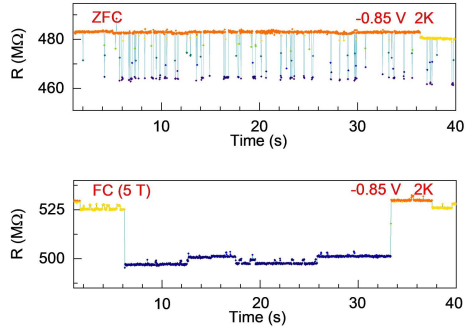


Electrically tunable magnetic fluctuations in multilayered vanadium-doped tungsten diselenide

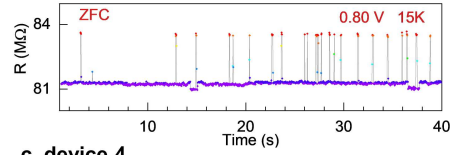
In the format provided by the
authors and unedited

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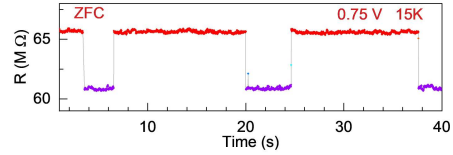
a. device 2



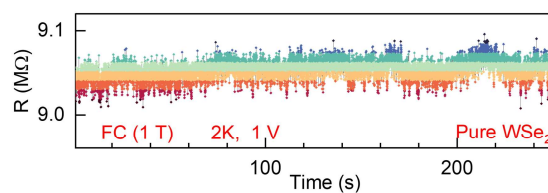
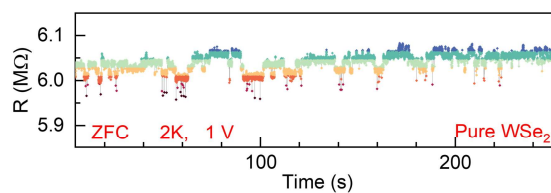
b. device 3



c. device 4

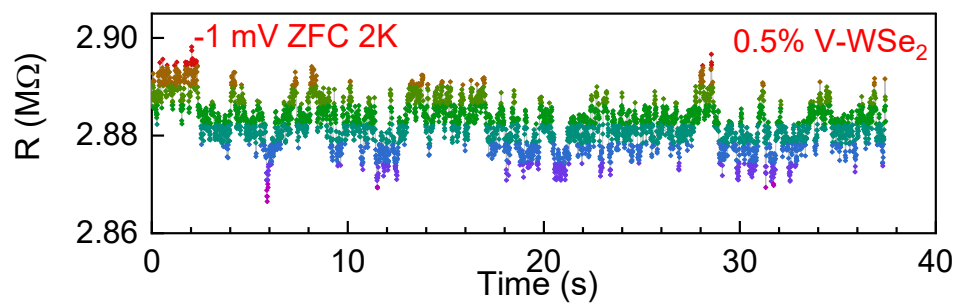


Supplementary Information Fig. 1 | Examples of RTN signals in various Gr/V-WSe₂/Gr devices. a, Time evolution of resistance change of device 2 at 0.8 V and 2 K after ZFC (top) and FC (5 T)(bottom), **b,** device 3 after ZFC at 0.8 V and 15 K, and **c,** device 4 after ZFC at 0.75 V and 15 K.

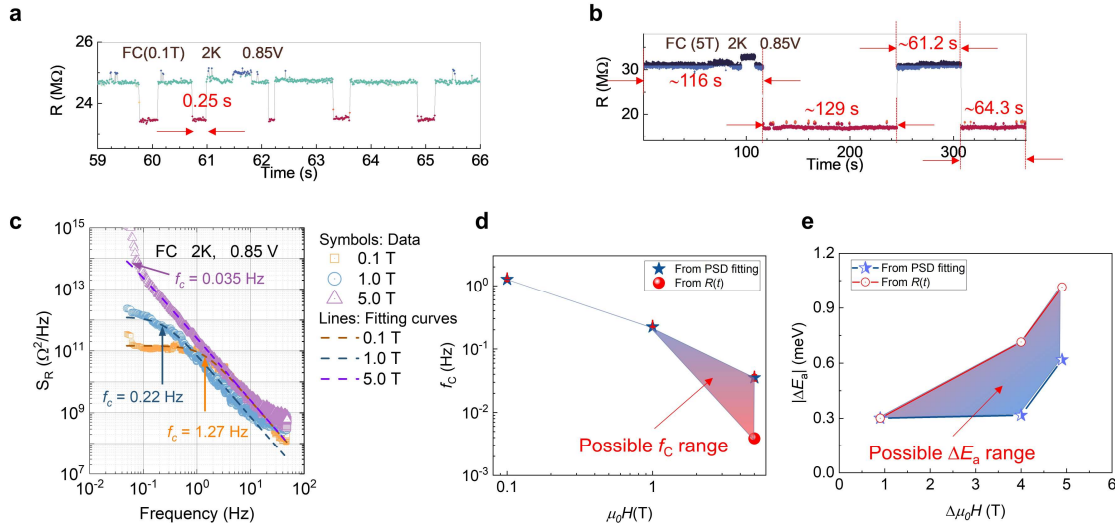


Supplementary Information Fig. 2 | Time evolution of resistance change in a Gr/WSe₂/Gr device.

Random noise from pure WSe₂ after ZFC (left) and FC (right) at 2 K and 1 V.



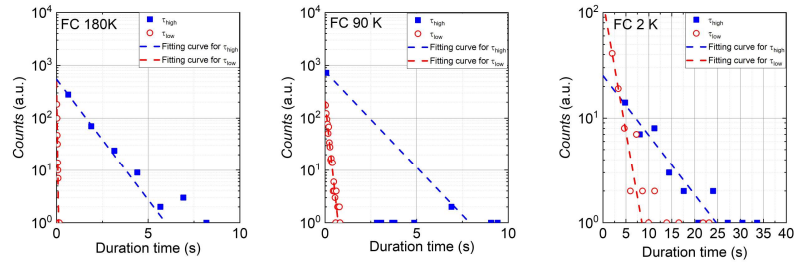
13
 14 **Supplementary Information Fig. 3 | Suppression of the RTN signal in high V-doping concentration**
 15 **(0.5% V-doped WSe₂).** The data were collected after ZFC at 2 K and -1 mV.



Supplementary Information Fig. 4 | Magnetic field-dependent power spectrum density (PSD) analysis of a Gr/V-WSe₂/Gr device. Time evolution of the resistance curve $R(t)$ at $V = 0.85$ V and 2 K after FC with **a**, $\mu_0 H = 0.1$ T or **b**, $\mu_0 H = 5.0$ T. **c**, PSD and corresponding $1/f^2$ fitting curves (dotted lines) as a function of magnetic field at $V = 0.85$ V and $T = 2$ K. **d**, Magnetic field -dependent f_c determined from PSD curve fitting and $R(t)$. After FC with high magnetic field, the number of jumps in the collected data is not large enough to accurately determine f_c , and we instead estimated this parameter from the $R(t)$ data. Error bars for f_c , standard deviation from obtained mean f_c (red cross). **e**, ΔE_a in the observed magnetic field at $T = 2$ K based on the f_c determined by PSD and $R(t)$. Shading areas in Figures S4d-e indicate a possible range for f_c and ΔE_a , respectively. See **Supplementary Note** for details.

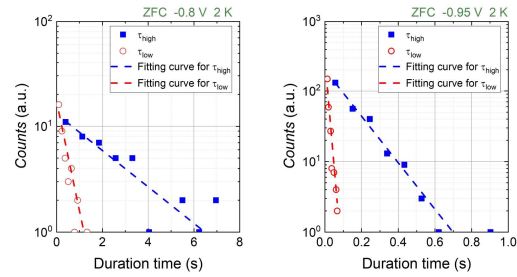
a.

Time constant analysis for data of Fig. 4a



b.

Time constant analysis for data of Fig. 5c



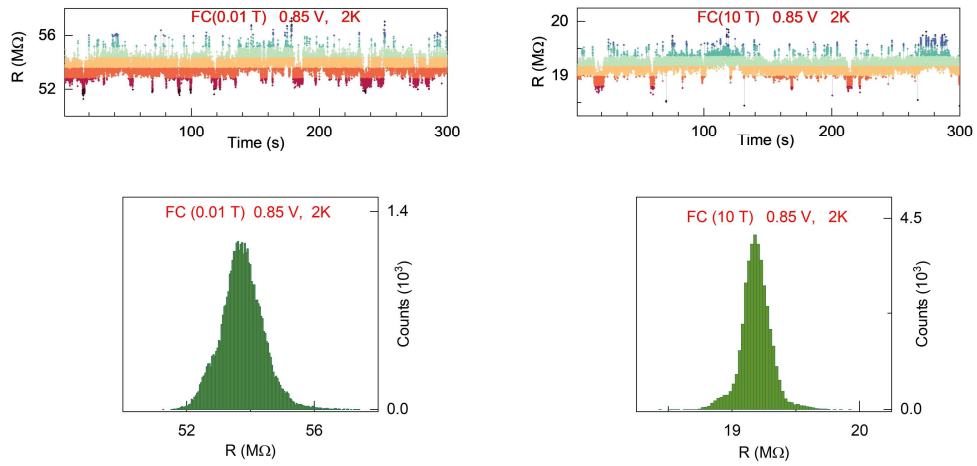
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28 **Supplementary Information Fig. 5 | Representative statistical RTN analysis for the time constant of**
 29 **high and low resistance levels of the RTN noise. a, temperature-dependence (Fig. 4a) and b, bias-**
 30 **dependence (Fig. 5c) time constants of RTNs.**

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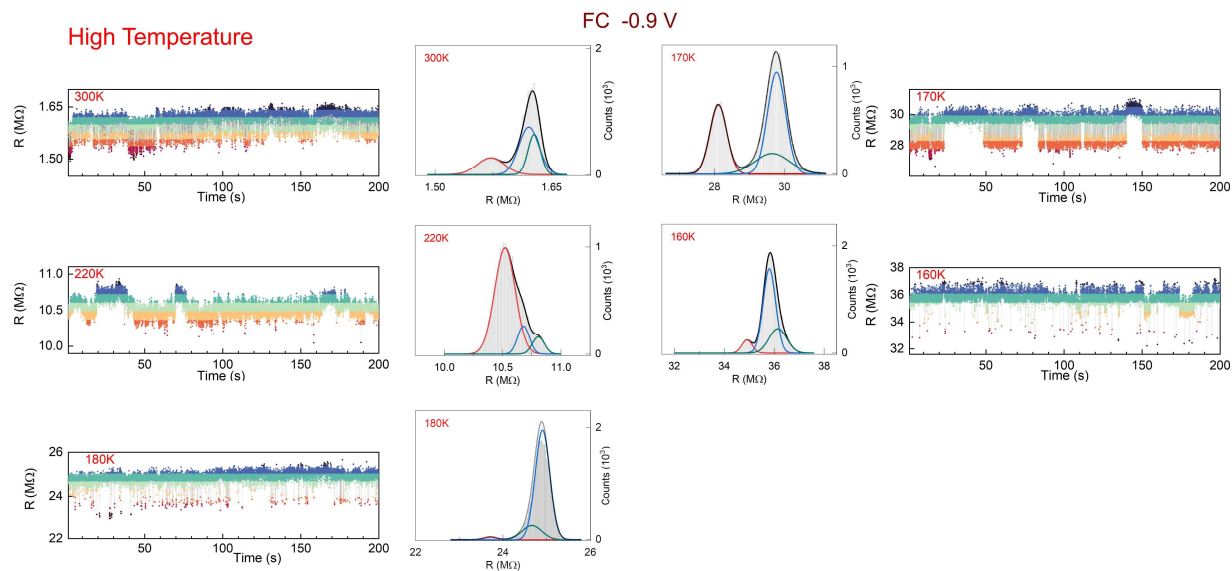
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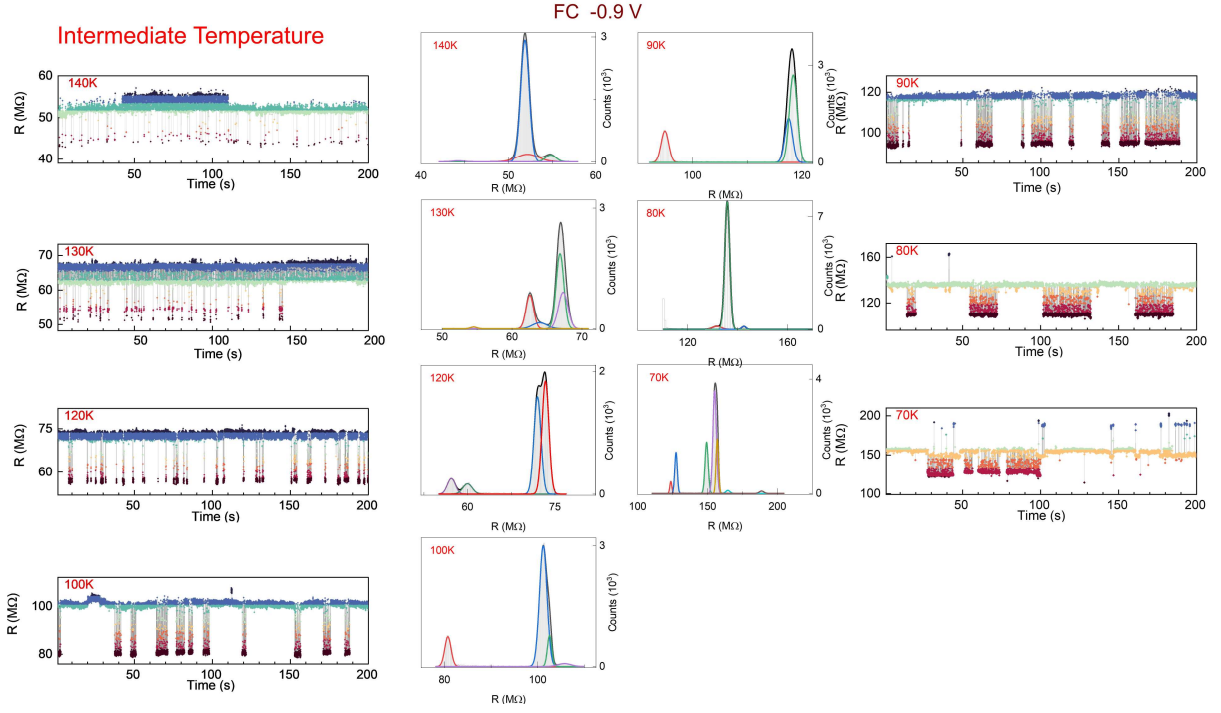
35 **Supplementary Information Fig. 6 | Control of RTNs at low and high magnetic fields.** RTNs (top) of
 36 device 1 at 2 K and 0.85 V without a magnetic field after FC with 0.01 T (left) or 10 T (right) with their
 37 corresponding single-peak histograms (bottom). No RTN signatures were observed in either condition.

38



Supplementary Information Fig. 7 | Time evolution of RTNs after FC (1 T) at -0.9 V in the high-temperature region above 140 K (160–300 K) and corresponding histograms with deconvoluted curves. The histograms were well-fitted with multiple peaks. Relative resistance changes (ΔR_{norm}) were $\sim 5\%$, corresponding to intralayer coupling interaction. Small $|\Delta R_{\text{norm}}|$ in the range of $\sim 1\%$ also appeared.

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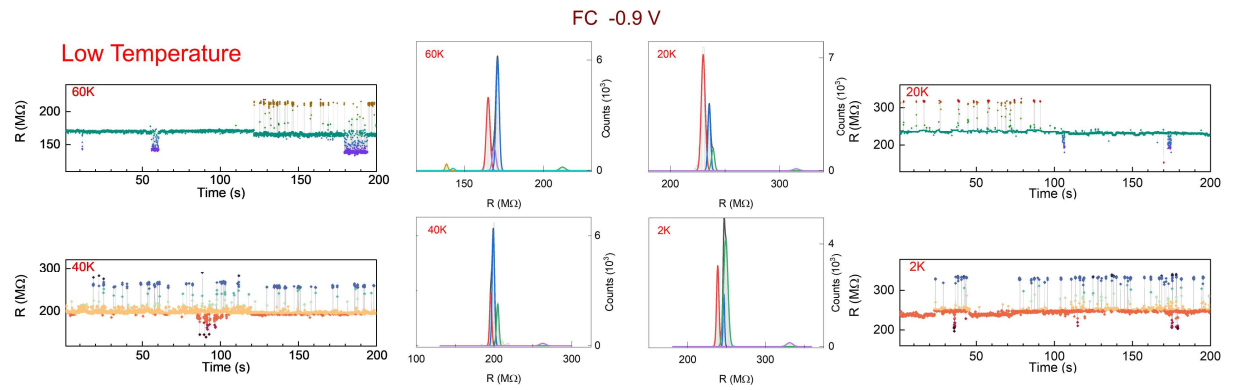
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47 **Supplementary Information Fig. 8 | Time evolution of RTNs after FC (1 T) at -0.9 V in the**
 48 **intermediate-temperature region (70–140 K) and corresponding histograms with deconvoluted**
 49 **curves. New peaks corresponding to giant $|\Delta R_{\text{norm}}|$ as large as $\sim 30\%$ are caused by the formation of**
 50 **interlayer coupling.**

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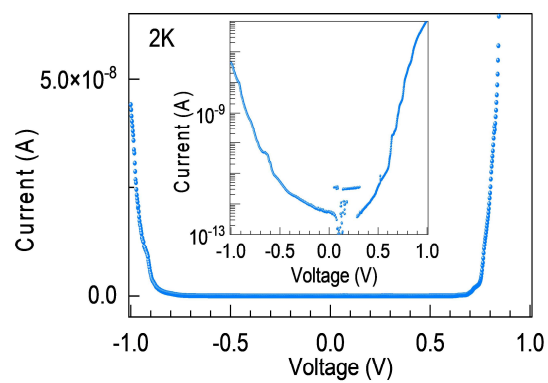
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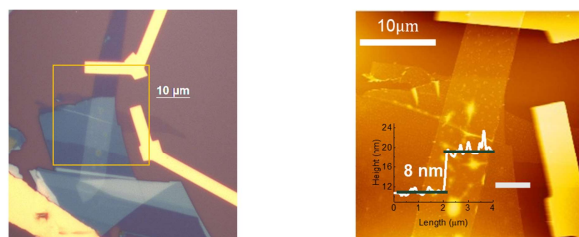
55 **Supplementary Information Fig. 9 | Time evolution of RTNs after FC (1 T) at -0.9 V in the low-**
 56 **temperature region below 70 K (2–60 K) and corresponding histograms with deconvoluted curves. A**
 57 **new peak corresponding to giant $|\Delta R_{\text{normS}}|$ as large as ~40% arises from the stable interlayer coupling.**

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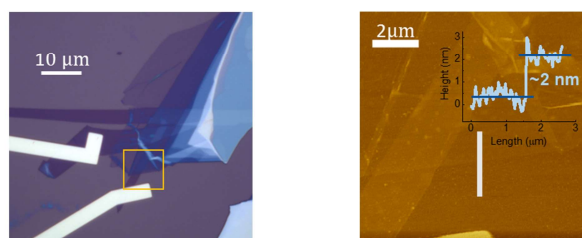


Supplementary Information Fig. 10 | The I-V characteristic of Gr/VWSe₂/Gr device 1 at 2 K in linear- and log-scales (inset) shows the Schottky junction's non-linear behavior.

a. Multilayer 0.1%V-WSe₂ (device 4)



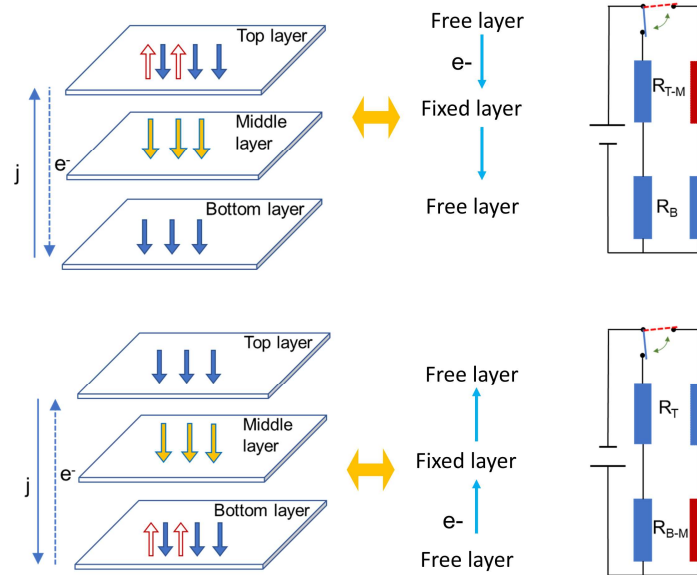
b. 2 nm-thick 0.1% V-WSe₂ (device 7)



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 65 **Supplementary Information Fig. 11 | AFM images of Gr/V-WSe₂/Gr device: a**, multilayer (device 4)
 66 have thickness around 5-8 nm, **b**, Thin layer has thickness around 2 nm (device 7)

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Spin-transfer torque in V-doped WSe₂ with different current flows



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70 **Supplementary Information Fig. 12 | Trilayer model of spin-transfer torque of vertical Gr/multilayer**
 71 **V-WSe₂/Gr device with different current flows.**

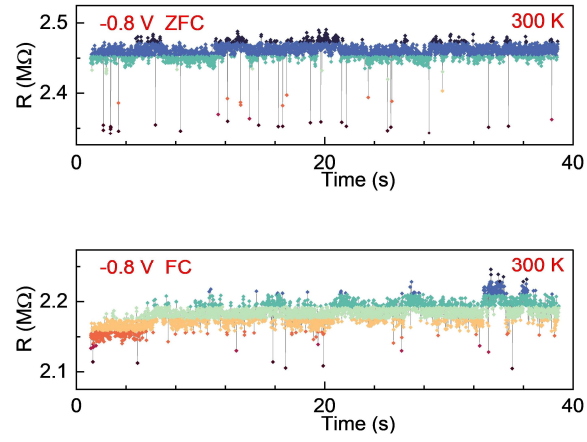
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78 **Supplementary Information Fig. 13 | RTN signal after ZFC and diminished after FC with -0.8 V at**
79 **300K. Data was measured in device 5.**

Device name	Thickness of V-WSe ₂ layer (nm)	Device dimensions (μm ²)
1	8	17x3
2	7	8x7
3	5	12x4
4	8	6x8
5	5	7x8
6	5	1x1
7	2	3x2

Supplementary Information Fig. 14 | Collection of the vertical 0.1% V- WSe₂ devices used in this paper.

Supplementary Note. The cut-off frequency $f_c = \frac{1}{2\pi\tau} = \frac{1}{2\pi\tau_0 \exp(\frac{E_a}{k_B T})} = f_0 \exp\left(-\frac{E_a}{k_B T}\right)$, where τ , τ_0 ($= 1/(2\pi f_0)$), E_a , k_B , and T denote the characteristic time constant, fitting constant for τ at a given temperature, activation energy, Boltzmann constant, and absolute temperature, respectively². These can be determined by fitting the PSD of magneto resistance fluctuation $S_R(f) = S_0 \frac{1}{\left(1 + \left(\frac{f}{f_c}\right)^2\right)} \propto 1/f^2$, where f and S_0 denote the respective frequency and noise plateau of $S_R(f)$ when $f < f_c$ (Supplementary Information Fig. S4a-c). f_c decreases with elevating magnetic fields, indicating the enhanced barrier height and suppressed transition rate between energy states 1 and 2 in the FC process (Supplementary Information Fig. S4d). The calculated τ from f_c ranging from 0.1 s to 1 s matches well to the time evaluation of RTN at $\mu_0 H = 0.1$ T (Supplementary Information Fig. S4a). Meanwhile, the estimated τ at $\mu_0 H = 5.0$ T is longer than 50 s, limiting an accurate determination of τ . Here, to define a realistic f_c , the effective τ ($1/\tau = 1/\tau_{\text{state1}} + 1/\tau_{\text{state2}} = 1.722$ mHz) was considered together on the basis of the time evolution resistance ($R(t)$) data as displayed in Supplementary Information Fig. S4b, particularly when $\mu_0 H = 5.0$ T. The Field-dependent f_c is presented in Supplementary Information Fig. S4d. In addition, the relative activation energy difference (ΔE_a) at $T = 2$ K was then estimated according to the following equations; $\Delta E_a = E_{a@ \mu_0 H = 1.0 \text{ T}} - E_{a@ \mu_0 H = 0.1 \text{ T}} = k_B T \cdot \ln\left(\frac{f_{c@ \mu_0 H = 0.1 \text{ T}}}{f_{c@ \mu_0 H = 1.0 \text{ T}}}\right)$.

References

1. Coey, J. M. D. *Magnetism and Magnetic Materials*. Nucl. Phys. vol. 13 (Cambridge University Press, 2001).
2. Grassler, T. *Noise in Nanoscale Semiconductor Devices*. Noise in Nanoscale Semiconductor Devices (Springer International Publishing, 2020). doi:10.1007/978-3-030-37500-3.