

Supplementary Information

Tuning scalar spin chirality in ultrathin films of the kagome-lattice ferromagnet Fe₃Sn

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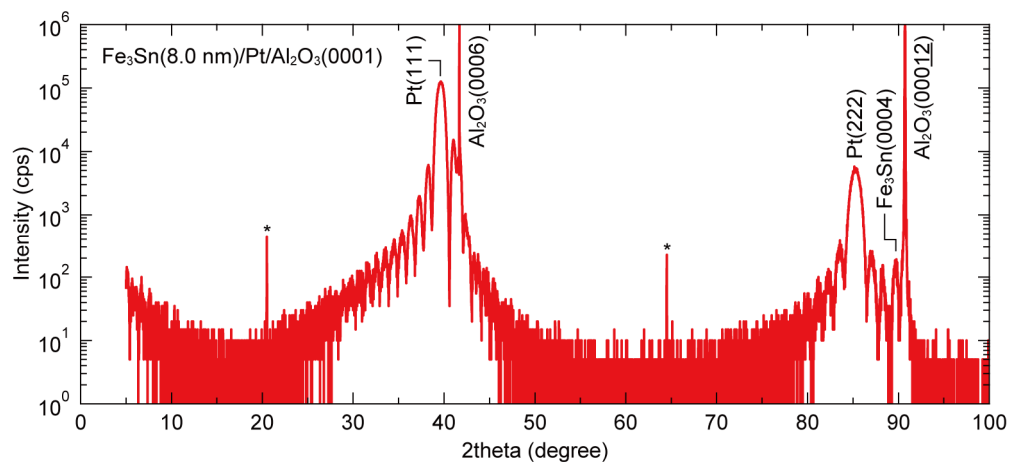
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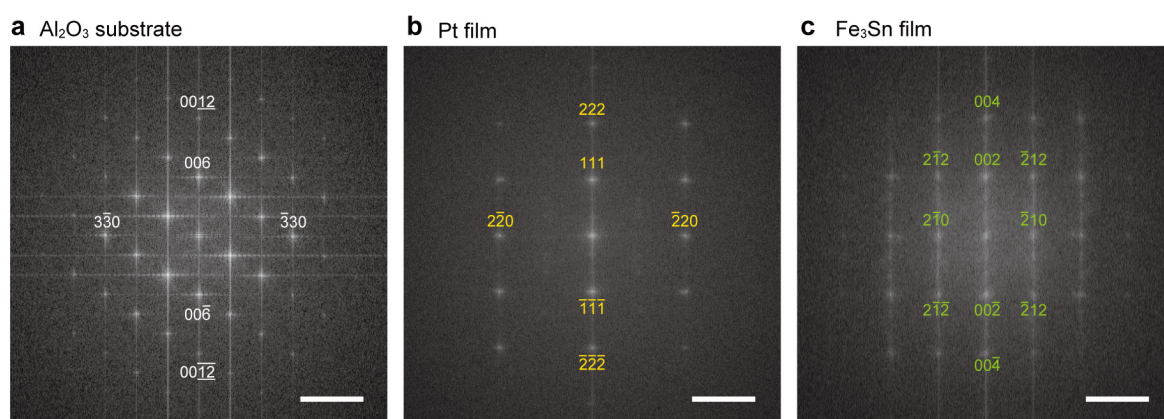
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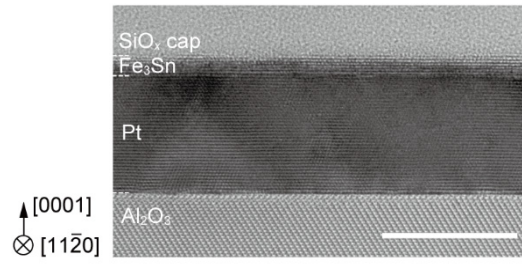
Supplementary Figures



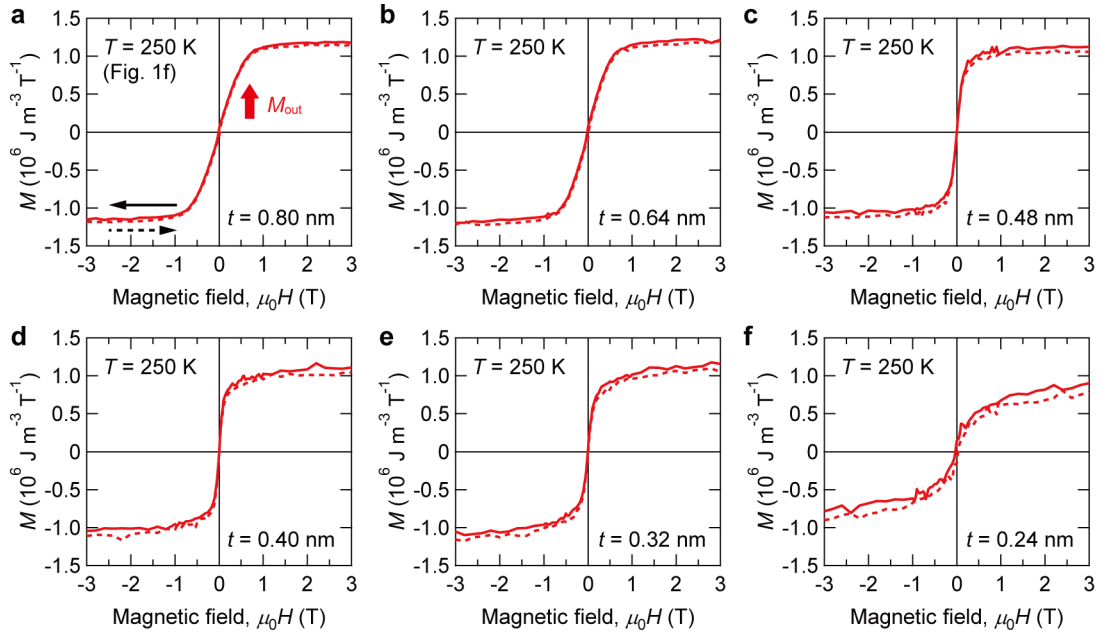
Supplementary Figure 1. Out-of-plane X-ray diffraction pattern of a 8.0-nm-thick Fe₃Sn/Pt/Al₂O₃(0001) sample analyzed by TEM. Although the Fe₃Sn(0002) peak at $2\theta \sim 41^\circ$ overlaps with the strong Pt(111) peak and the associated thickness fringes, the Fe₃Sn(0004) peak is discerned at $2\theta = 89.8^\circ$. Asterisks indicate forbidden reflections of Al₂O₃.



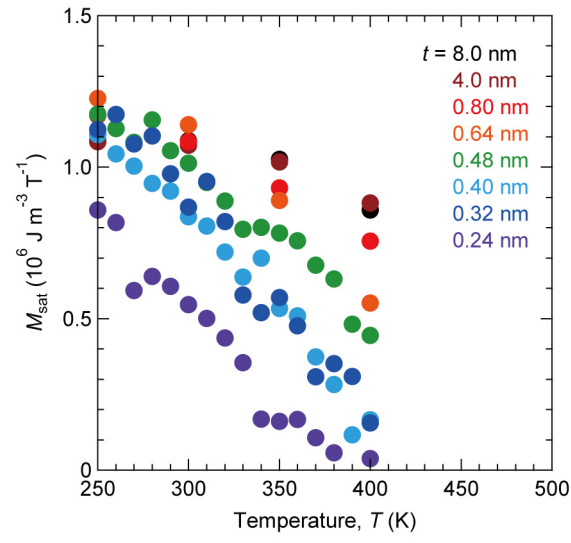
Supplementary Figure 2. Fast Fourier transformation (FFT) diffraction patterns calculated from the TEM image shown in Fig. 1d. a,b,c, The Al_2O_3 substrate, Pt film, and Fe_3Sn film regions, respectively. Scale bar, 5 nm^{-1} . The result of (c) is consistent with the high-temperature Fe_3Sn phase (JCPDS PDF 01-074-5857).



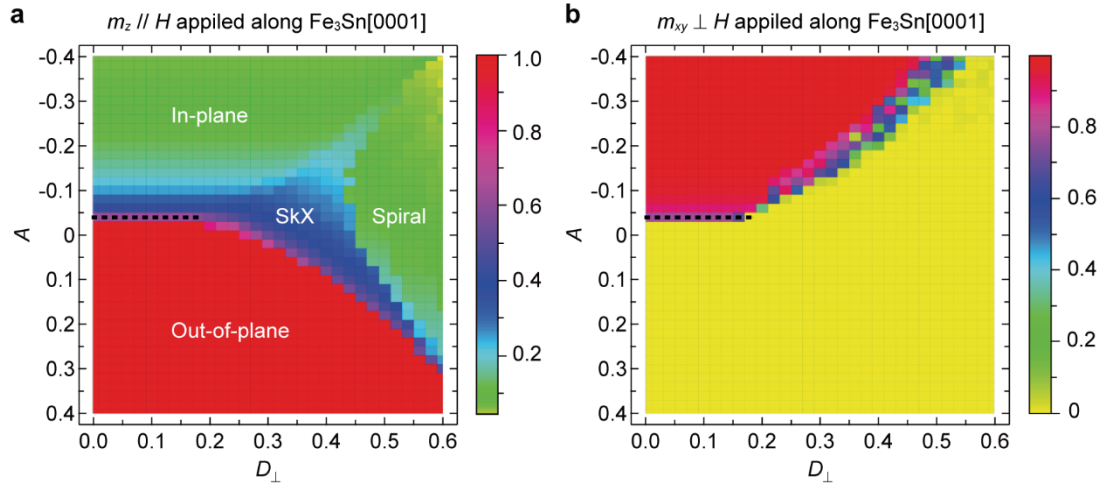
Supplementary Figure 3. Cross-sectional TEM image of a Fe₃Sn/Pt bilayer sample with $t = 1.6$ nm viewed along Al₂O₃[11 $\bar{2}$ 0]. Scale bar, 10 nm.



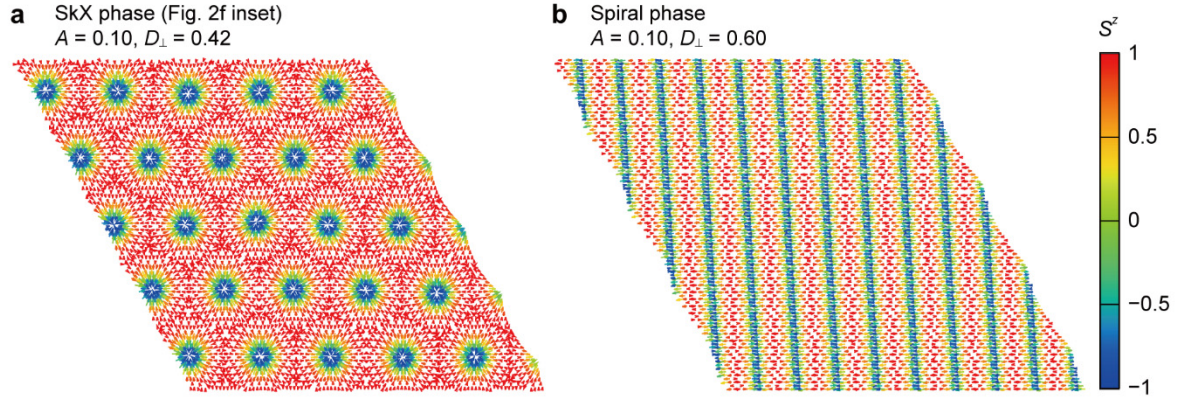
Supplementary Figure 4. M versus $\mu_0 H$ curves of $\text{Fe}_3\text{Sn}/\text{Pt}$ bilayer samples measured in an out-of-plane H . Typical data taken at $T = 250$ K are shown. **a**, $t = 0.80$ nm, **b**, $t = 0.64$ nm, **c**, $t = 0.48$ nm, **d**, $t = 0.40$ nm, **e**, $t = 0.32$ nm, and **f**, $t = 0.24$ nm. The data for $t = 0.80$ nm are replotted from Fig. 1f. The red solid and dashed curves correspond to the decreasing-field and increasing-field branches, as shown by the black solid and dashed arrows, respectively.



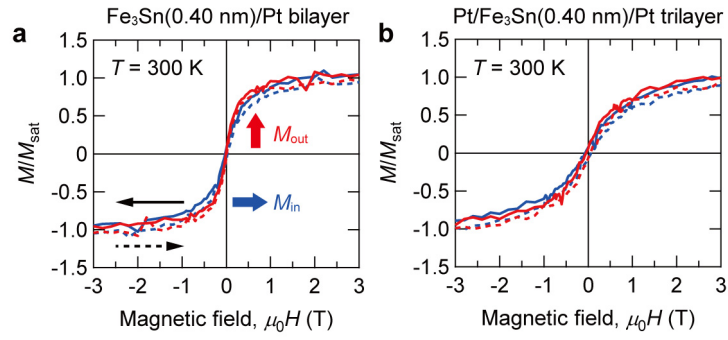
Supplementary Figure 5. T dependence of M_{sat} for $\text{Fe}_3\text{Sn}/\text{Pt}$ bilayer samples with $t = 8.0\text{--}0.24 \text{ nm}$.



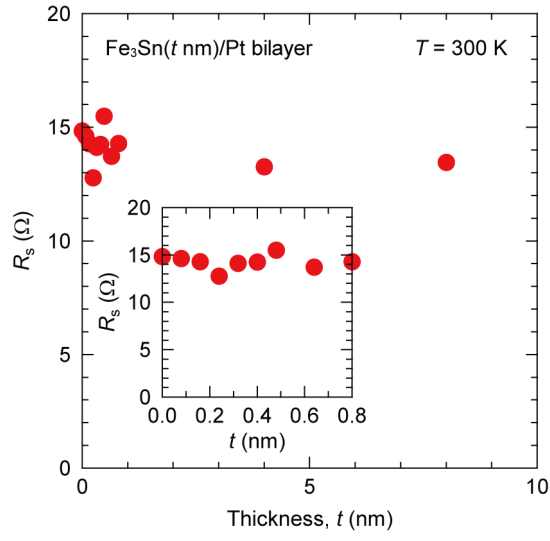
Supplementary Figure 6. Simulation results of magnetic moments in Fe₃Sn single layer. a, Out-of-plane magnetization component m_z , **b,** in-plane magnetization component m_{xy} in an magnetic field H applied along the out-of-plane Fe₃Sn[0001] direction. Dotted lines indicate the boundary between the in-plane and out-of-plane phases. Typical spin textures in the SkX and spiral phases are shown in Supplementary Fig. 7.



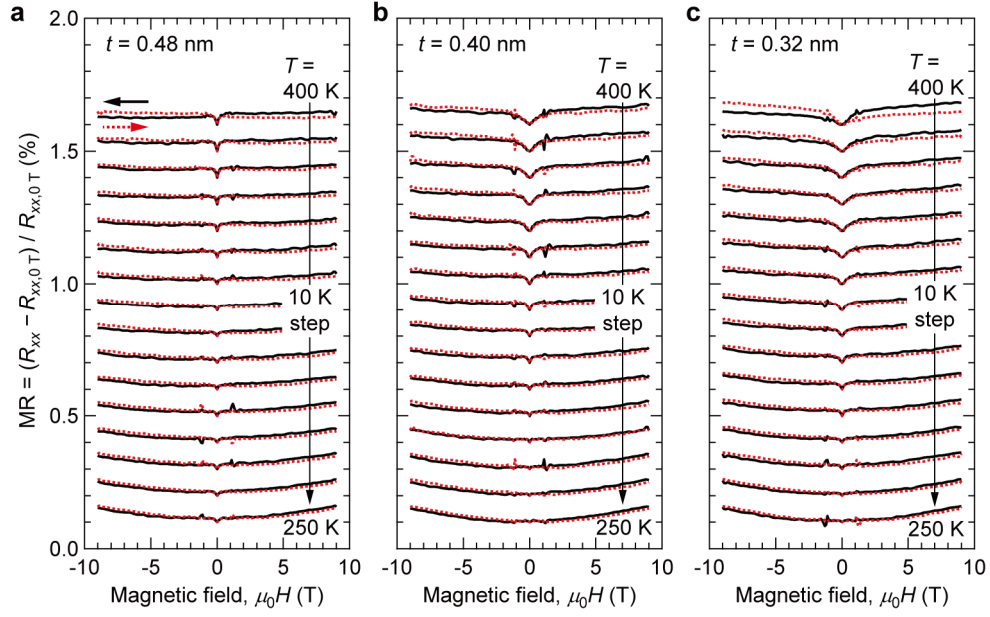
Supplementary Figure 7. Simulation results of spin textures in Fe_3Sn single layer. **a**, The SkX phase obtained with $A = 0.10$ and $D_{\perp} = 0.42$ (magnified image of Fig. 2f inset). **b**, The spiral phase obtained with $A = 0.10$ and $D_{\perp} = 0.60$. The color corresponds to S^z of each spin. The integrated spin solid angle $|\Omega_{\text{tot}}|$ becomes finite in the SkX phase but becomes zero in the spiral phase (Fig. 2f).



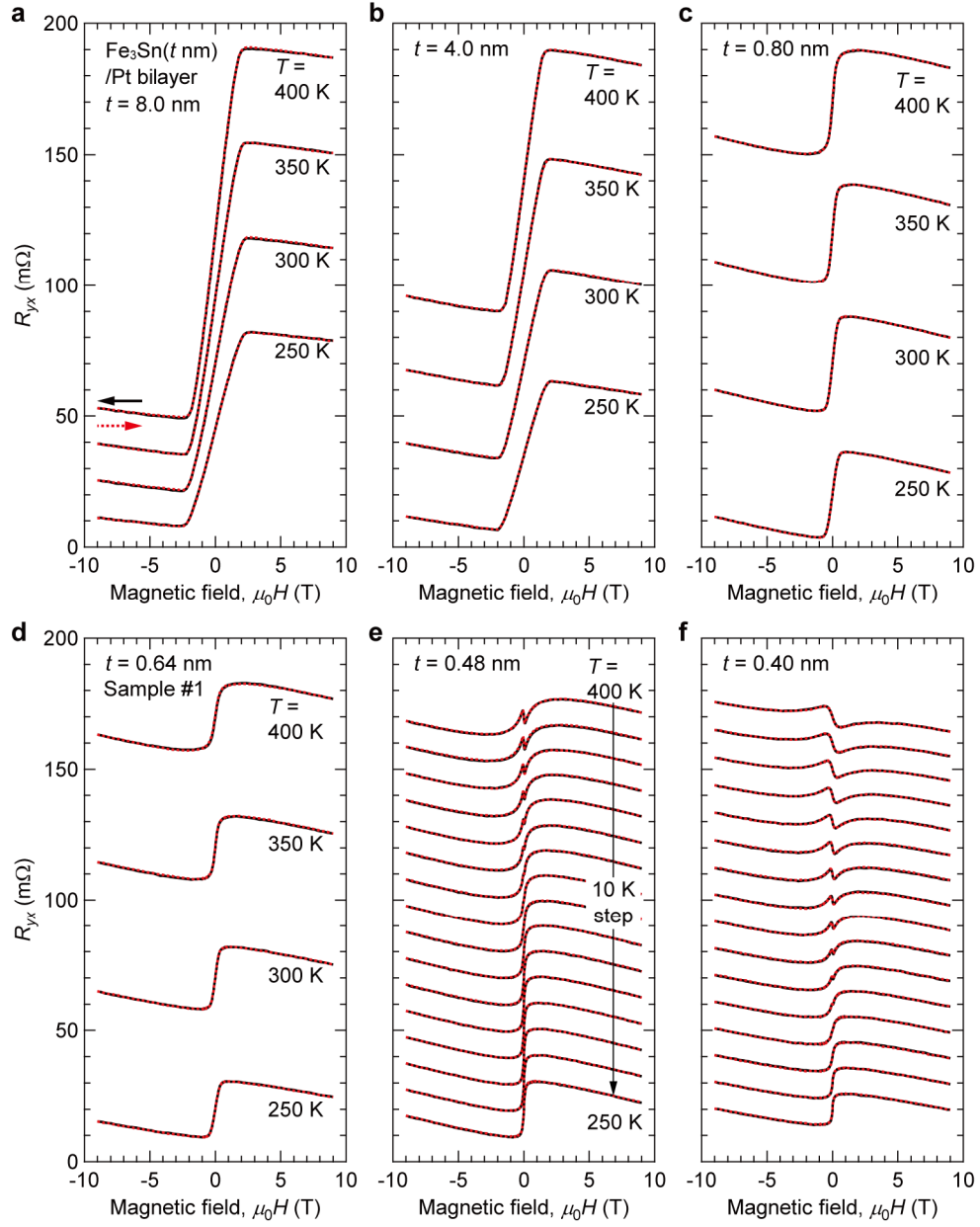
Supplementary Figure 8. Normalized magnetization M/M_{sat} versus $\mu_0 H$ curves. a, $\text{Fe}_3\text{Sn}(0.40 \text{ nm})/\text{Pt}$ thin-bilayer and **b,** $\text{Fe}_3\text{Sn}(0.40 \text{ nm})/\text{Pt}$ thin-trilayer structures measured in out-of-plane and in-plane H configurations at $T = 300$ K. The solid and dashed curves correspond to the decreasing-field and increasing-field branches, as shown by the black solid and dashed arrows, respectively.



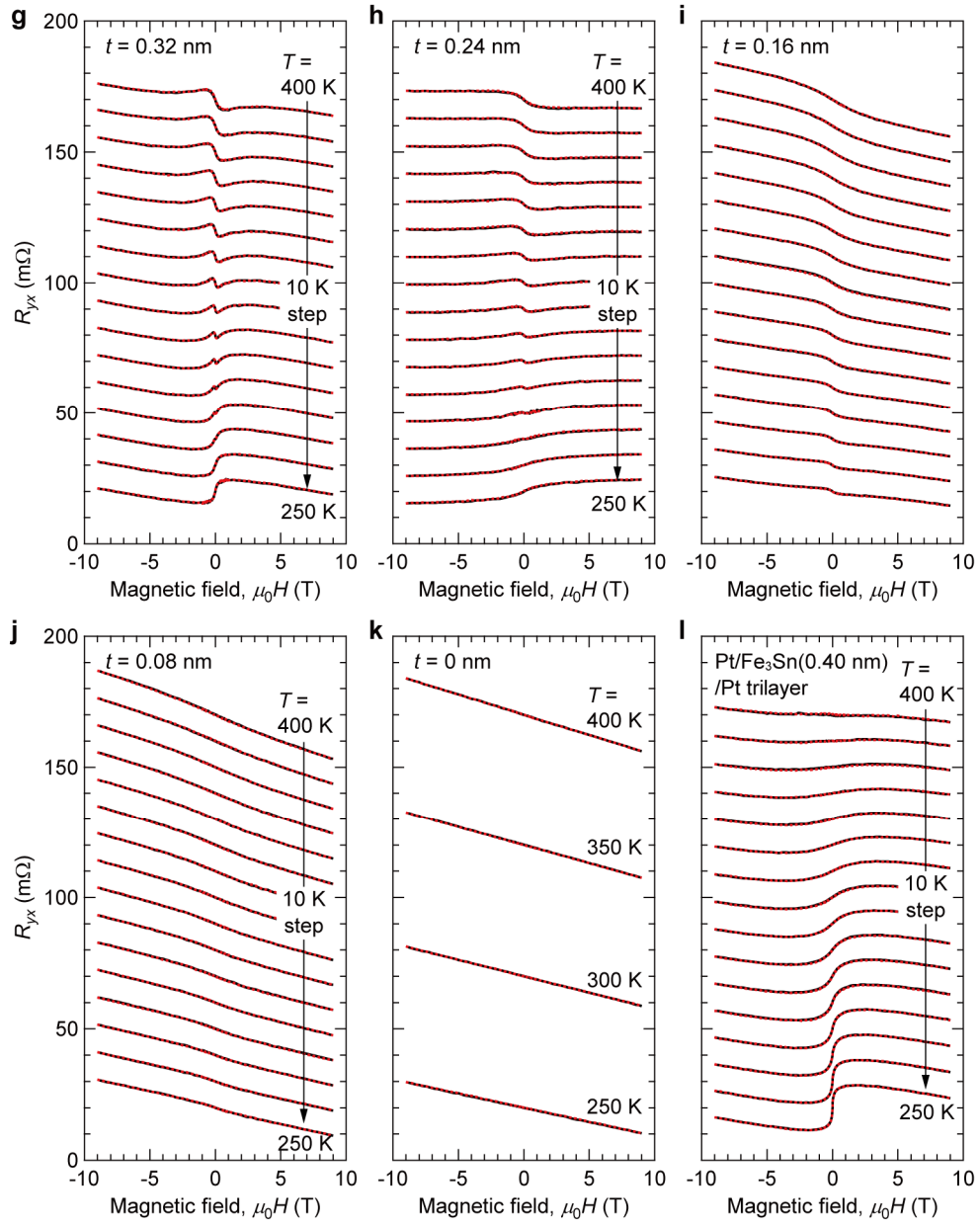
Supplementary Figure 9. t dependence of sheet resistance R_s at $T = 300$ K in $\text{Fe}_3\text{Sn}/\text{Pt}$ bilayer samples. The inset shows the data for $t = 0$ – 0.80 nm. Using the data for $t = 0$ nm (bare 10-nm-thick Pt without Fe_3Sn), the electrical resistivity of Pt is calculated to be 1.48×10^{-5} Ω cm. The virtually t -independent R_s indicates that the 10-nm-thick Pt bottom layer is significantly more conductive than the Fe_3Sn layer.



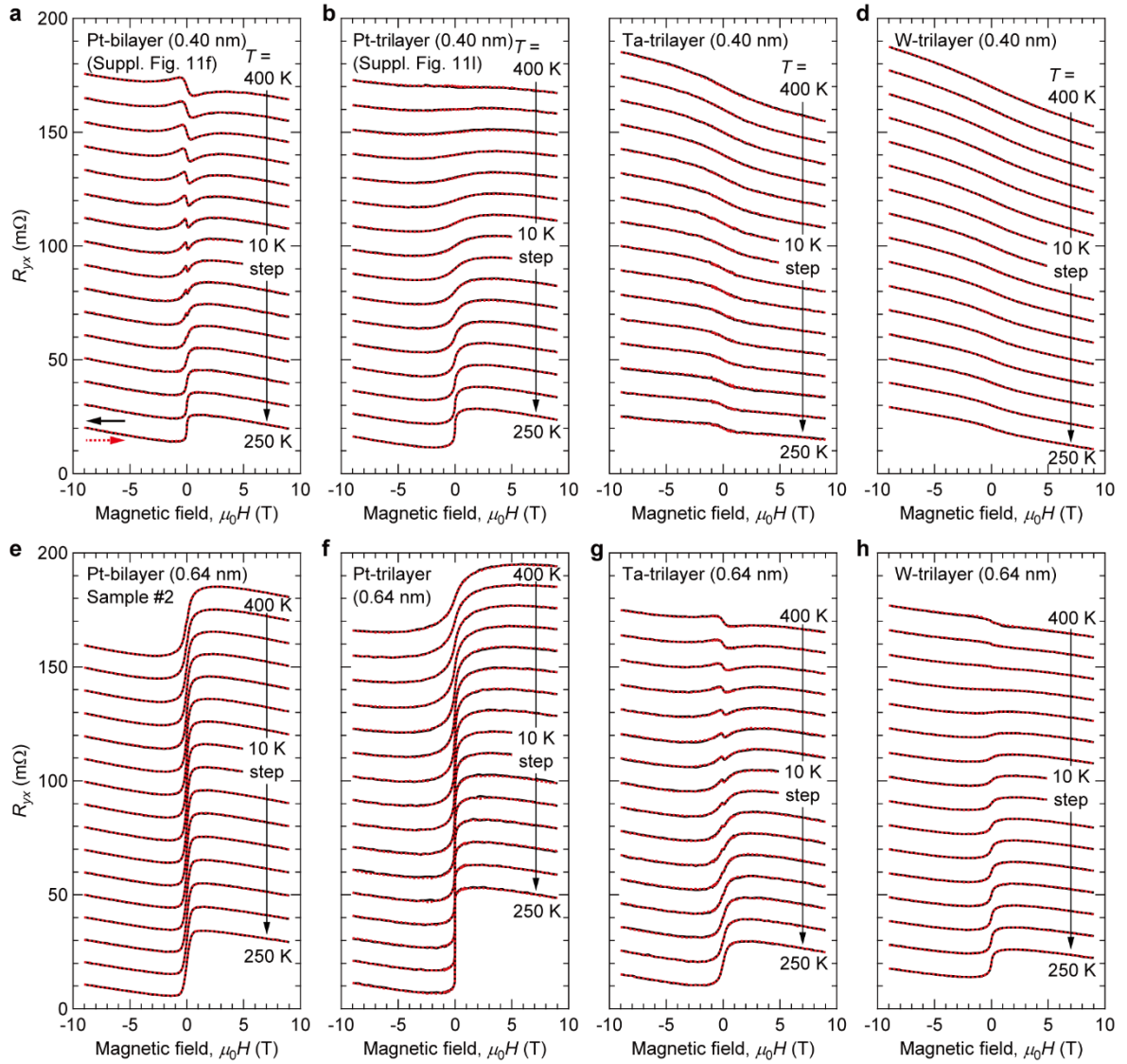
Supplementary Figure 10. Magnetoresistance MR versus $\mu_0 H$ curves at varied T . $\text{Fe}_3\text{Sn}(t \text{ nm})/\text{Pt}$ bilayer samples with **a**, $t = 0.48 \text{ nm}$, **b**, $t = 0.40 \text{ nm}$, and **c**, $t = 0.32 \text{ nm}$. MR is defined as $\text{MR} = \frac{R_{xx} - R_{xx,0 \text{ T}}}{R_{xx,0 \text{ T}}}$, where R_{xx} is the longitudinal resistance at a given field and $R_{xx,0 \text{ T}}$ is that at $\mu_0 H = 0 \text{ T}$. The R_{xx} was simultaneously measured with R_{yx} upon decreasing $\mu_0 H$ from 9 T to -9 T and increasing $\mu_0 H$ from -9 T to 9 T. By symmetrizing the decreasing-field and increasing-field R_{xx} data, the symmetrized MR curves were obtained. The two curves corresponding to the decreasing-field and increasing-field scans are shown, which are represented by black solid and red dotted curves, respectively. The data are shifted vertically for clarity. The MR is as small as 0.1%. The spike-like behavior at about $\pm 1 \text{ T}$ might be associated with the change in the field-sweep rate at $\pm 1 \text{ T}$.



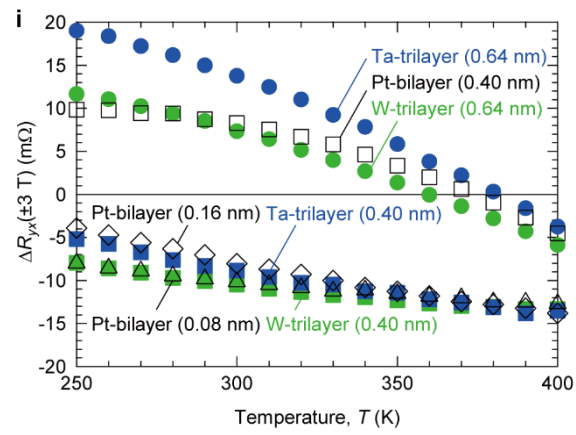
Supplementary Figure 11. R_{yx} versus $\mu_0 H$ curves at varied T . The two curves corresponding to the decreasing-field and increasing-field scans are shown, which are represented by black solid and red dotted curves, respectively. The data are shifted vertically for clarity. $\text{Fe}_3\text{Sn}(t \text{ nm})/\text{Pt}$ bilayer samples with **a**, $t = 8.0 \text{ nm}$, **b**, $t = 4.0 \text{ nm}$, **c**, $t = 0.80 \text{ nm}$, **d**, $t = 0.64 \text{ nm}$ (sample #1), **e**, $t = 0.48 \text{ nm}$, and **f**, $t = 0.40 \text{ nm}$.



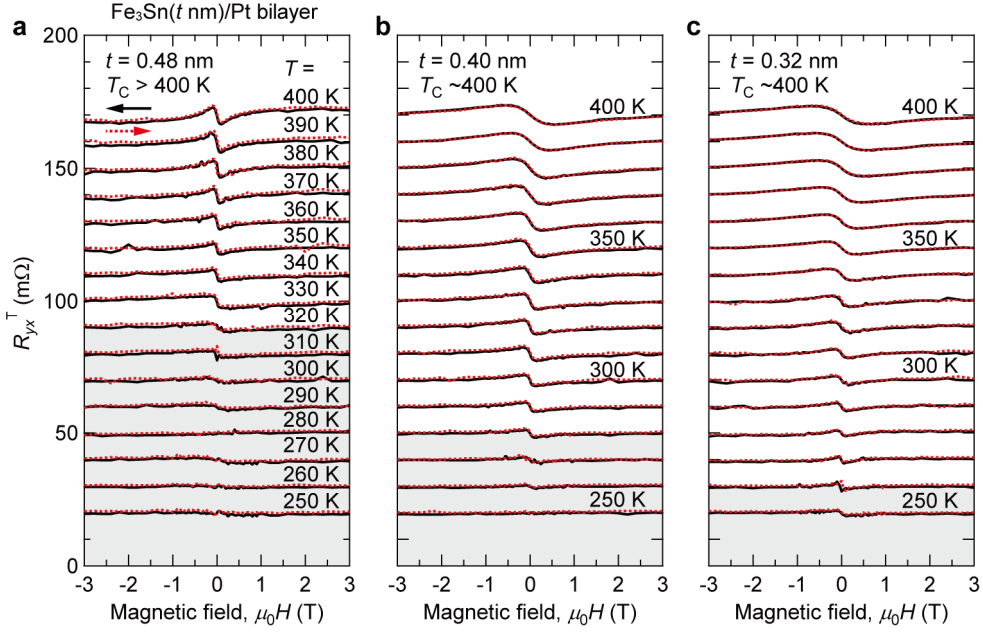
(Continued) Supplementary Figure 11. **g**, $t = 0.32$ nm, **h**, $t = 0.24$ nm, **i**, $t = 0.16$ nm, **j**, $t = 0.08$ nm, and **k**, $t = 0$ nm (Pt monolayer). **l**, Pt/Fe₃Sn($t = 0.40$ nm)/Pt trilayer. The AHE behavior is very similar to that of a Fe₃Sn($t = 0.40$ nm)/Pt bilayer (Supplementary Fig. 11f) but no THE-like responses occur at all measured T .



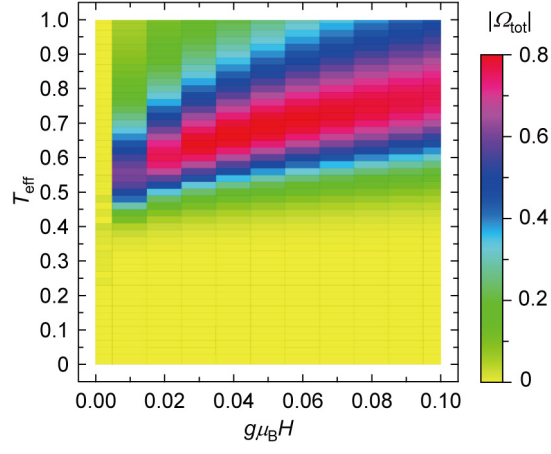
Supplementary Figure 12. R_{yx} versus μ_0H curves at varied T . The two curves corresponding to the decreasing-field and increasing-field scans are shown, which are represented by black solid and red dotted curves, respectively. The data are shifted vertically for clarity. **a**, $\text{Fe}_3\text{Sn}(t \text{ nm})/\text{Pt}$ bilayer (Pt-bilayer), **b**, symmetric $\text{Pt}/\text{Fe}_3\text{Sn}/\text{Pt}$ trilayer (Pt-trilayer), **c**, asymmetric $\text{Ta}/\text{Fe}_3\text{Sn}/\text{Pt}$ trilayer (Ta-trilayer), **d**, asymmetric $\text{W}/\text{Fe}_3\text{Sn}/\text{Pt}$ trilayer (W-trilayer) samples with $t = 0.40 \text{ nm}$, **e**, $\text{Fe}_3\text{Sn}/\text{Pt}$ bilayer, **f**, symmetric $\text{Pt}/\text{Fe}_3\text{Sn}/\text{Pt}$ trilayer, **g**, asymmetric $\text{Ta}/\text{Fe}_3\text{Sn}/\text{Pt}$ trilayer, **h**, asymmetric $\text{W}/\text{Fe}_3\text{Sn}/\text{Pt}$ trilayer samples with $t = 0.64 \text{ nm}$.



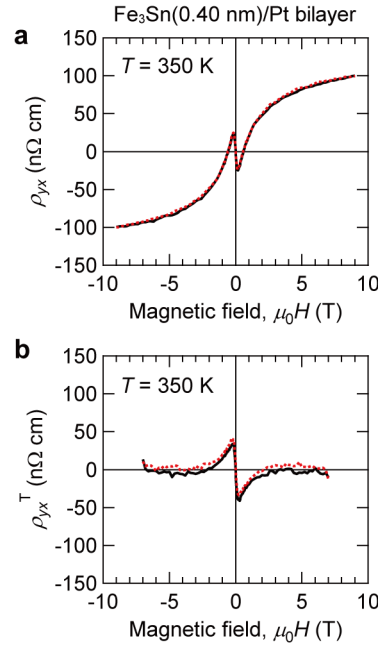
(Continued) Supplementary Figure 12. i, T dependence of $\Delta R_{yx}(\pm 3 \text{ T})$. See Supplementary Note 1 for the explanations about these results.



Supplementary Figure 13. a,b,c, R_{yx}^T versus μ_0H curves obtained by analyzing the data shown in Figs. 4a, b, and c, respectively. The two curves corresponding to the decreasing-field and increasing-field scans are shown, which are represented by black solid and red dotted curves, respectively. The data are shifted vertically for clarity. The grey-shaded regions represent the T range where no clear THE signals are discerned; THE-like behavior may also be seen at $T = 320$ K for $t = 0.48$ nm, $T = 280$ K for $t = 0.40$ nm, and $T = 260$ K for $t = 0.32$ nm. We focused on the data showing clear humps both in the raw R_{yx} and the analyzed R_{yx}^T in the discussion of THE.



Supplementary Figure 14. Simulated $|\Omega_{\text{tot}}|$ as a function of $g\mu_B H$ and T_{eff} . The simulation conditions are the same to that used for Fig. 4f.



Supplementary Figure 15. Calculation of topological Hall resistivity ρ_{yx}^T . **a**, Hall resistivity ρ_{yx} of the Fe₃Sn layer. For the analysis, the data of the Fe₃Sn($t = 0.40$ nm)/Pt bilayer and reference Pt monolayer samples at $T = 350$ K shown in Supplementary Figs. 11f and 11k were used. **b**, Calculated ρ_{yx}^T . The ρ_{yx}^T was calculated by subtracting the ordinary Hall resistivity $R_0\mu_0H$ and anomalous Hall resistivity (proportional to M) components from the ρ_{yx} . The two curves corresponding to the decreasing-field and increasing-field scans are shown, which are represented by black solid and red dotted curves, respectively.

Supplementary Table

Supplementary Table 1. $|\rho_{yx}^T|$, R_0 , $n_{\text{sk}}^{-0.5}$, the temperature where THE appears (T_{THE}).
The data were taken from the data of interface systems in literatures. $\rho_{yx}^T = PR_0 n_{\text{sk}} \phi_0$

Interface	$ \rho_{yx}^T $ ($\mu\Omega$ cm)	R_0 ($\text{cm}^3 \text{C}^{-1}$)	$n_{\text{sk}}^{-0.5}$ (nm)	T_{THE} (K)	Suppl. Ref.
SrRuO ₃ /SrIrO ₃	0.10–1.1	$6.6\text{--}8.1 \times 10^{-4}$	4.7–15	5–120	1
MnGa/Pt(5 nm)	1.2 at 300 K	8.57×10^{-3}	35 at 300 K	5–300	2
MnGa/Ta(5 nm)	2.7 at 300 K	1.33×10^{-3}	10 at 300 K	5–300	2
Ir/Fe/Co/Pt	0.0042 at 300 K	-6.2×10^{-5}	270 at 300 K	5–300	3
Fe ₃ Sn(0.40 nm)/Pt	0.037 at 350 K	8.48×10^{-5}	9.68–30.6 at 350 K	290–400	This work

Supplementary Note

Supplementary Note 1:

Asymmetric Ta (2 nm)/Fe₃Sn (t nm)/Pt (10 nm) and W (2 nm)/Fe₃Sn (t nm)/Pt (10 nm) trilayer structures (t -nm-thick Ta-trilayer and W-trilayer) were fabricated on Al₂O₃(0001) substrates. The Ta and W capping layers were deposited at the substrate temperature of 100 °C, which is the same condition for the deposition of Pt capping layer. The topmost surfaces were capped with SiO_x (15 nm) layers as in the Fe₃Sn (t nm)/Pt bilayer and symmetric Pt/Fe₃Sn (t nm)/Pt trilayer structures (t -nm-thick Pt-bilayer and Pt-trilayer). In Supplementary Fig. 12, we compare the Pt-bilayer and trilayer structures with identical t values (see (a)–(d) for $t = 0.40$ nm and (e)–(h) for $t = 0.64$ nm). In (c,d) the 0.40-nm-thick Ta- and W-trilayer structures, AHE is not obvious even at $T = 250$ K; the overall behavior looks those of the 0.16- or 0.08-nm-thick Pt-bilayer structures (see the panel (i)). In the thicker (g,h) 0.64-nm-thick Ta- and W-trilayer structures, AHE occurs clearly; the magnitude and T dependence are closer to those of (a) the 0.40-nm-thick Pt-bilayer and (b) 0.40-nm-thick Pt-trilayer structures rather than (e) the 0.64-nm-thick Pt-bilayer and (f) 0.64-nm-thick Pt-trilayer structures. These results indicate that the effective Fe₃Sn thickness in the Ta- and W-trilayer structures is reduced by approximately 0.2–0.3 nm as compared with the cases using SiO_x and Pt capping layers. Interdiffusion might be more significant at the interfaces of Ta/Fe₃Sn and W/Fe₃Sn. Taking into account the reduced effective Fe₃Sn thickness, we focused on the 0.64-nm-thick Ta-and W-trilayer structures as the control samples of the 0.40-nm-thick Pt-bilayer and 0.40-nm-thick Pt-trilayer structures for which the occurrence of THE by the interfacial DMI is discussed in the manuscript.

In the 0.64-nm-thick Ta-trilayer structure, R_{yx} humps (R_{yx}^T) appear at low $\mu_0 H$ in the range of $T = 300$ – 400 K. In the 0.64-nm-thick W-trilayer structure, no clear humps are detected except for $T = 400$ K. These results can be explained by considering the different strengths of interfacial DMI at the top and bottom interfaces. It has been reported that the interfacial DMI of W for Fe [A. Belabbes *et al.*, *Phys. Rev. Lett.* **117**, 247202 (2016)] and CoFeB [I. Gross *et al.*, *Phys. Rev. B* **94**, 064413 (2016)] is as strong as that of Pt and has the same sign. Hence, as in the symmetric Pt/Fe₃Sn/Pt trilayer structure, the opposite interfacial DMI contributions from the top W/Fe₃Sn and bottom Fe₃Sn/Pt interfaces in the W/Fe₃Sn/Pt trilayer structure are expected to suppress each other. On the other hand, the interfacial DMI of Ta is known to be much weaker than Pt [A. Casiraghi *et al.*, *Commun. Phys.* **2**, 145 (2019)]. In the Ta/Fe₃Sn/Pt trilayer structure, the effective interfacial DMI should be governed by the large contribution from the bottom Fe₃Sn/Pt interface. Therefore, these results add further support for the interfacial DMI origin of the observed THE.

Supplementary References

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2. Meng, K. *et al.* Robust emergence of a topological Hall effect in MnGa/heavy metal bilayers. *Phys. Rev. B* **97**, 060407(R) (2018).
3. Raju, M. *et al.* The evolution of skyrmions in Ir/Fe/Co/Pt multilayers and their topological Hall signature. *Nat. Commun.* **10**, 696 (2019).
4. Belabbes, A., Bihlmayer, G., Bechstedt, F., Blügel, S. & Manchon, A. Hund's Rule-Driven Dzyaloshinskii-Moriya Interaction at 3d-5d Interfaces. *Phys. Rev. Lett.* **117**, 247202 (2016).
5. Gross, I. *et al.* Direct measurement of interfacial Dzyaloshinskii-Moriya interaction in X[CoFeB|MgO] heterostructures with a scanning NV magnetometer (X=Ta, TaN, and W). *Phys. Rev. B* **94**, 064413 (2016).
6. Casiraghi, A. *et al.* Individual skyrmion manipulation by local magnetic field gradients. *Commun. Phys.* **2**, 145 (2019).