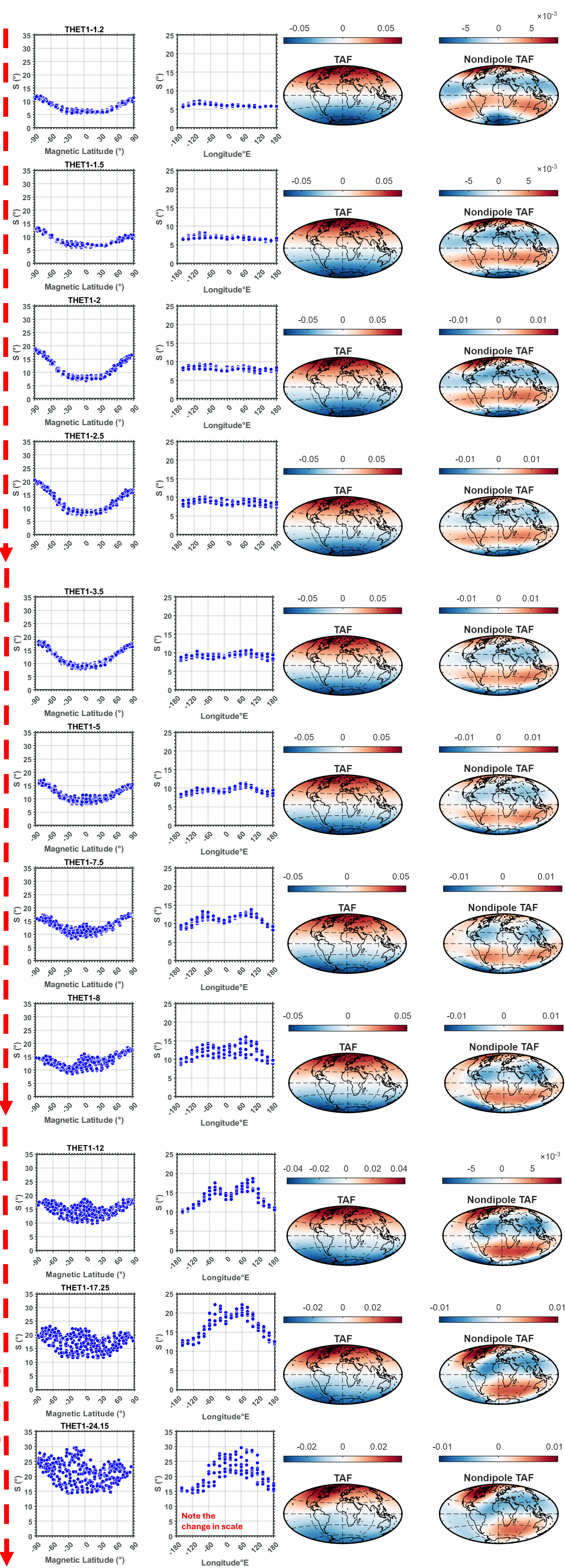


Supplementary Figure 1: Palaeosecular variation (PSV) and time-averaged field (TAF) output from THOM1 dynamo simulations (thermally driven with homogeneous outer boundary conditions). See Table S1 for input parameters of models and Figure 1 for descriptions of panels. All units are dimensionless unless specified. The M_Map tool⁵⁴ was used for mapping.

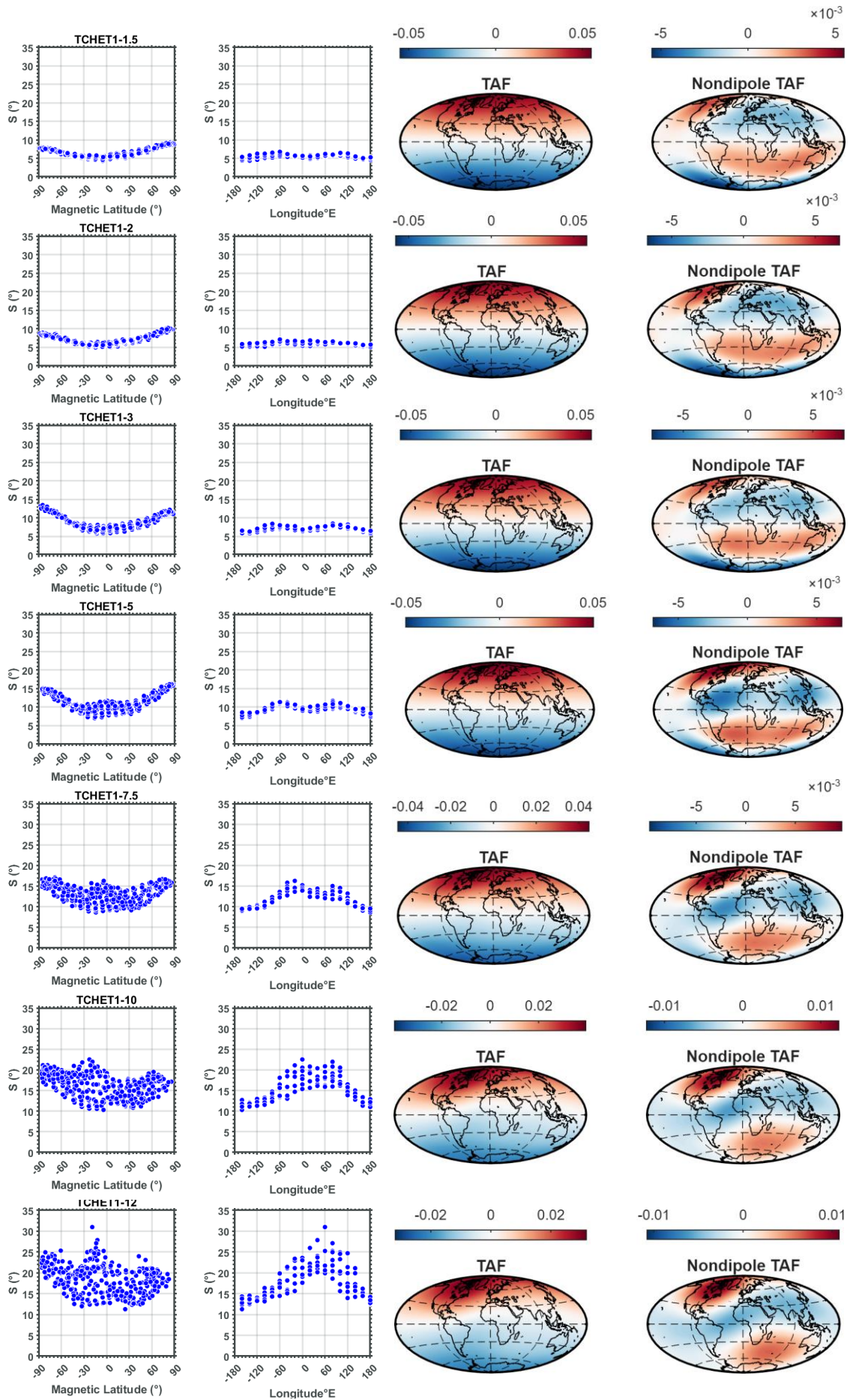
Increasing Rayleigh Number

Increasing Rayleigh Number

Increasing Rayleigh Number

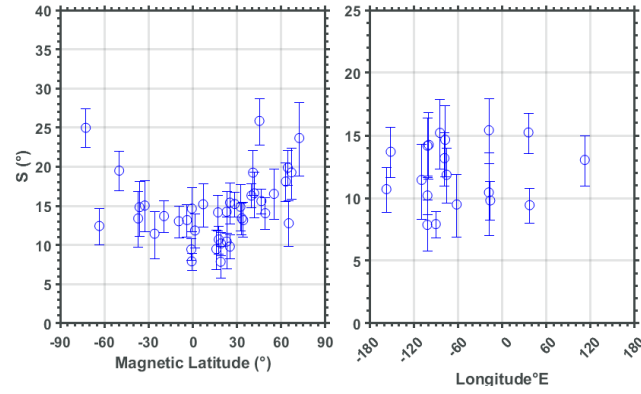


Supplementary Figure 2: Palaeosecular variation (PSV) and time-averaged field (TAF) output from THET1 dynamo simulations (thermally driven with heterogeneous outer boundary conditions). See Table S1 for input parameters of models and Figure 1 for descriptions of panels. All units are dimensionless unless specified. The M_Map tool⁵⁴ was used for mapping.



Supplementary Figure 3: Palaeosecular variation (PSV) and time-averaged field (TAF) output from TCHET1 dynamo simulations (thermochemically driven with heterogeneous outer boundary conditions). See Table S1 for input parameters of models and Figure 1 for descriptions of panels. All units are dimensionless unless specified. The M_Map tool⁵⁴ was used for mapping.

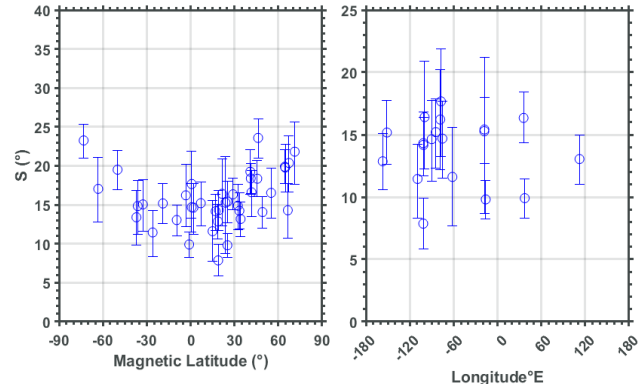
PSV10-24 (0-5 Ma)



Variable Cutoff applied

$$S_{|30|median} = 11.9 + 2.3 / - 1.7^{\circ}$$

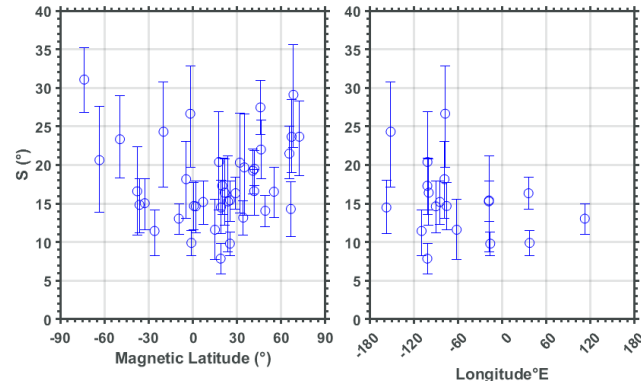
$$S_{|30|IQR} = 4.3 + 1.4 / - 1.9^{\circ}$$



45° Cutoff applied

$$S_{|30|median} = 14.6 + 0.6 / - 1.8^{\circ}$$

$$S_{|30|IQR} = 3.5 + 2.5 / - 2.4^{\circ}$$

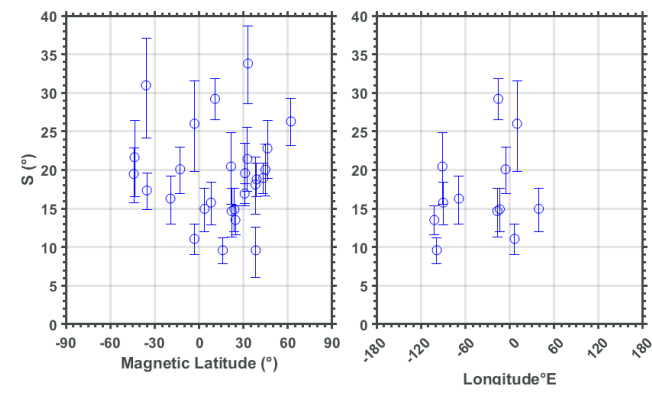


No cutoff applied

$$S_{|30|median} = 15.2 + 1.2 / - 2.2^{\circ}$$

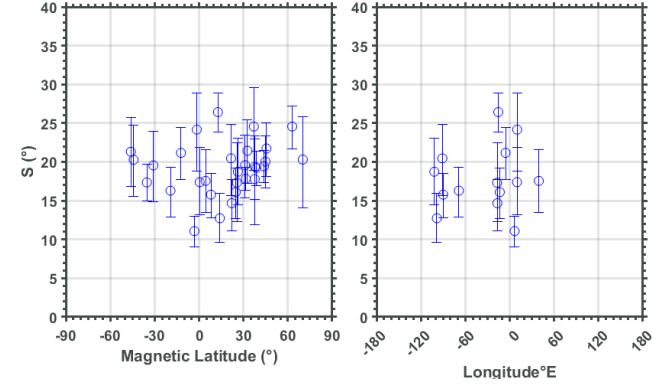
$$S_{|30|IQR} = 5.1 + 4.7 / - 3.4^{\circ}$$

PSVM (5-23 Ma)



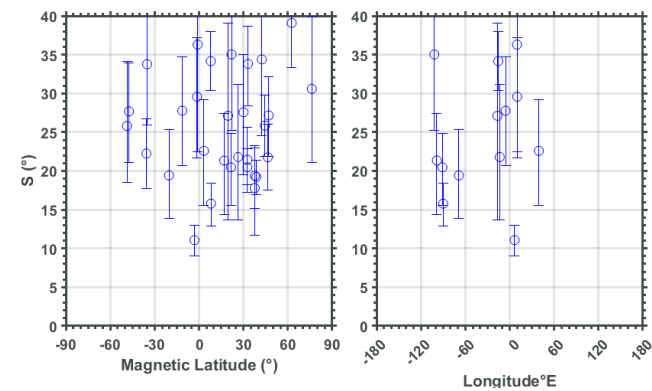
$$S_{|30|median} = 15.4 + 4.9 / - 1.3^{\circ}$$

$$S_{|30|IQR} = 6.2 + 7.6 / - 4.8^{\circ}$$



$$S_{|30|median} = 17.4 + 2.6 / - 1.6^{\circ}$$

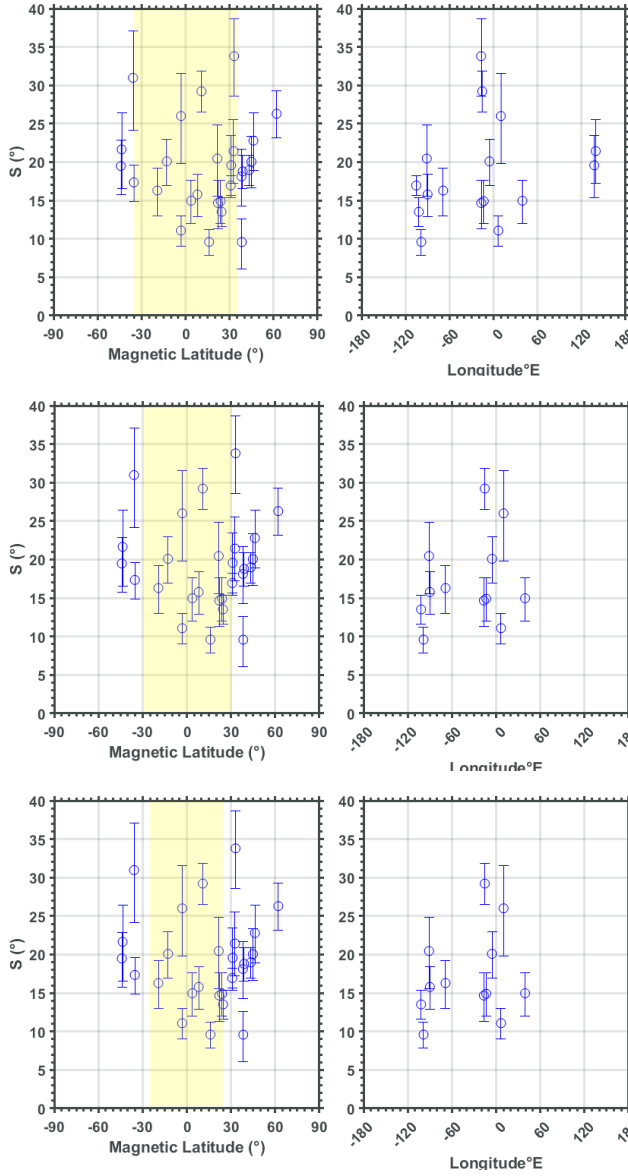
$$S_{|30|IQR} = 4.7 + 4.8 / - 3.3^{\circ}$$



$$S_{|30|median} = 22.6 + 7.0 / - 2.1^{\circ}$$

$$S_{|30|IQR} = 10.5 + 7.9 / - 6.6^{\circ}$$

Supplementary Figure 5: Illustration of effects of applying different VGP cutoffs to the two main PSV datasets^{27,35} used in this study. The variable cutoff was used throughout this study but parameters calculated using alternatives have overlapping uncertainty bounds with the exception of $S_{|30|median}$ for PSVM which is uniquely high. The data underlying all plots is identical and the same process (outlined in *Methods*) was followed for each except that a fixed cutoff of 45° or no cutoff was applied as indicated. S represents virtual geomagnetic pole dispersion as defined in *Methods* and error bars were calculated using 10,000 bootstraps with replacement.



$$S_{|35|median} = 16.6 + 3.8 / - 1.7^{\circ}$$

$$S_{|35|IQR} = 6.2 + 8.4 / - 2.8^{\circ}$$

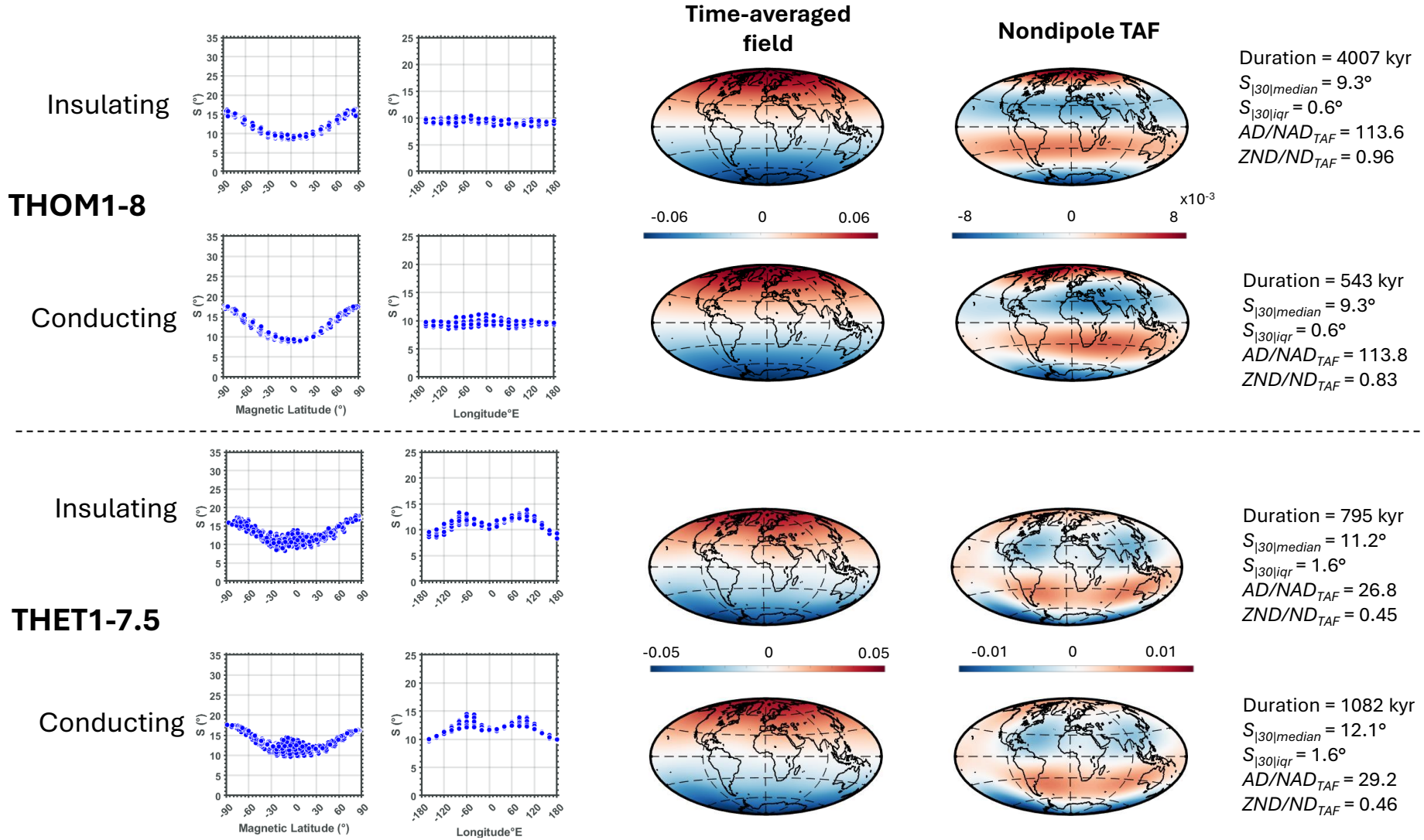
$$S_{|30|median} = 15.4 + 4.9 / - 1.3^{\circ}$$

$$S_{|30|IQR} = 6.2 + 7.6 / - 4.8^{\circ}$$

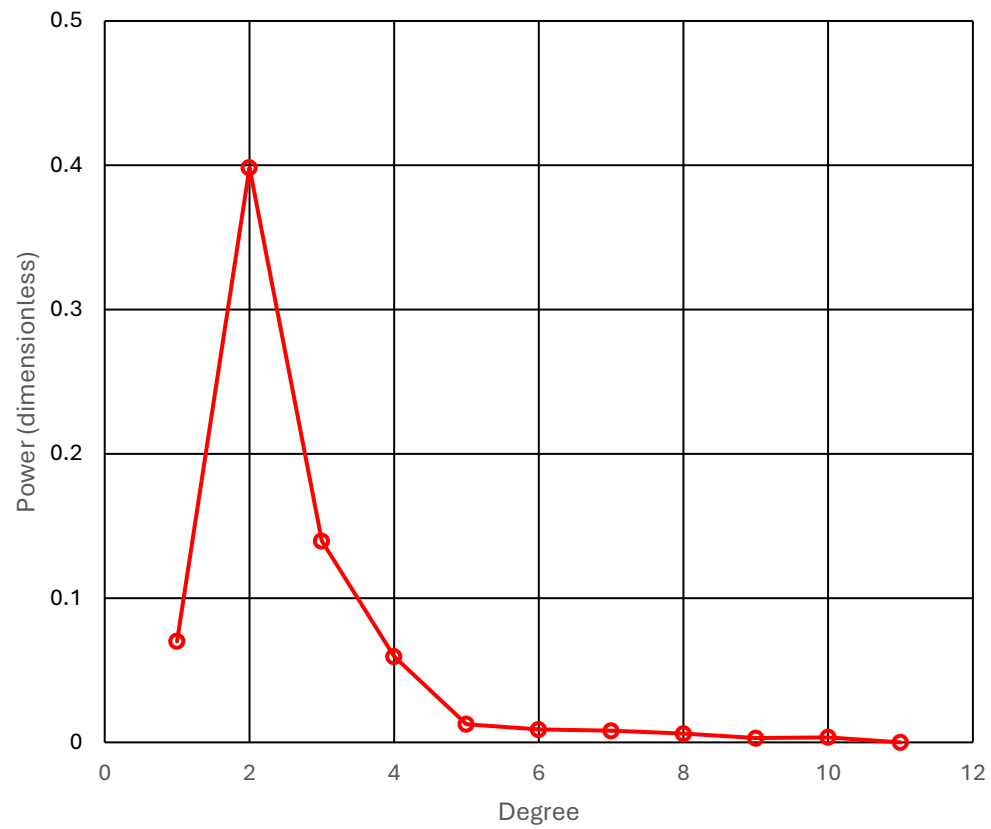
$$S_{|25|median} = 15.4 + 4.9 / - 1.3^{\circ}$$

$$S_{|25|IQR} = 6.2 + 7.5 / - 4.8^{\circ}$$

Supplementary Figure 6: Test of robustness for $S_{|30|median}$ and $S_{|30|IQR}$ for PSVM: the smallest, noisiest and, therefore, most at-risk dataset (Extended Data Table 1). Varying the latitudinal cutoff by $\pm 5^{\circ}$ is found to produce no significant impact on values. The data underlying all plots is identical and the same process (outlined in *Methods*) was followed for each except that the low latitude bounds were modified as indicated. S represents virtual geomagnetic pole dispersion as defined in *Methods* and error bars were calculated using 10,000 bootstraps with replacement.



Supplementary Figure 7: Outputs of magnetic field behaviour from two simulations shown alongside simulations run with identical input parameters except the inner core was changed from electrically insulating to conductive. For description of panels, see figure 1. For model parameters, see Table S1. All units are dimensionless unless specified. The M_Map tool⁵⁴ was used for mapping.



Supplementary Figure 8: Power spectrum of heat flow boundary condition used in the heterogeneous simulations.

Model	Reference	Group		Duration (kyr)	Ra_{τ}	Ra_c	AD/NAD_{median}	f_{dip}	E_m/E_k	Rm	Ro	f_{ohm}	$S_{ 30 median}$ (°)	$S_{ 30 iqr}$ (°)	AD/NAD_{TAF}	ZND/ND_{TAF}	
THOM1-1.5	This study	THOM1	$q^* = 0$	Thermal $E = 3 \times 10^{-4}$ $Pr = 1$ $Pm = 3$	3426	150	0	42.8	0.84	2.54	107	0.011	0.37	5.9	0.4	289.1	0.99
THOM1-2	Me21				5688	200	0	26.4	0.75	3.42	121	0.012	0.43	7.4	0.3	178.7	1.00
THOM1-3	Me21				5110	300	0	22.4	0.70	2.98	148	0.015	0.43	7.9	0.4	147.8	0.99
THOM1-4	Me21				4345	400	0	22.5	0.69	2.27	176	0.018	0.41	7.9	0.5	130.1	1.00
THOM1-8	Me21				4007	800	0	16.7	0.63	1.16	262	0.026	0.35	9.3	0.6	113.6	0.96
THOM1-12	Me21				3156	1200	0	12.1	0.57	0.75	333	0.033	0.31	11.4	0.6	136.4	0.97
THOM1-17.5	This study				765	1750	0	0.2	0.15	0.17	724	0.072	0.19	53.8	2.5	36.0	0.92
THET1-1.2	This study	THET1	$q^* = 2.3$		709	120	0	40.2	0.79	4.60	94	0.009	0.43	6.0	0.5	94.3	0.67
THET1-1.5	This study				2393	150	0	29.1	0.77	4.64	104	0.010	0.45	6.9	0.6	80.0	0.85
THET1-2	This study				2673	200	0	16.6	0.66	4.52	115	0.012	0.46	8.0	0.6	45.4	0.73
THET1-2.5	This study				708	250	0	14.1	0.64	3.84	148	0.015	0.45	8.4	0.9	45.2	0.83
THET1-3.5	This study				1230	350	0	13.8	0.63	2.61	156	0.016	0.40	9.1	0.7	40.1	0.67
THET1-5	This study				1718	500	0	13.7	0.61	1.76	205	0.021	0.36	9.3	1.1	40.6	0.62
THET1-7.5	This study				795	750	0	10.1	0.56	0.91	288	0.029	0.29	11.2	1.6	26.8	0.45
THET1-8	This study				182	800	0	9.4	0.53	0.91	274	0.027	0.34	11.9	2.9	28.0	0.44
THET1-12	This study				795	1200	0	7.9	0.50	0.60	340	0.034	0.27	13.9	3.6	24.2	0.32
THET1-17.25	This study				836	1725	0	5.7	0.46	0.46	389	0.039	0.26	16.8	5.7	19.2	0.29
THET1-24.15	This study				804	2415	0	3.5	0.38	0.34	496	0.050	0.24	20.7	7.0	11.6	0.29
TCHET1-1.5	This study	TCHET1	$q^* = 2.3$	Thermochemical $E = 3 \times 10^{-4}$ $Pr = 1$ $Pm = 3$	771	150	7500	53.2	0.82	1.73	125	0.013	0.31	5.4	0.6	224.5	0.34
TCHET1-2	This study				870	200	10000	42.2	0.78	1.56	146	0.015	0.31	5.9	0.8	155.6	0.36
TCHET1-3	This study				983	300	15000	27.8	0.72	1.13	185	0.019	0.29	7.1	1.0	118.9	0.46
TCHET1-5	This study				497	500	25000	16.7	0.64	0.79	244	0.024	0.27	9.6	1.6	82.2	0.50
TCHET1-7.5	This study				432	750	37350	10.8	0.57	0.56	306	0.031	0.25	12.2	3.6	35.5	0.41
TCHET1-10	This study				480	1000	49800	5.3	0.48	0.45	357	0.036	0.24	15.5	5.5	12.7	0.38
TCHET1-12	This study				385	1200	60000	3.8	0.41	0.37	398	0.040	0.23	17.4	6.9	9.3	0.35
THOM2-20	MD23	THOM2	$q^* = 0$	Thermal $E = 2 \times 10^{-5}$ $Pr = 0.2$ $Pm = 1$	121	2000	0	22.6	0.71	2.17	889	0.018	0.67	8.0	0.8	1008.3	0.76
THOM2-60	MD23	THOM2			127	6000	0	0.5	0.19	0.41	1848	0.037	0.52	46.0	10.3	52.6	0.90
THET2-20	MD23	THET2			116	2000	0	18.5	0.64	2.69	851	0.017	0.68	9.2	0.7	109.6	0.48
THET2-60	MD23	THET2			131	6000	0	25.0	0.66	0.85	1608	0.032	0.59	9.4	1.2	173.8	0.47
THET3-20	MD23	THET3			53	2000	0	8.5	0.54	3.54	830	0.017	0.69	12.0	2.5	21.4	0.36
THET3-60	MD23	THET3			91	6000	0	17.5	0.63	1.41	1483	0.030	0.61	9.6	1.8	68.8	0.63

Supplementary Table 1: Summary of studied dynamo simulations. References Me21 and MD23 refer to refs 67 and 11 respectively. Group refers to definitions given in the Methods where q^* is the thermal heterogeneity on the outer boundary, E is the Ekman number, Pr is the Prandtl number, and Pm is the magnetic Prandtl number. Calculated durations assume a magnetic diffusion time of 200 kyr. Ra_T and Ra_C are the thermal and chemical Rayleigh numbers respectively. AD/NAD_{median} is the median of the time series of time-instantaneous ratios of AD/NAD calculated at Earth's surface (ref 37; see Methods); f_{dip} is time-average dipolar fraction of the field at the core-mantle boundary (ref 69). E_m/E_k is the ratio of total magnetic and kinetic energies. Rm is the magnetic Reynolds number, Ro is the Rossby Number, and f_{ohm} is the fraction of Ohmic dissipation. Palaeosecular variation and time-averaged field parameters are given in the last four columns and are defined in the text.