

I. SUPPLEMENTARY TABLES

Supplementary Table I. Table documenting processing time for various steps throughout the data acquisition and analysis pipeline.

Process	Software	Time/Sample (Minutes)	# Samples	Total Time (hours)
Morphometer Extraction	ImageJ	0.038	4250	2.69
Finite Element Analysis	MOOSE	73.08	654	796.57
Sample Concatenation	Python	0.006	654	0.07
Grid Search Optimization	Python, MATLAB	0.074	600	0.74
Final Model Training	MATLAB	0.002	600	0.02

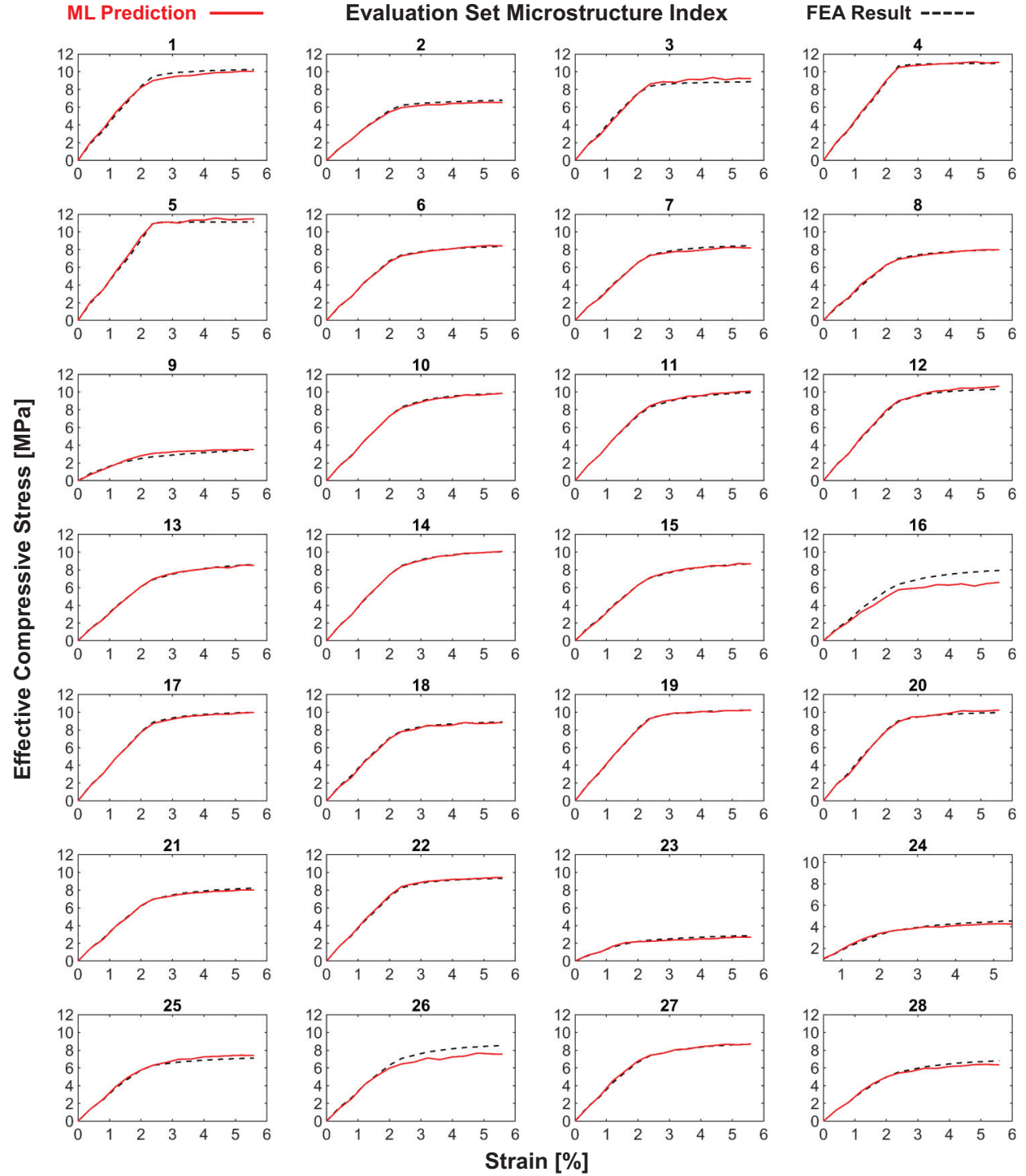
Supplementary Table II. Table documenting data sources used for base CT scans.

Data Source	Description
Eckley ¹	4D Imaging of Acid Leaching in Porous Carbonado Diamond
Mascini ²	4D micro-CT imaging of oil and waterflood in water and mixed-wet complex sandstones
Neumann ³	11 Sandstones: raw, filtered and segmented data
Mohammadmoradi ⁴	A Micro CT Image of Tight Carbonate
Ivonin ⁵	A MicroCT Image of Silty Loam Phaeozem Albic
Mohammadmoradi ⁶	A Multiscale Sandy Microstructure
Rucker ⁷	A Time-Resolved Synchrotron X-Ray Micro-Tomography Dataset of a Waterflood in an Altered Mixed-Wet Ketton Limestone
Heidari ⁸	Austin Chalk
Bultreys ⁹	Belgian Fieldstone
Ferreira ¹⁰	Carbonates: Porosity and Permeability Voxel to Voxel
Lin ¹¹	Data for Pore-Scale Imaging of Displacement Patterns in an Altered-Wettability Carbonate
Wang ¹²	Dataset for Unsteady-State Capillary Drainage experiment on Estailades Carbonate
Andrew ¹³	Doddington Sandstone
Ni ¹⁴	Drainage Experiment in an Intermediate-Scale Beadpack
Bultreys ¹⁵	Estailades Carbonate #2
Crandall ¹⁶	Foamed Cement API RP 10B-4
Ketcham ¹⁷	Fracture in Granite
Luo ¹⁸	Fracture Patterns in Laminated Mancos Shale
Berg ¹⁹	Gildehauser Sandstone
Chen ²⁰	Grain-scale Failure Mechanism of a Porous Sandstone in Brazilian Tensile Test
Chen ²¹	Hydrate-Bearing Sand
Karpyn ²²	Induced Rough Fracture in Berea Sandstone Core
Moon ²³	Intergranular Pore Structures in Sandstones
Dalton ²⁴	Laboratory Foamed-Cement-Curing Evolution Using CT Scanning: Insights from Elevated-Pressure Generation
Bultreys ²⁵	Massangis Jaune Carbonate
Patmonoajji ²⁶	Micro-tomographic Imaging of the Dissolution of Trapped Nitrogen Gas with and without Dissolution Fingering
Beckingham ²⁷	Paluxy Sandstone
Pradanovic ²⁸	Partially Cemented Tight Sandstone Fracture
Khan ²⁹	Particulate Straining in Simple Porous Media
Karpyn ³⁰	Pore Scale Multiphase Flow Experiments in Bead Packs of Variable Wettability
Dalton ³¹	Sessile Drop and Micro-CT Data for Six Sandstone Formations
Mehmani ³²	Wilcox Tight Gas Sandstone
Saur ³³	X-ray Micro-CT Images of Calcareous Shale Samples

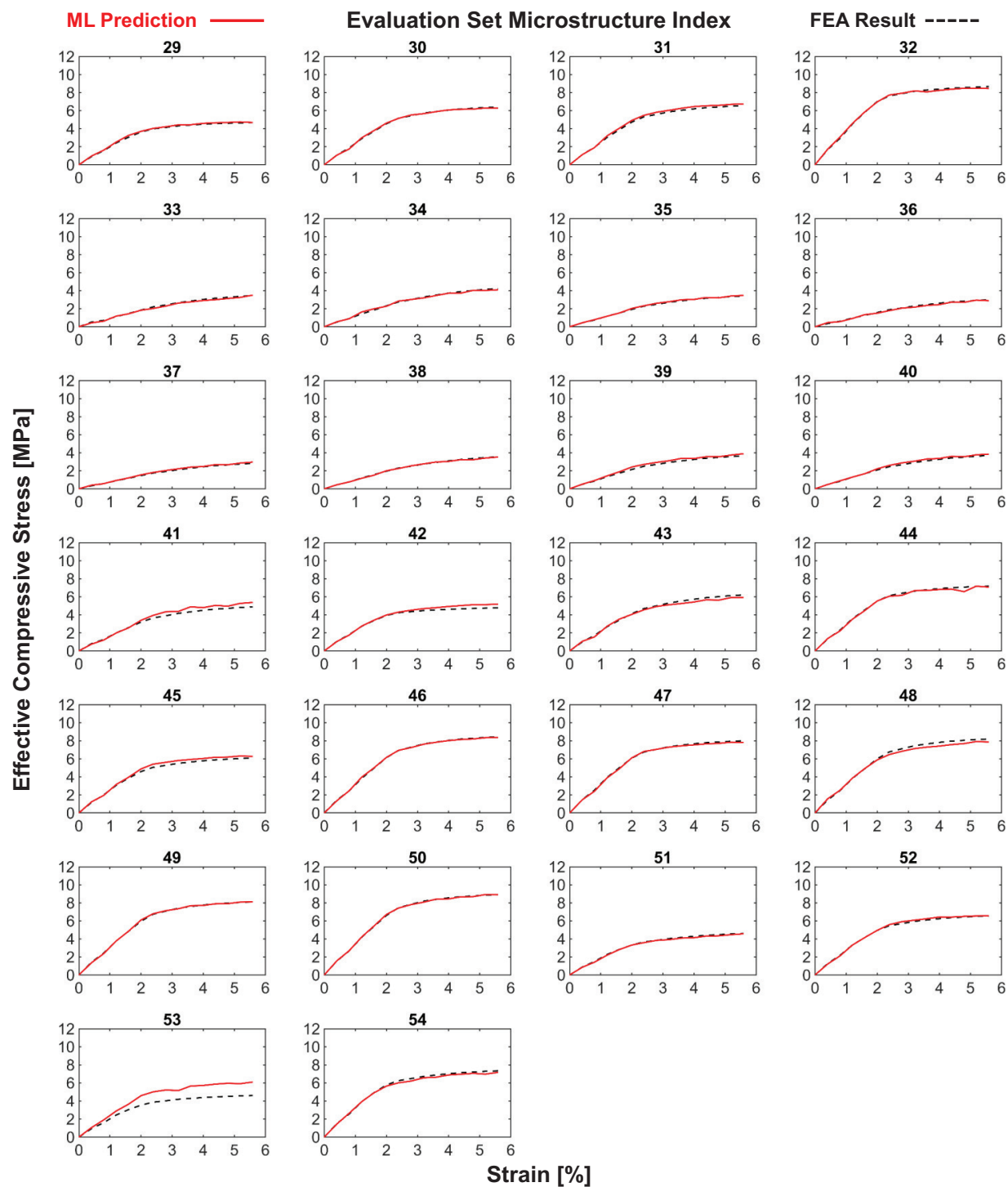
Supplementary Table III. Table indicating which extracted geometric features were compared against Minkowski functionals.

Feature Name	Description
Volume Density	Shape volume normalized by total volume of the sampling window
Surface Area Density	Shape surface area normalized by total volume of the sampling window
Mean Breadth Density	Average of caliper diameter over all directions normalized by total volume of the sampling window
Euler Number Density	Euler number of the shape normalized by total volume of the sampling window
Grain Count	Number of grains in 3D reconstruction
Volume	Number of voxels in 3D reconstruction multiplied by volume of one voxel
Surface Area	Surface area of shape
Mean Breadth	Average caliper diameter over all directions
Sphericity	Ratio of squared volume over the cube of the surface area
Euler Number	Descriptor of region topology (connected components minus number of holes)
Box X. Min.	Smallest Feret diameter in the X direction
Box X. Max.	Largest Feret diameter in the X direction
Box Y. Min.	Smallest Feret diameter in the Y direction
Box Y. Max.	Largest Feret diameter in the Y direction
Box Z. Min.	Smallest Feret diameter in the Z direction
Box Z. Max.	Largest Feret diameter in the Z direction
Centroid X	X-coordinate of the shape centroid
Centroid Y	Y-coordinate of the shape centroid
Centroid Z	Z-coordinate of the shape centroid
Ellipse Center X	X-coordinate of the inertial ellipse centroid
Ellipse Center Y	Y-coordinate of the inertial ellipse centroid
Ellipse Center Z	Z-coordinate of the inertial ellipse centroid
Ellipsoid Radius 1	Length of the largest semi-axis of the inertial ellipse
Ellipsoid Radius 2	Length of the medium semi-axis of the inertial ellipse
Ellipsoid Radius 3	Length of the smallest semi-axis of the inertial ellipse
Ellipsoid Azimuth	Azimuth of the projection of the major axis on the XY plane of the inertial ellipse, in degrees
Ellipsoid Elevation	Elevation of the major axis on the XY plane of the inertial ellipse, in degrees
Ellipsoid Roll	Rotation of the inertial ellipsoid around the main axis, in degrees
Ellipsoid R1/R2	Ratio of Radius 1 to Radius 2 of the inertial ellipse
Ellipsoid R1/R3	Ratio of Radius 1 to Radius 3 of the inertial ellipse
Ellipsoid R2/R3	Ratio of Radius 2 to Radius 3 of the inertial ellipse
Inscribed Ball X	The X-coordinate of the mean largest sphere that can fit in a corresponding grain
Inscribed Ball Y	The Y-coordinate of the mean largest sphere that can fit in a corresponding grain
Inscribed Ball Z	The Z-coordinate of the mean largest sphere that can fit in a corresponding grain
Inscribed Ball Radius	The mean radius of the largest sphere that can fit in a corresponding grain

II. SUPPLEMENTARY FIGURES



Supplementary Figure 1. Predicted and simulated compressive stress-strain curves for evaluation set samples 1-28.



Supplementary Figure 2. Predicted and simulated compressive stress-strain curves for evaluation set samples 29-54.

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