

Theorem 1. All of the substrings can be obtained.

Proof. We know that all of the substrings are the prefix of some suffixes. For any substring S , suppose that $Suffix[i]$ is the smallest suffix of all the suffixes which have the prefix of S . $Suffix[SA[Rank[i] - 1]]$ is smaller than $Suffix[i]$ so it does not contain S as a prefix. In addition, $LCP[i]$ must be smaller than the length of S . As a result, with the situation that substring S is a prefix of $Suffix[i]$ and the length of S is larger than $LCP[i]$, substring S can be generated by $Suffix[i]$ by Property 1. End of proof.

Theorem 2. No two obtained substrings are the same.

Proof. Let i and k be the positions of the two copies of the repeated substring S , and assume that $Rank[i] < Rank[k]$. If $Rank[i] + 1 == Rank[k]$ then property 2 is violated. Otherwise, all suffixes j with $Rank[j]$ between $Rank[i]$ and $Rank[k]$ must have prefix S , and hence $lcp(Suffix[SA[Rank[k]-1]], Suffix[k]) \geq \text{length}(S)$, violating property 2. End of proof.